# Probing gravity in the strong field regime

Jason Hessels on behalf of Anne Archibald

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# LETTER

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# Universality of free fall from the orbital motion of a pulsar in a stellar triple system

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Einstein's theory of gravity—the general theory of relativity<sup>1</sup>—is based on the universality of free fall, which specifies that all objects accelerate identically in an external gravitational field. In contrast to almost all alternative theories of gravity<sup>2</sup>, the strong equivalence principle of general relativity requires universality of free fall to apply even to bodies with strong self-gravity. Direct tests of this principle using Solar System bodies<sup>3,4</sup> are limited by the weak selfgravity of the bodies, and tests using pulsar–white-dwarf binaries<sup>5,6</sup> have been limited by the weak gravitational pull of the Milky Way. PSR J0337+1715 is a hierarchical system of three stars (a stellar triple system) in which a binary consisting of a millisecond radio pulsar and a white dwarf in a 1.6-day orbit is itself in a 327-day orbit nonlinearity of gravity, and  $\gamma$ , which measures the degree to which gravity curves space-time. Both of these parameters take the value 1 in general relativity. We chose a point-particle Lagrangian that permits arbitrarily strong gravity internal to the bodies and parameterized post-Newtonian interactions between them<sup>10</sup>. We then used computer algebra<sup>11</sup> to construct equations of motion. Each orbit was specified by an initial system configuration at modified Julian date (MJD) 55,920.0 (2011 December 25 00:00 UTC). The evolution of this configuration was governed by  $\beta$ ,  $\gamma$  and the strong equivalence principle (SEP)violation parameter  $\Delta$ . Because the self-gravity of the pulsar (which is a neutron star) exceeds that of the white dwarfs by a factor 10<sup>4</sup> and the SEP violation that we seek arises from self-gravity, we neglect possi-

# "Pulsar Timing"

## Using pulsars as precision clocks



Receive and record pulses

Stack pulses to get high S/N

54255.1231254524233 54255.2643443523453 54255.3123524545899 54255.3513745623467 54255.4418456543355 54255.5001234234688

Measure the pulse arrival times

# **Pulsar Timing Model**



## What does this teach us?

#### Model is complete!



## Count each pulse... for years.

PSR J1012+5307: P = 0.005255749014115410 +/- 0.00000000000000015s

> 100 billion pulses in the last 15 years, and not a single one missed

# **Pulsar binary**

# **Pulsar Recycling**

Alpar, Cheng, Ruderman & Shaham 1982

Rhadakrishnan & Srinivasan 1982



LMXB (some IMXB) Radio (some also g-ray)

# Millisecond pulsars are the products of astrophysical accretion

# Keplerian Timing Effects



Need mass function + two other equations for m1, m2, and i

# **Post-Keplerian Effects**

Periastron adv. 
$$\dot{\omega} = 3 \left(\frac{P_b}{2\pi}\right)^{-5/3} (T_{\odot}M)^{2/3} (1-e^2)^{-1}$$

Grav. redshift 
$$\gamma = e \left( rac{P_b}{2\pi} 
ight)^{1/3} T_{\odot}^{2/3} \, M^{-4/3} \, m_2 \, (m_1 + 2m_2)$$

= 10

**Orbital decay** 

$$\dot{P_b} = -\frac{192\pi}{5} \left(\frac{P_b}{2\pi}\right)^{-5/3} \left(1 + \frac{73}{24}e^2 + \frac{37}{96}e^4\right) (1 - e^2)^{-7/2} T_{\odot}^{5/3} m_1 m_2 M^{-1/3}$$
$$r = T_{\odot} m_2 \quad \text{"Range"}$$

Shapiro

s = 
$$x \left(\frac{P_b}{2\pi}\right)^{-2/3} T_{\odot}^{-1/3} M^{2/3} m_2^{-1}$$
. = Sin i "Shape"

"Range"

Depend on m1, m2, and the Keplerian parameters Measure any 2 PK params and get m1, m2

# **Nobel Prize Physics 1993**



Russell Hulse & Joseph Taylor

"for the discovery of a new type of pulsar, a discovery that has opened up new possibilities for the study of gravitation"







# Pulsar riddle

## PSR J0337+1715



# **Pulsar riddle**

## PSR J0337+1715









Tauris & van den Heuvel (2014)

# **Pulsar riddle**

## PSR J0337+1715

Dynamical interactions between the two nested binaries



# **Pulsar riddle**

## PSR J0337+1715



Work done by Anne Archibald, directly integrating the motions of the 3 bodies

## J0337+I7I5 - Timing model

Parameter	Symbol	Value				
Fixed	values	Value				
Bight ascension	RA	$03^{h}37^{m}43^{s}82589(13)$				
Declination	Dec	17°15′14″ 828(2)				
Dispersion measure	DM	$21.3162(3) \text{ pc cm}^{-3}$				
Solar system ephemeris	2	DE405				
Reference epoch		MJD 55920.0				
Observation span		MJD 55930.9 - 56436.5				
Number of TOAs		26280				
Weighted root-mean-squared residual		1.34 µs				
Fitted p	arameters					
Spin-dowr	parameters					
Pulsar spin frequency	f	365.953363096(11) Hz				
Spin frequency derivative	Ġ	$-2.3658(12) \times 10^{-15} \text{ Hz s}^{-1}$				
Inner Keplerian para	meters for pulsar	orbit				
Semimajor axis projected along line of sight	$(a \sin i)_I$	1.21752844(4) lt-s				
Orbital period	$P_{b,I}$	1.629401788(5) d				
Eccentricity parameter $(e \sin \Omega)$	$\epsilon_{1,I}$	$6.8567(2) \times 10^{-4}$				
Eccentricity parameter $(e \cos \Omega)$	$\epsilon_{2,I}$	$-9.171(2) \times 10^{-5}$				
Time of ascending node	$t_{asc,I}$	MJD 55920.407717436(17)				
Outer Keplerian parameters for	or centre of mass	of inner binary				
Semimajor axis projected along line of sight	$(a \sin i)_O$	74.6727101(8) lt-s				
Orbital period	$P_{b,O}$	327.257541(7) d				
Eccentricity parameter $(e \sin \Omega)$	$\epsilon_{1,O}$	$3.5186279(3) \times 10^{-2}$				
Eccentricity parameter ( $e \cos \Omega$ )	$\epsilon_{2,O}$	$-3.462131(11) \times 10^{-3}$				
Time of ascending node	$t_{asc,O}$	MJD 56233.935815(7)				
Interaction	parameters					
Semimajor axis projected in plane of sky	$(a \cos i)_I$	1.4900(5) It-s				
Semimajor axis projected in plane of sky	$(a\cos i)_O$	91.42(4) It-s				
Inner companion mass over pulsar mass	$q_I = m_{cI}/m_p$	0.13737(4)				
Difference in longs. of asc. nodes		$2.7(6) \times 10^{-0.00}$				
Pulsar	proportios					
Pulsar pariod		2 72258862244(0) mc				
Rulear period derivative	ı D	$1.7666(0) \times 10^{-20}$				
Inforred surface dipole magnetic field	Г Р	$1.7000(9) \times 10^{-10}$				
Spin down newer	D Ė	$2.2 \times 10^{-1}$				
Characteristic age	E -	3.4 × 10° erg s				
Orbital	acomotry	$2.3 \times 10$ y				
Pulsar semimaior axis (inner)	geometry	1.0242(4) lt-e				
Eccentricity (inner)	a <sub>I</sub> eı	$6.0178(2) \times 10^{-4}$				
Longitude of periastron (inner)	61	0.5176(2) × 10				
Pulsar semimaior axis (outer)	ω <sub>1</sub> 0.0	118 04(3) It-s				
Eccentricity (outer)	eo	$353561955(17) \times 10^{-2}$				
Longitude of periastron (outer)	ωο	95.619493(19) °				
Inclination of invariant plane	i	39.243(11) °				
Inclination of inner orbit	i,	39.254(10) °				
Angle between orbital planes	$\delta_i$	$1.20(17) \times 10^{-2}$ °				
Angle between eccentricity vectors	$\delta_{\omega} \sim \omega_{\Omega} - \omega_{T}$	-1.9987(19) °				
Masses						
Pulsar mass	$m_{p}$	$1.4378(13) M_{\odot}$				
Inner companion mass	$m_{cI}^{\nu}$	$0.19751(15) M_{\odot}$				
Outer companion mass	$m_{cO}$	$0.4101(3) M_{\odot}$				

Pulsar mass: 1.4378(13) MSun "Inner" WD mass: 0.19751(15) MSun "Outer" WD mass: 0.4101(3) MSun





# **Strong Equivalence Principle**



All objects should fall with same acceleration regardless of their mass or composition

**Key idea:** test whether two bodies fall the same way in the gravitational field of a third **Need:** binary falling in an external gravitational field

- Earth and Moon falling in Sun's gravity (LLR)
- Pulsar-WD binary falling in Galactic potential (e.g. Gonzalez et al.)
- Triple system: pulsar and inner WD falling in gravity of outer WD



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### Observations

Tel.	Band	Num.	Hours	Date range
AO	1400	92	58.9	2012 Mar – 2017 Mar
GBT	1400	172	236.0	2012 Feb – 2017 May
WSRT	1400	439	836.7	2012 Jan – 2013 Jul
AO	430	36	12.9	2012 May – 2017 Mar
WSRT	350	20	17.3	2012 Feb – 2013 Jul







Arecibo Observatory (AO)

Green Bank Telescope (GBT)

No adequate formula is known for directly describing the three-body orbit, so we use direct integration of equations of motion:

$$F_j = M_{j,l} a_j, \tag{1}$$

and

$$F_j = -\sum_k \frac{GM_{j,G}M_{k,G}}{r_{jk}^2}\hat{r}_{jk}$$
(2)

A standard ODE solver allows us to calculate an orbit given initial conditions.

This scheme is easily adapted to allow gravitational mass different from inertial mass.

#### **Relativistic timing model**

- Nordtvedt (1985) derives a "point particle" Lagrangian
  - Taylor expansion around the Newtonian Lagrangian
  - Lorentz invariance and symmetry used to eliminate terms
  - Bodies may contain strong fields but internal structure is frozen
  - Fields away from bodies approximated to first post-Newtonian order
- Computer algebra straightforwardly yields equations of motion
  - Direct integration simulates orbits

$$\begin{split} L_{PPN} &= -\sum_{i} M_{i,i} \left( 1 - \frac{v_i^2}{2} - \frac{v_i^4}{8} \right) \\ &+ \frac{1}{2} \sum_{i,j} \frac{M_{i,G} M_{j,G}}{r_{ij}} \left( 1 + \frac{v_i^2 + v_j^2}{2} - \frac{3v_i \cdot v_j}{2} - \frac{(v_i \cdot \hat{r}_{ij})(v_j \cdot \hat{r}_{ij})}{2} \right) \\ &+ \frac{\gamma}{2} \sum_{i,j} \frac{M_{i,G} M_{j,G}}{r_{ij}} (v_i - v_j)^2 + \left( \frac{1}{2} - \beta \right) \sum_{i,j,k} \frac{M_{i,G} M_{j,G} M_{k,G}}{r_{ij} r_{ik}} \end{split}$$

#### **Testing the SEP**



In principle we simply:

- include  $\Delta$  in the timing model,
- fit timing model to TOAs, and
- determine best-fit values and uncertainties.

Ideally, the value of  $\Delta$  and its uncertainty would determine how well we constrain SEP violation and whether GR is violated.

But: only correct once we've accounted for all systematics, and formally the effects of  $\Delta$  are constrained at the 7 ns level.

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#### Known systematics

Cause	Remedy
Profile variation with frequency	TOAs no more than 20 MHz
Telescope polarization variations	Matrix template matching
Intrinsic profile variations	?
Interstellar DM variations	Variable DM fitting
Interplanetary medium effects	IPM fitting
Tidal effects in inner WD	Too small
GW losses	Too small
Red noise	Too small at freq. of interest
Uncertainty in DE435 ephemeris	Position fitting
Kopeikin and inverse parallax	Too small
Kabouters	?

We need to estimate the impact of unknown or poorly modeled systematics.

Key idea: look for structure in the residuals that looks like SEP violations.

SEP violation produces a shift in the pulsar's orbit toward the the outer companion: approximately a sinusoid with frequency  $2f_{inner} - f_{outer}$ .



#### The signature of an SEP violation

Key idea: look for structure in the residuals that looks like SEP violations.

SEP violation produces a shift in the pulsar's orbit toward the the outer companion: approximately a sinusoid with frequency  $2f_{inner} - f_{outer}$ .





### Wiggles in our residuals

Look at sinusoids with frequency  $kf_{inner} + lf_{outer}$ :



Estimate no more than  $\sim$ 77 ns in the SEP position based on distribution of all arrows.

When we carry out the basic fitting, we obtain

$$\Delta = (-1.1 \pm 0.2) imes 10^{-6}.$$

But: that's a  $\sigma$  corresponding to a 7 ns uncertainty. If we take into account all the wiggles we see in the data from our arrow plot we get a more realistic  $\sigma$  corresponding to a 22 ns uncertainty:

$$\Delta = (-1.1\pm0.7)\times10^{-6}$$

We conclude that our result agrees with General Relativity at the 1.6 $\sigma$  level.

With the best-fit value and uncertainty we computed, we can set a  $2\sigma$  upper limit on SEP violation. We can say that for a  $1.4378M_{\odot}$  neutron star, its acceleration differs from that of its white dwarf companion:

 $|\Delta| <$  2.6 imes 10<sup>-6</sup>

(Triple system)

Fundamentally, this difference in acceleration is the key quantity we limit. So we constrain any theory that predicts such an anomalous difference in acceleration, for example, Einstein-Aether or scalar-tensor theories.

But: how does our result compare to existing tests?

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(Triple system)

The wide pulsar-white-dwarf binary PSR J1713+0747 falling in the Galactic potential gives:

$$|\Delta| < 2 imes 10^{-3}$$
 (WB)

But: how do we compare this to lunar laser ranging or dipole gravitational wave tests?

#### The Nordtvedt parameter

In PPN we measure a theory's SEP violation by using the Nordtvedt parameter:

$$\Delta = \eta_N \frac{E_g}{Mc^2}$$

Lunar Laser Ranging constrains the Earth-Moon-Sun system to  $|\Delta| < 1.3 \times 10^{-13}$ , and for the Earth  $E_g/Mc^2 \sim -4.5 \times 10^{-10}$ , so  $|\eta_N| < 2.4 \times 10^{-4}$ .

In the triple system, the pulsar interior is not 1PN!

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We can calculate the "strong-field Nordtvedt parameter"  $\hat{\eta}_N$  the same way:

$$\Delta = \hat{\eta}_N \frac{E_g}{Mc^2}$$

Since  $|\Delta| < 2.6 \times 10^{-6}$  and  $E_g/Mc^2 \sim -0.1$ ,  $|\hat{\eta}_N| < 2.6 \times 10^{-5}$  — improving on LLR by a factor of about ten.

But: funny things can happen in the strong field!

These theories include a scalar field  $\phi$  in addition to the metric that mediates gravity. Matter responds to a modified version of the metric:

$$ilde{g}_{\mu
u}={e}^{2(lpha_0\phi+eta_0\phi^2/2)}g_{\mu
u}^*$$

The scalar field is sourced in matter:

$$\Box \phi = -\frac{4\pi G^*}{c^4} (\alpha_0 + \beta_0 \phi) T_*$$

If  $\beta_0 \lesssim -4$  spontaneous scalarization can occur, resulting in order-unity deviations from GR in strong fields, no matter how small the weak-field effects are.

#### Our constraint on quasi-Brans-Dicke theories



Our constraint  $|\Delta| < 2.6 \times 10^{-6}$  rules out the light-gray area.

## Universality of free fall



Tests the foundation on which Einstein's theory of gravity, general relativity, is built:

- Used I200hr of WSRT, GBT and Arecibo data to see if pulsar and white dwarf fall differently towards a 2nd white dwarf companion.
- Find equal accelerations to within a few parts in a million. Best-ever test of the strong equivalence principle:

Pulsar triple system PSR J0337+1715  $|\Lambda|$ 

Archibald, Gusinskaia, Hessels et al. 2018, Nature

 $|\Delta| < 2.6 \times 10^{-6}$ 

## **Does Extreme Gravity Change How Things Fall?** The Triple System PSR J0337+1715



The pulsar spins 366 times per second, sweeping beams of radio waves over the Earth

The pulsar's gravity is tremendous: the energy holding it together is about 10% of its mass (times  $c^2$ )

accelerate

Einstein predicts the accelerations should be the same.

Alternative theories of gravity mostly predict that the pulsar's extreme gravity should interact nonlinearly with the pull of the outer white dwarf and produce a *different* acceleration

Arecibo Observatory

level of three parts per million

Microsecond-accurate measurements of the arrival times of the radio pulses show

no difference between the accelerations of

the pulsar and the inner white dwarf at the



Green Bank Telescope



Westerbork Synthesis Radio Telescope

Universality of Free Fall from the Orbital Motion of a Pulsar in a Stellar Triple System Nature, 2018 July 5 Archibald, A. M., Gusinskaia, N. V., Hessels, J. W. T., Deller, A. T., Kaplan, D. L., Lorimer, D. R., Lynch, R. S., Ransom, S. M., Stairs, I. H.

Even with its extreme gravity, the pulsar falls exactly the way Einstein predicted