

# Multi-frequency imprints of Pulsar radio emission models

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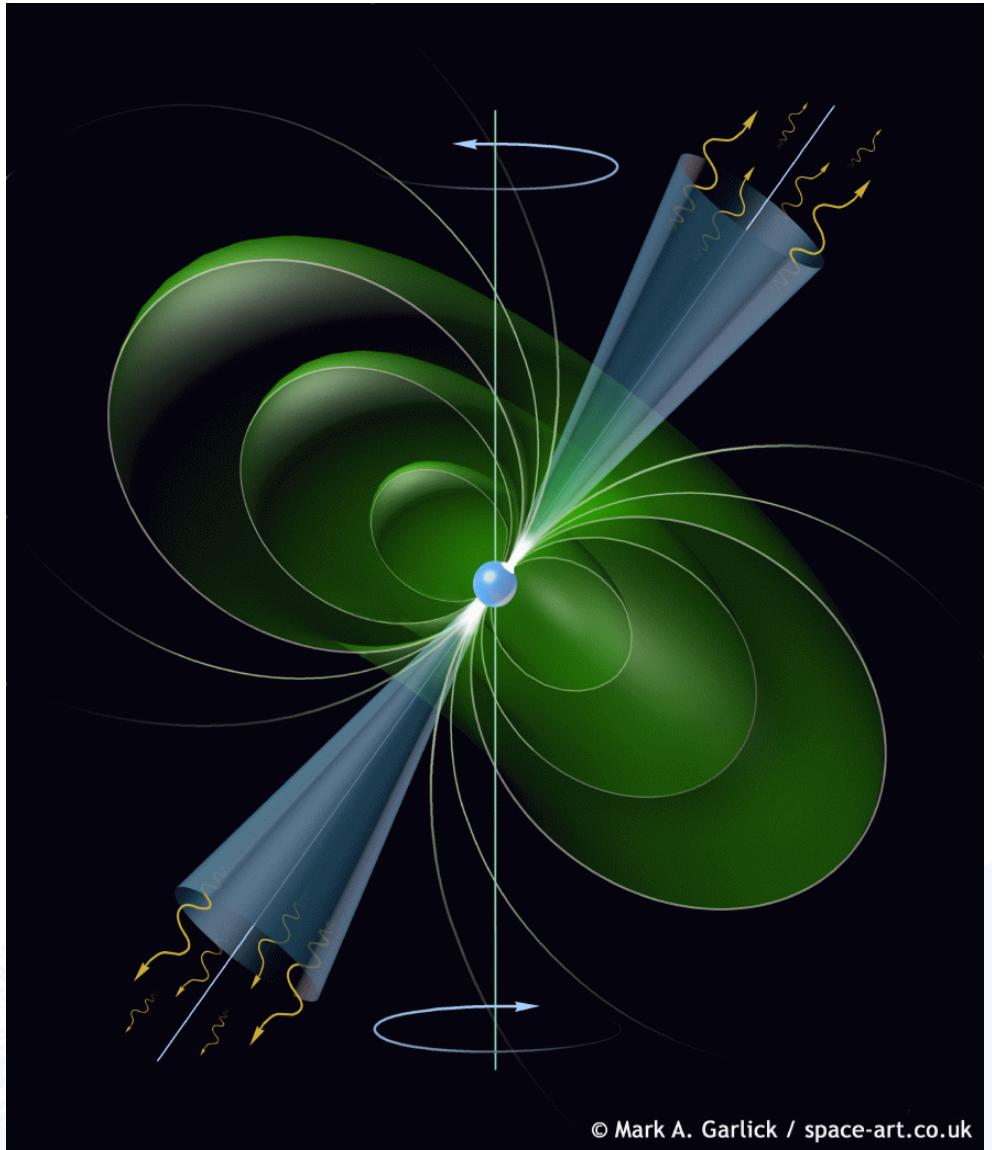
March 2019

**MWSKY-II**

# Radio emission from pulsars

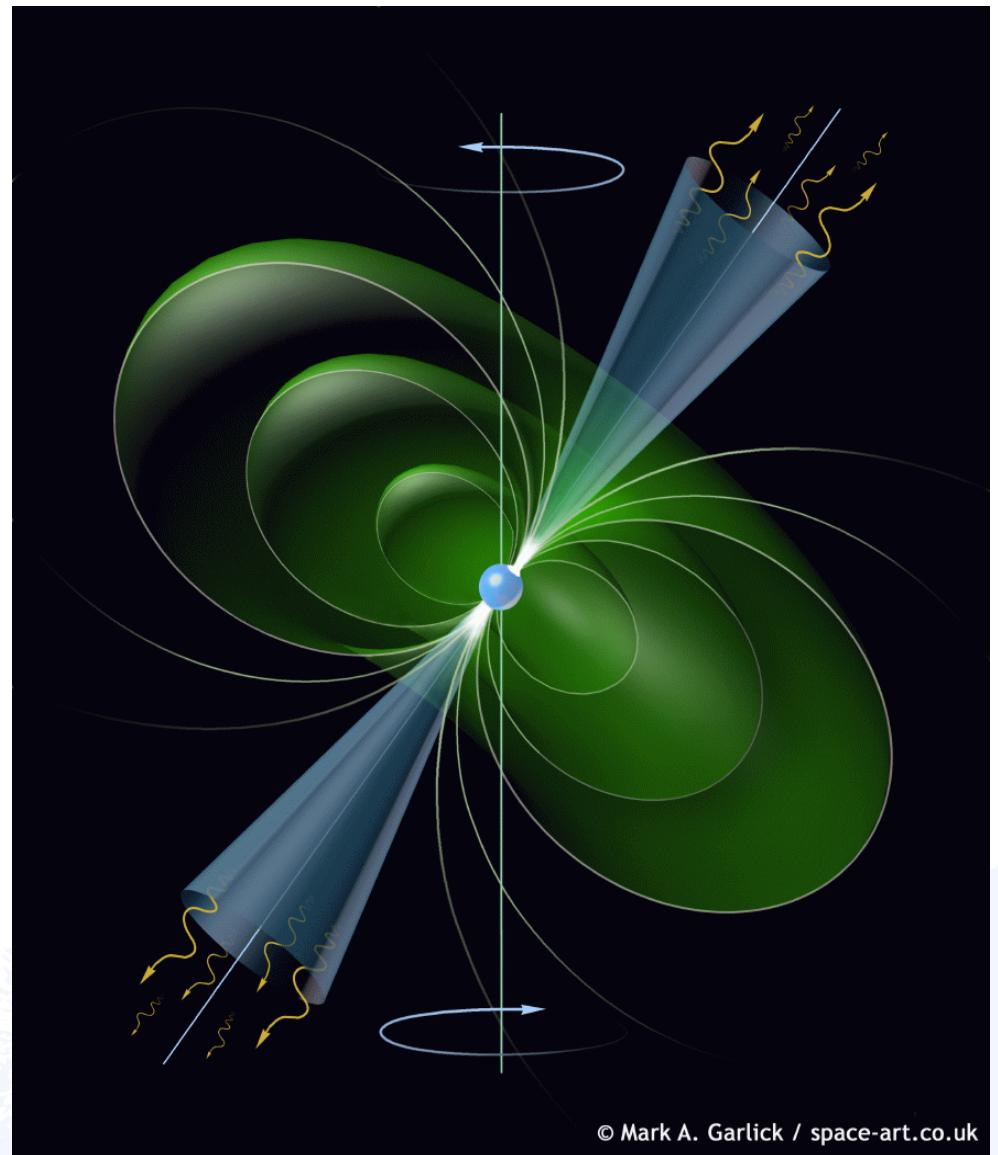
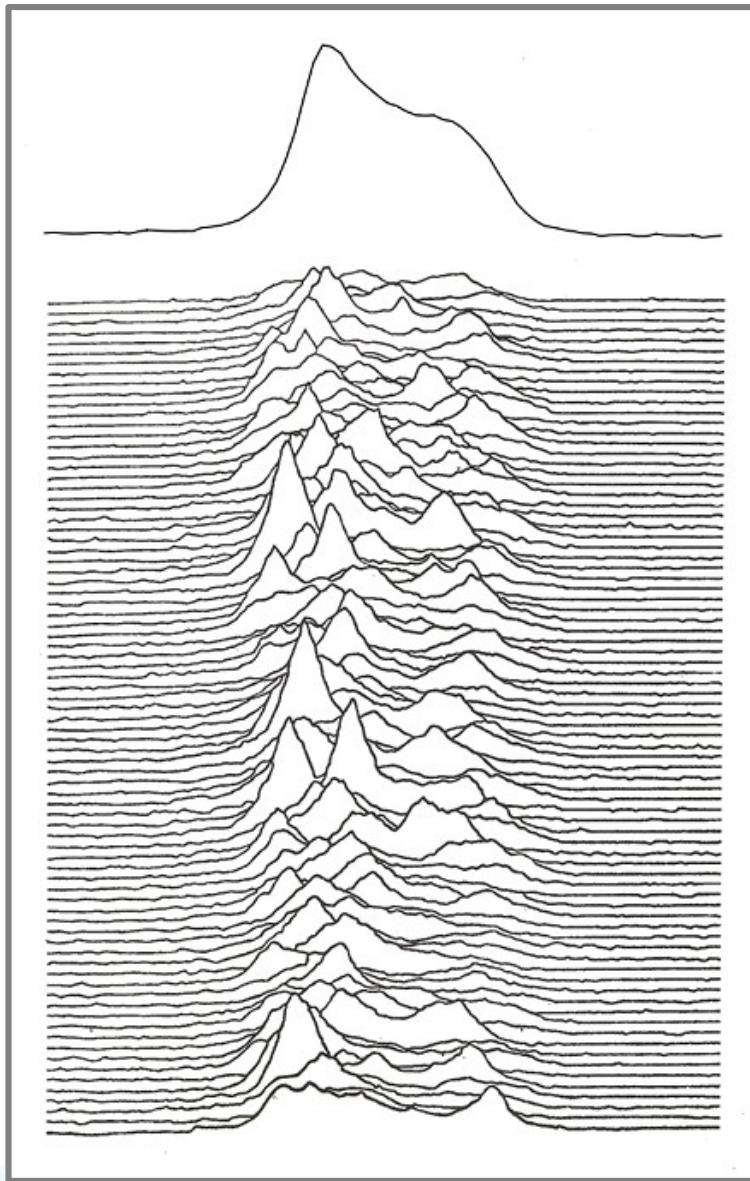
**Emission from charged particles streaming along the curved magnetic field lines in the open field line region.**

**Emission at any given frequency comes from a limited range of altitudes.**



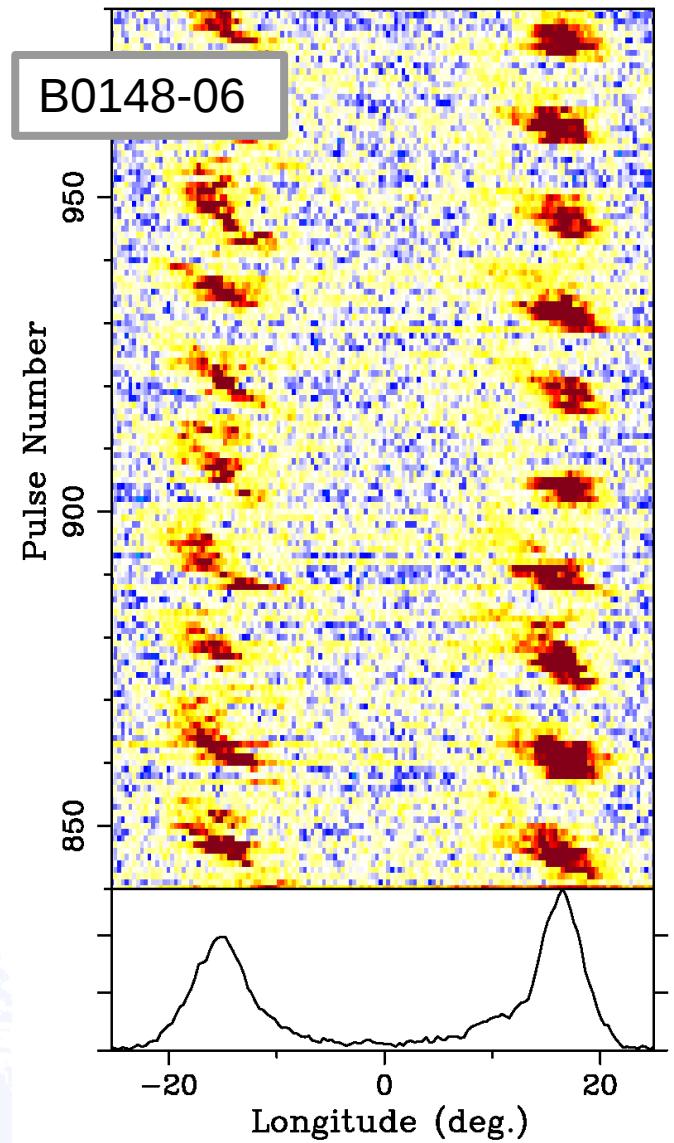
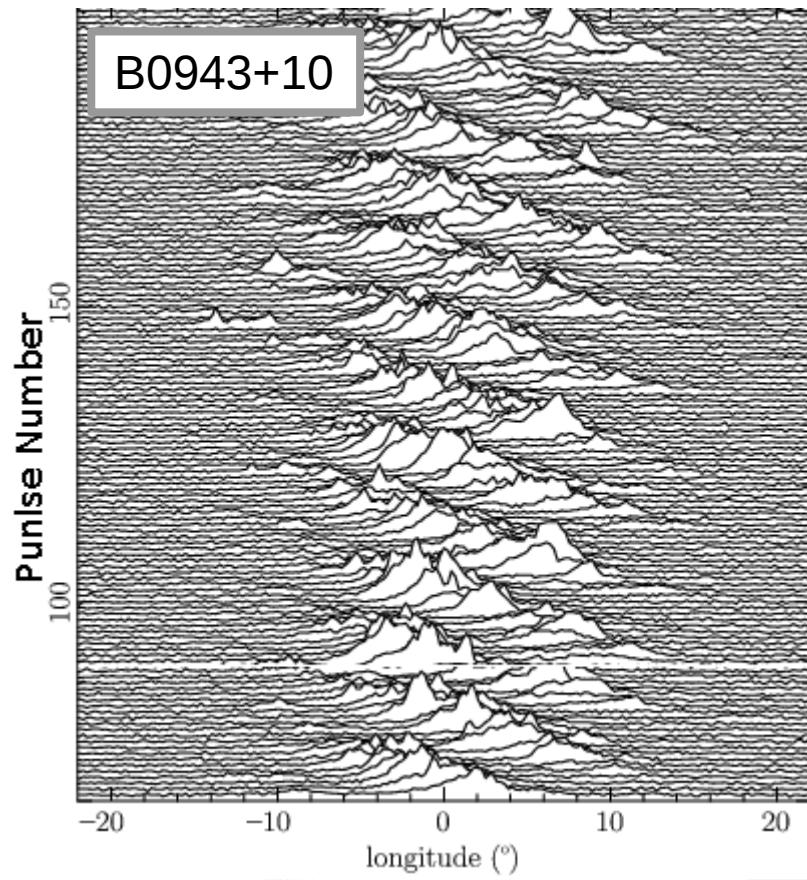
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# Radio emission from pulsars



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# Emission from pulsars: Sub-pulse drifting



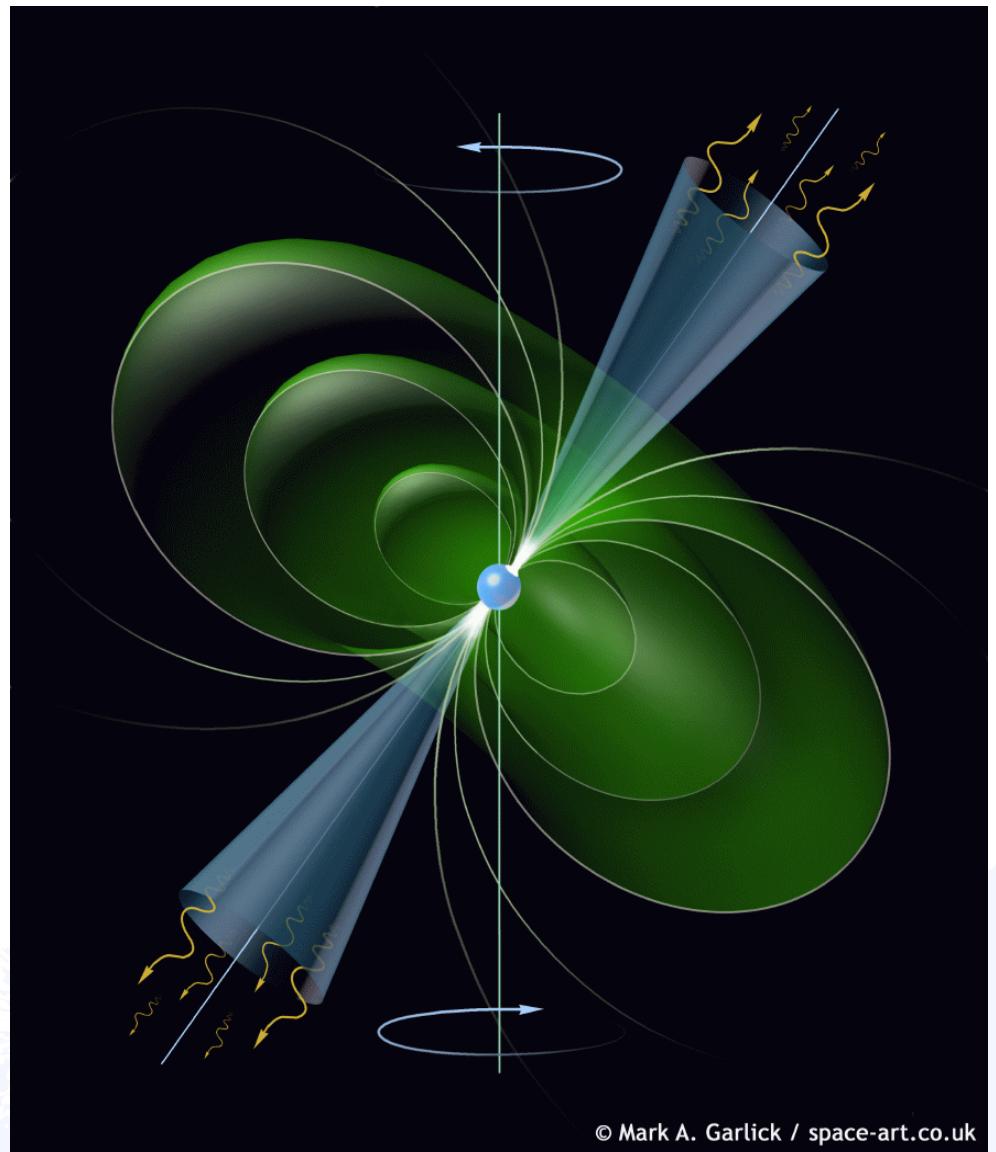
# Emission from pulsars: Carousel model

“Spark” discharges in the Acc. Gap  
(~100 meters,  $10^{12}$  eV)

Sparks rotate about the magnetic axis, due to  $E \times B$  drift  $\Rightarrow$  **A carousel of sparks.**

A system of emission columns, seeded by a **carousel of sparks**, appears to rotate about the magnetic axis.

Carousel Model  
(Ruderman & Sutherland 1975)

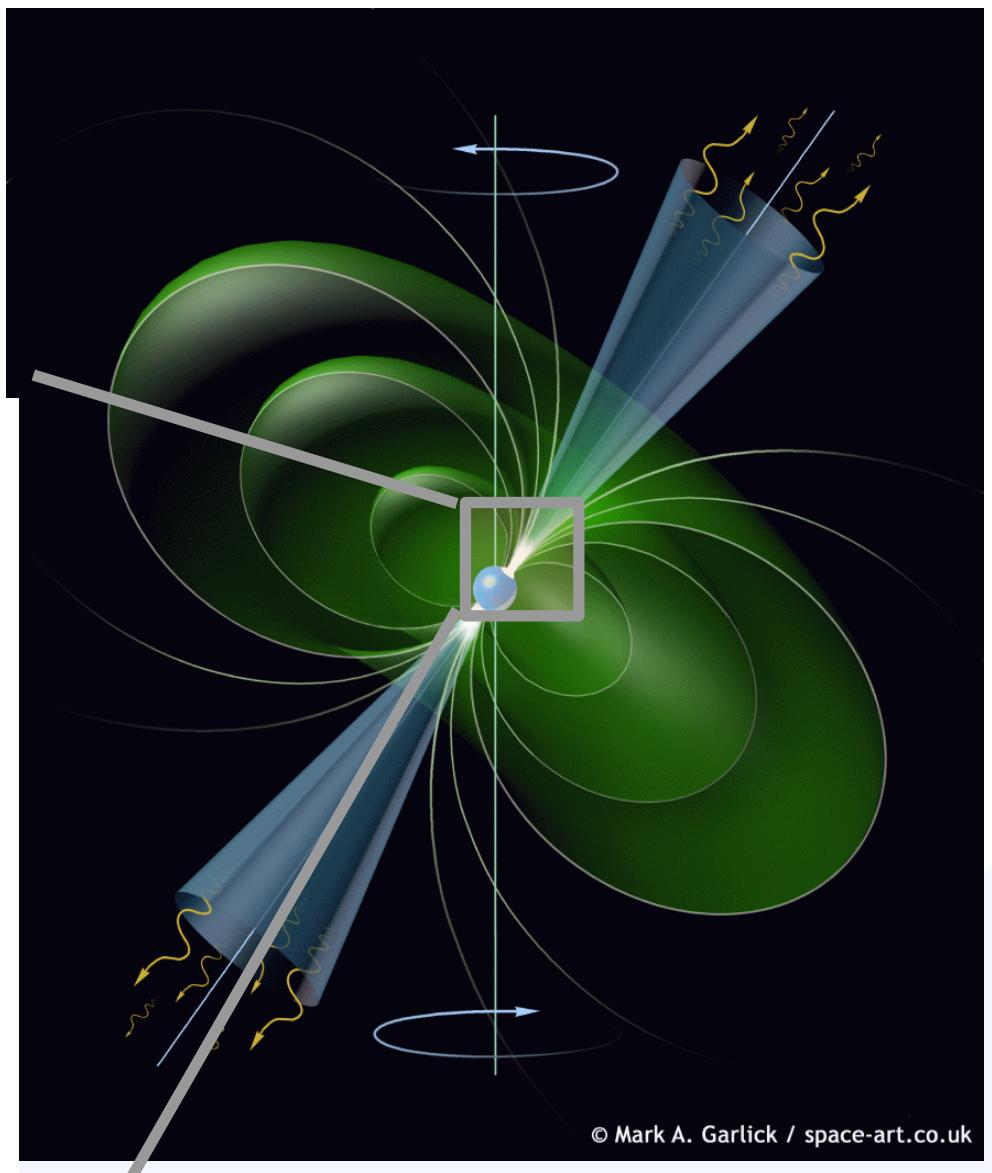
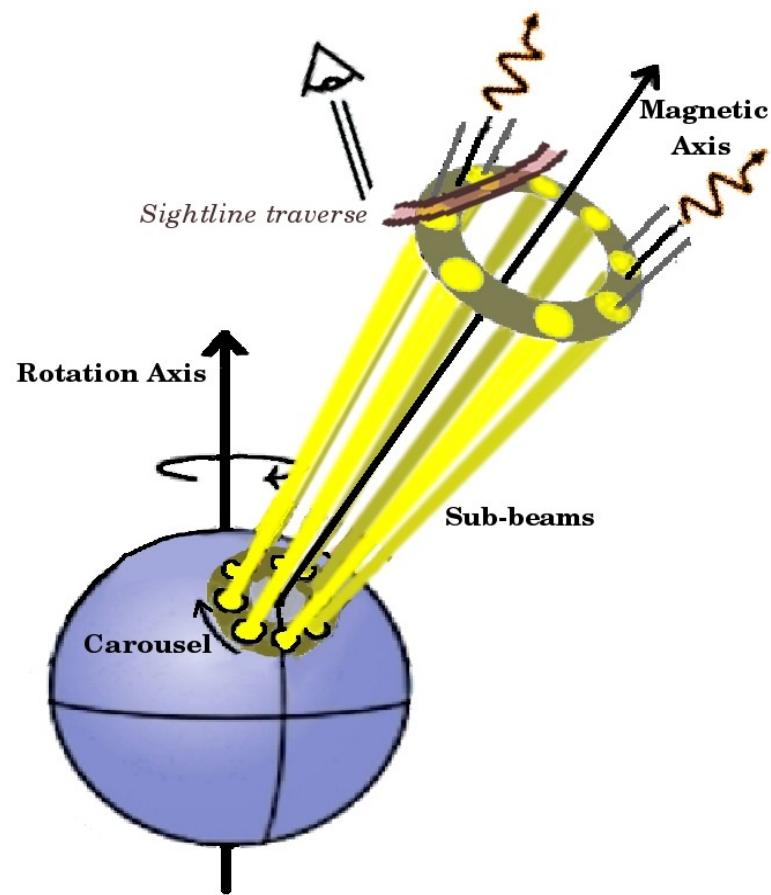


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(Ruderman & Sutherland 1975)

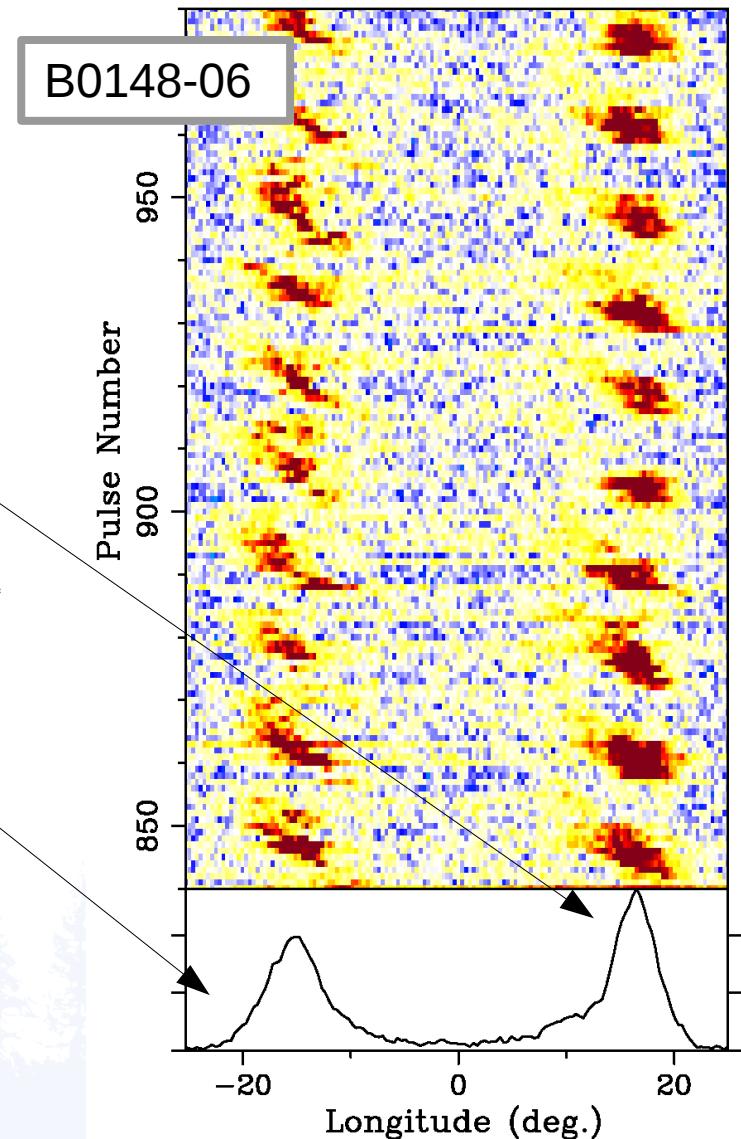
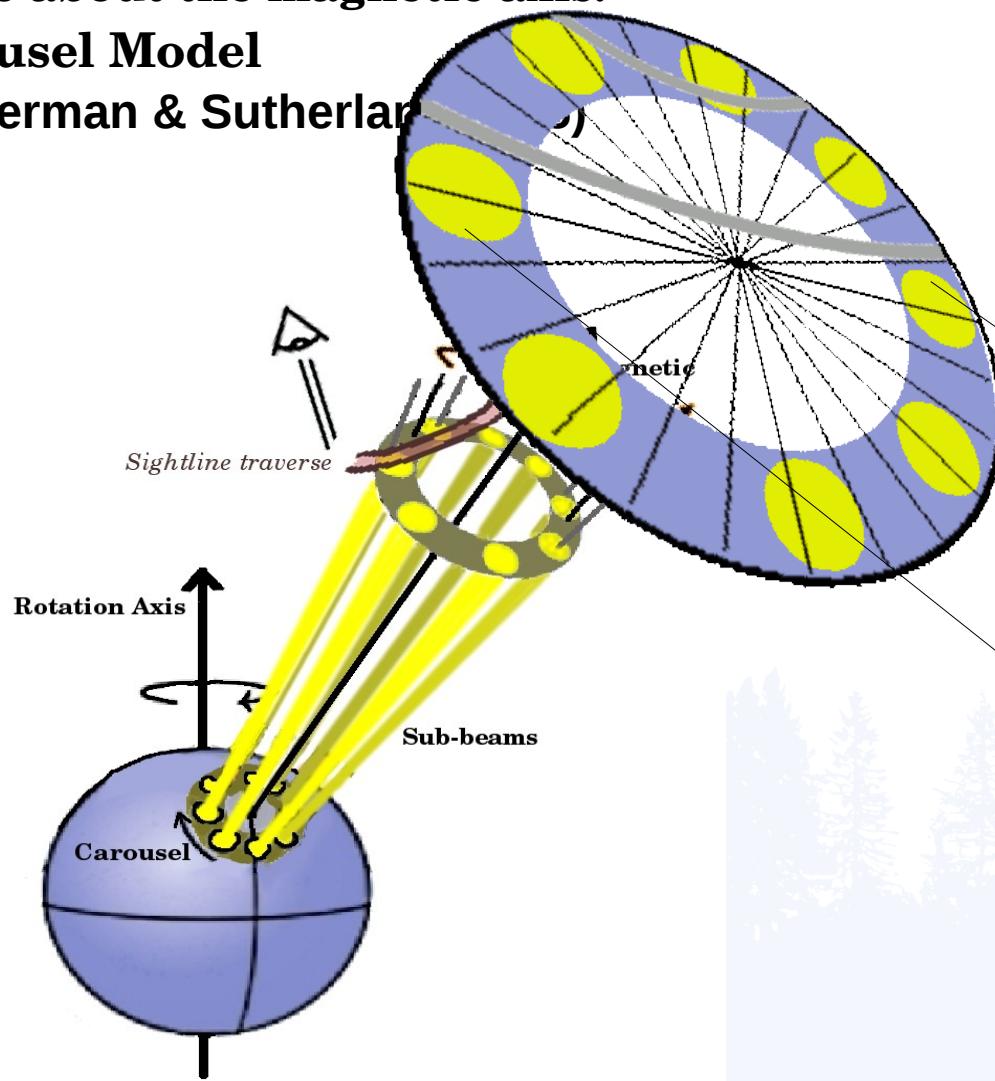


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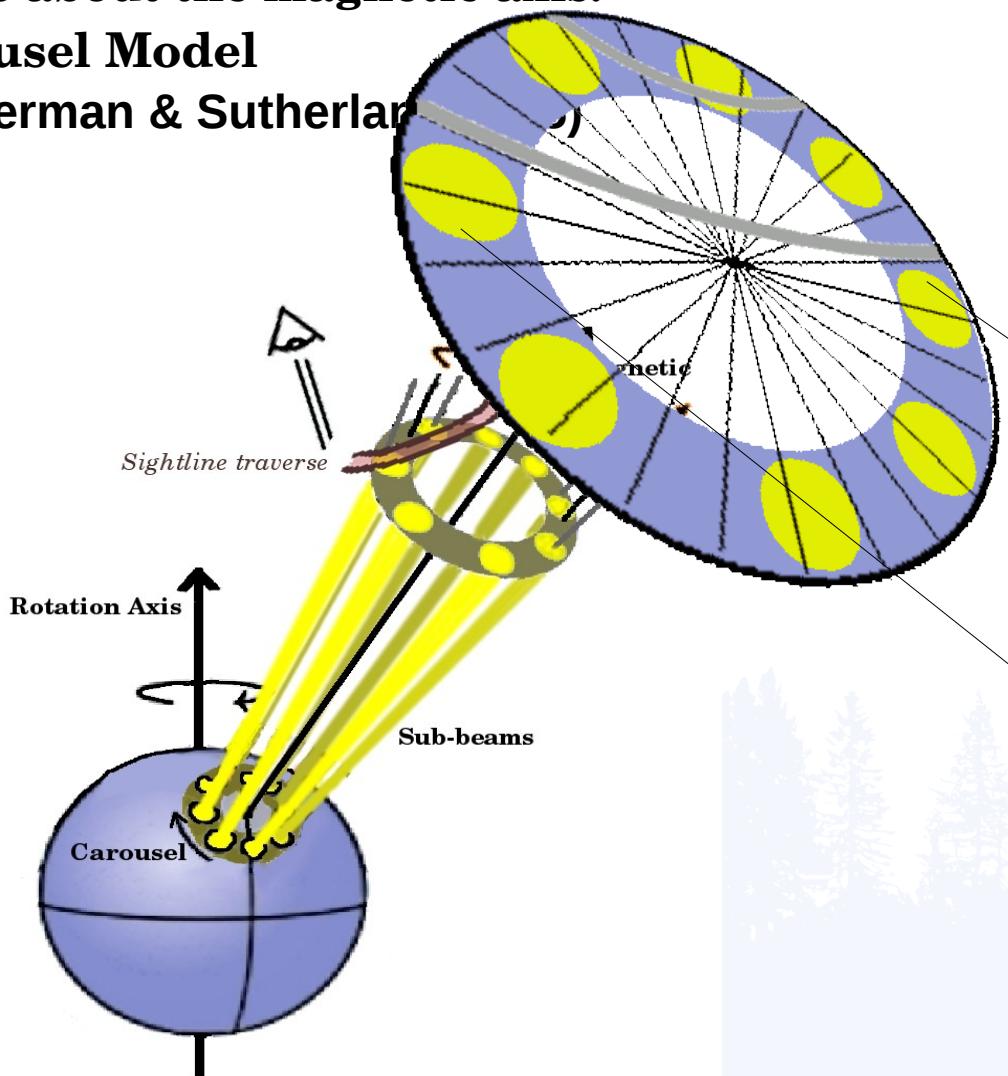
Carousel Model  
(Ruderman & Sutherland)



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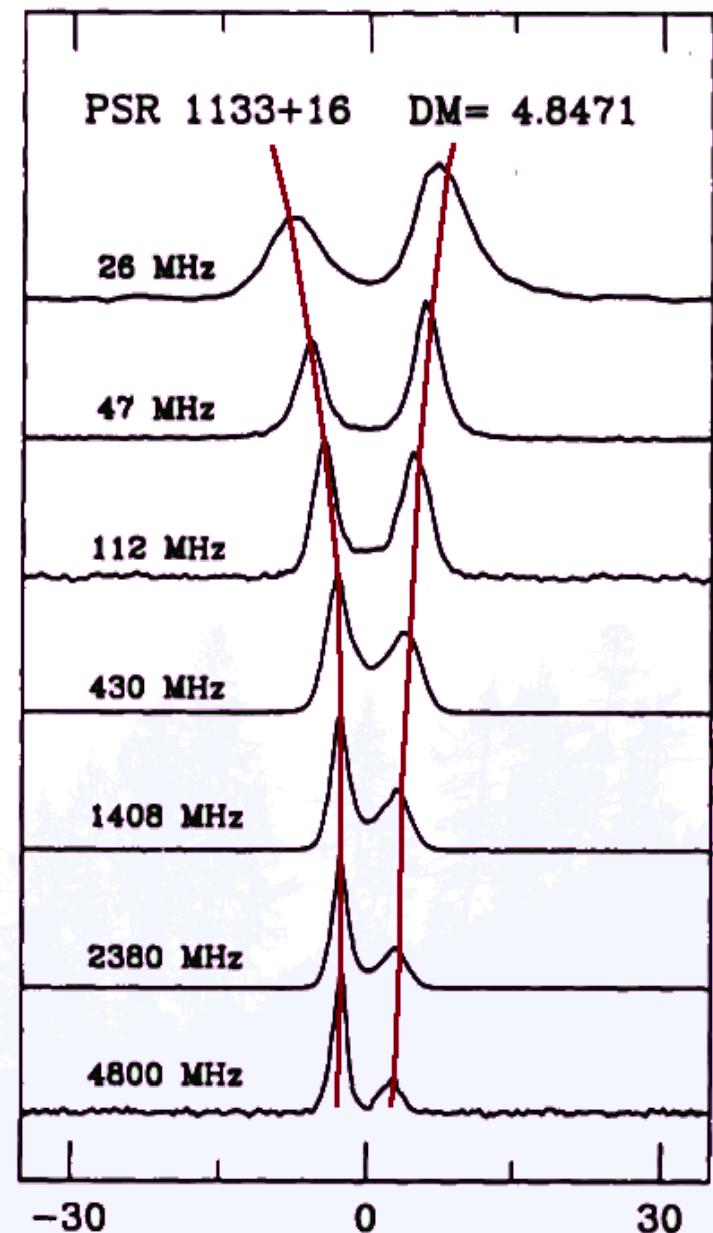


Many observational phenomena unexplained in this model:  
Bi-drifting, Multiple drift modes, etc.

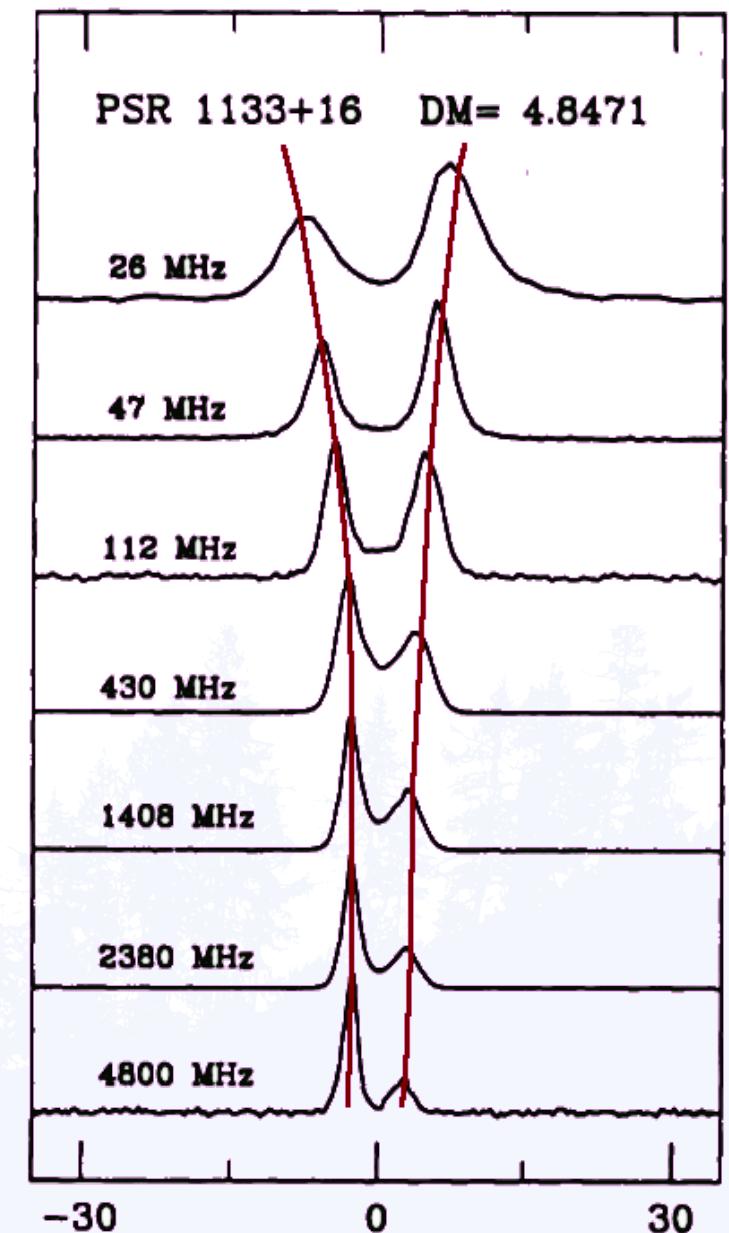
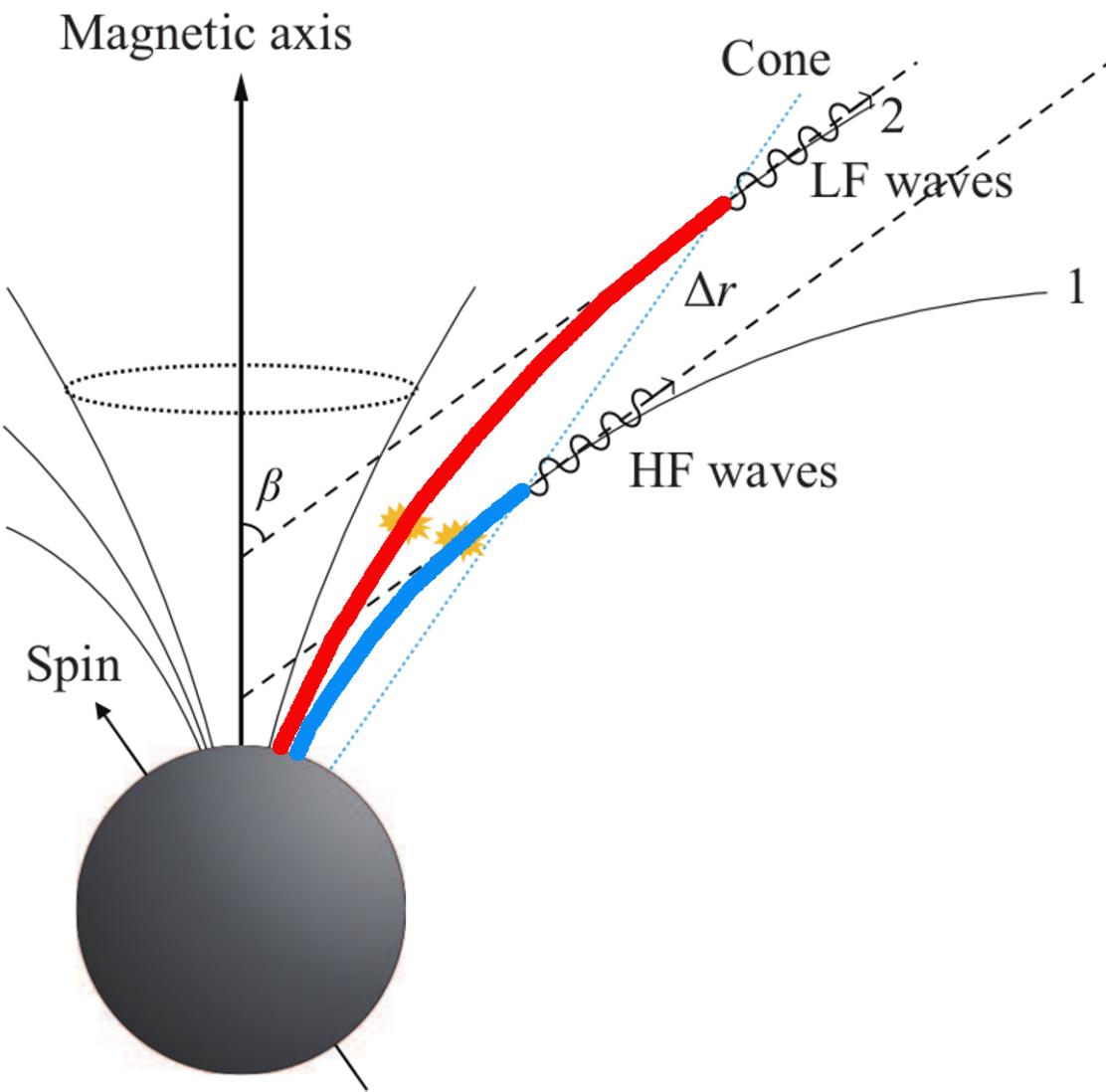
Recently more questions on the symmetry axis of the carousel.

Expected signatures in multi-frequency observations remain largely unexplored.

# Radius-to-frequency mapping (RFM)

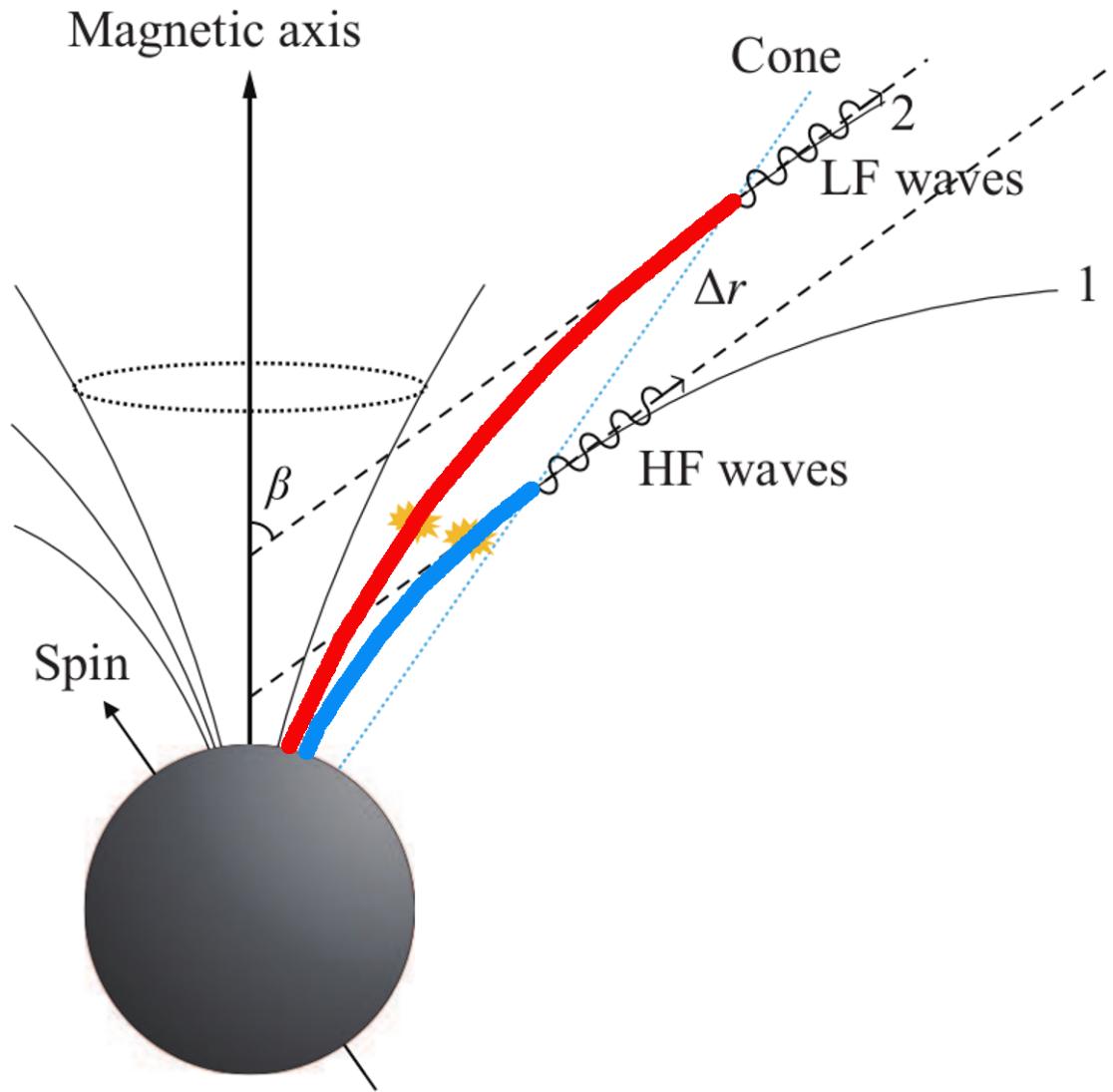


# Radius-to-frequency mapping (RFM)



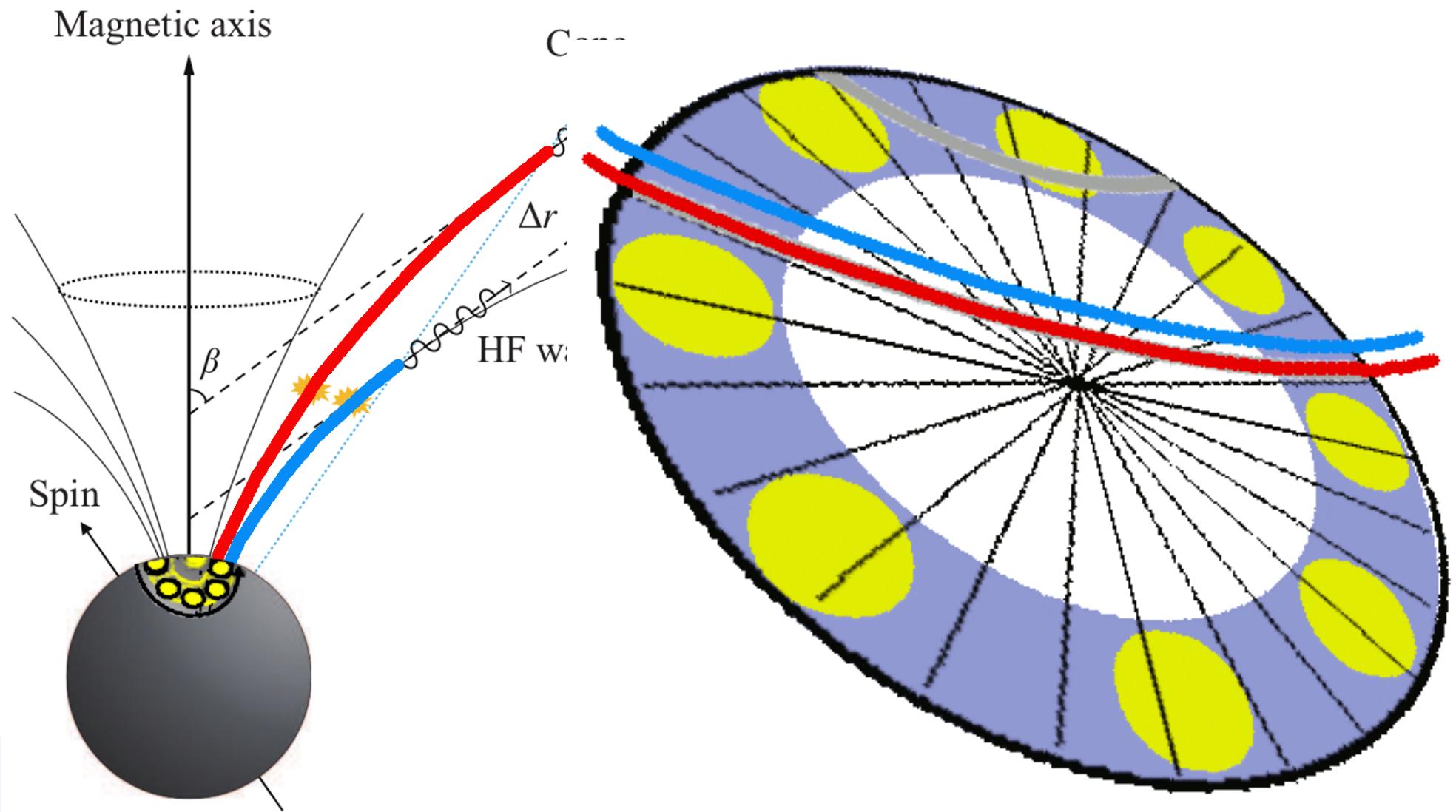
# RFM: Implications for the Carousel model

Different frequencies probe slightly different set of field lines.

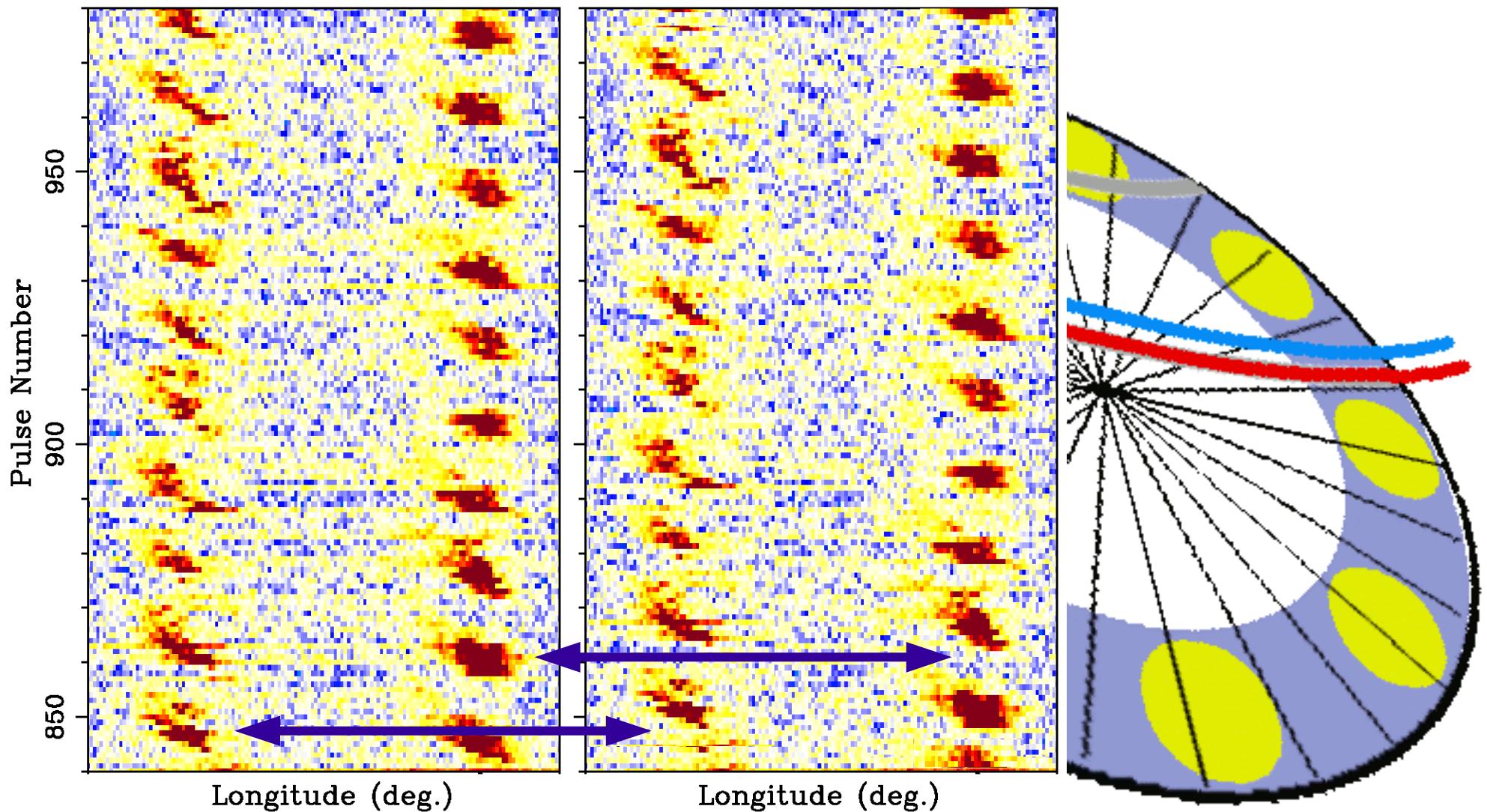


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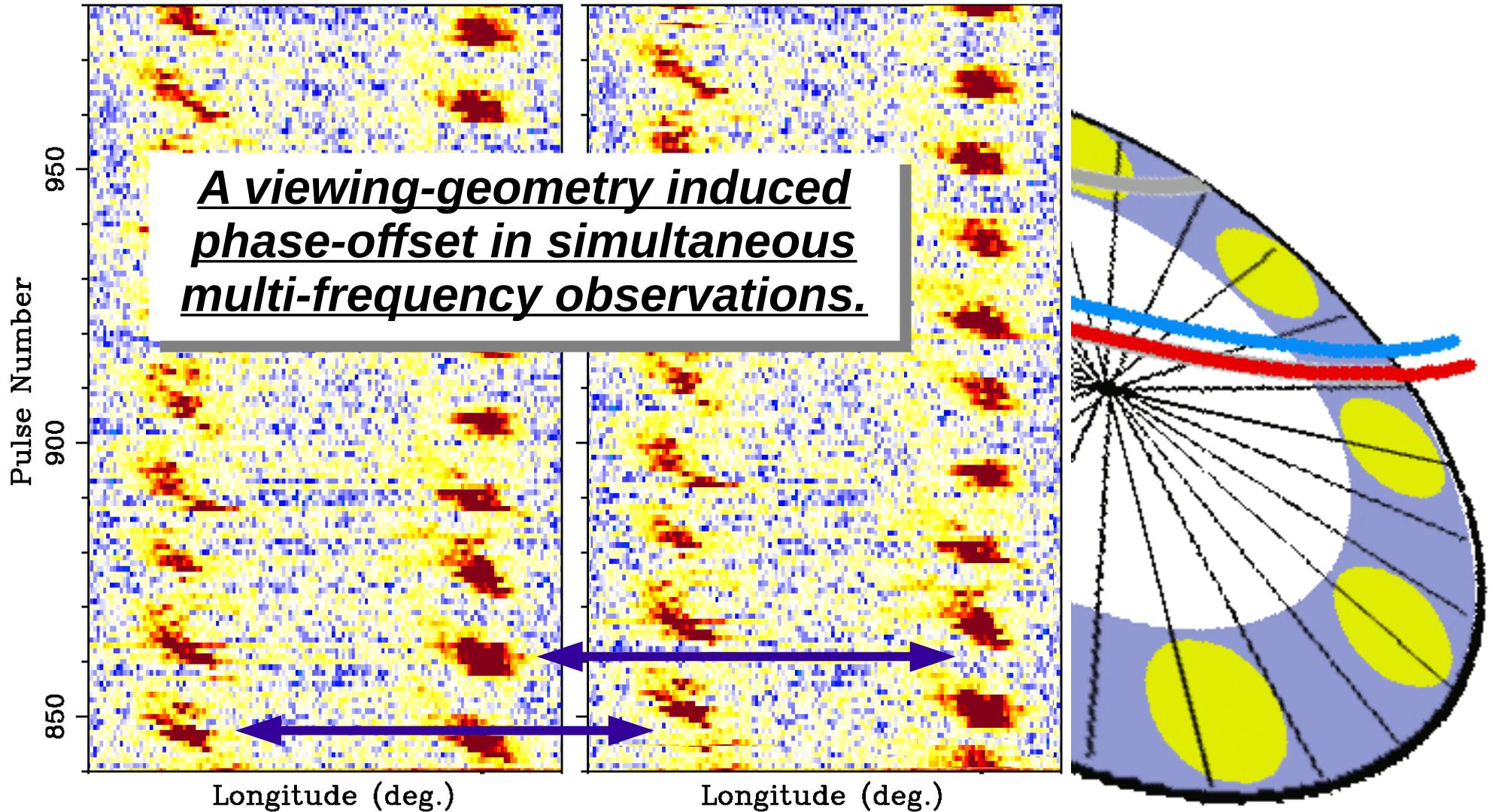
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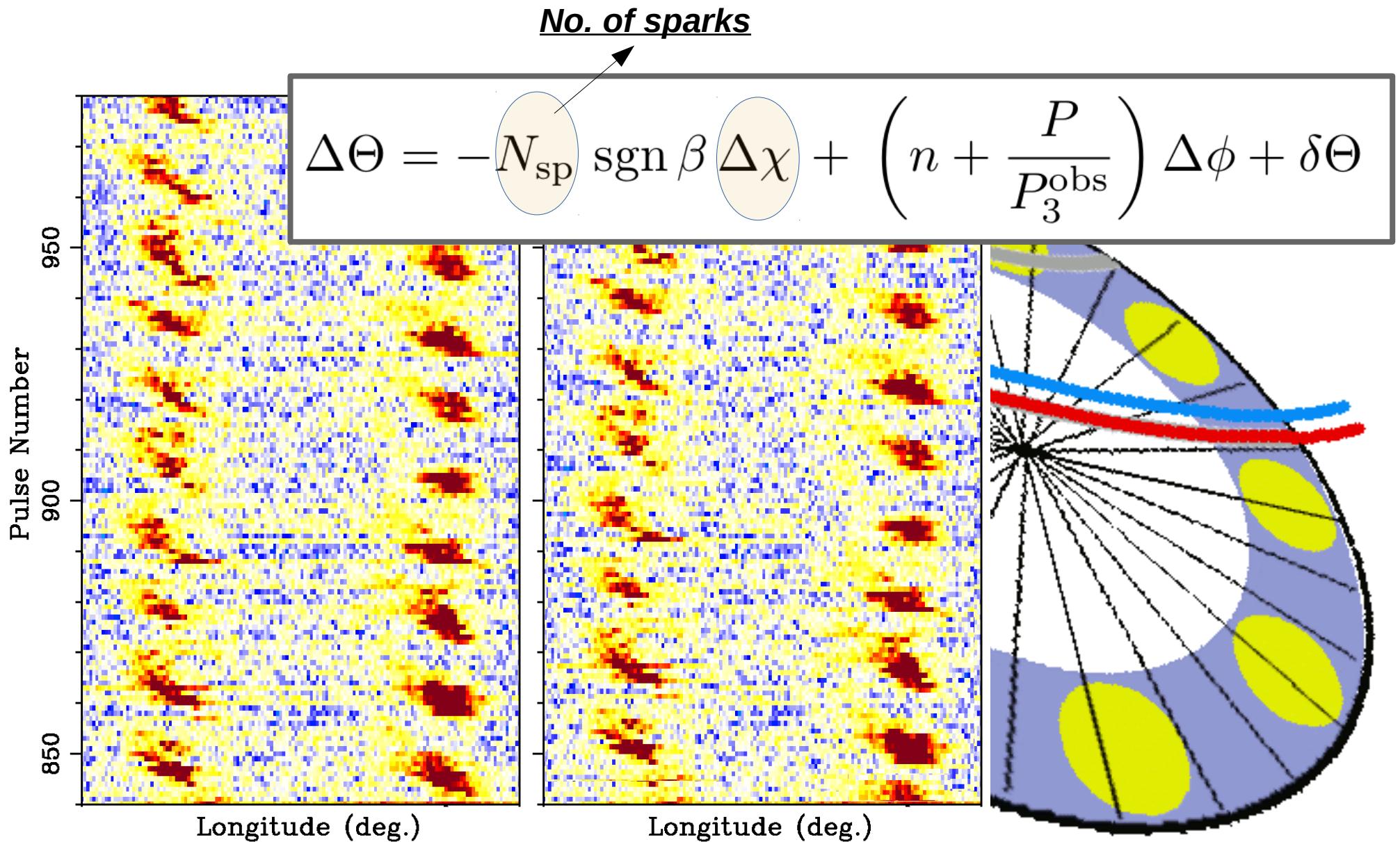
# RFM: Expected multi-frequency imprints



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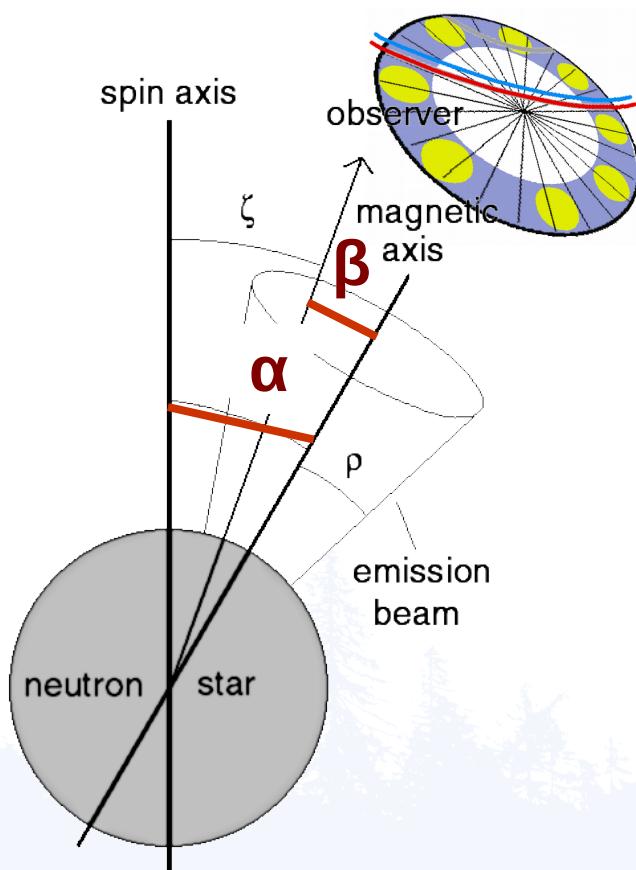
# A geometry-induced phase-offset



# A geometry-induced phase-offset

No. of sparks

$$\Delta\Theta = -N_{sp} \operatorname{sgn} \beta \Delta\chi + \left( n + \frac{P}{P_{3\text{obs}}} \right) \Delta\phi + \delta\Theta$$



**Primary dependence on:**

- 1) No. of sub-beams
- 2) Magnetic inclination angle ( $\alpha$ )
- 3) The impact angle ( $\beta$ )

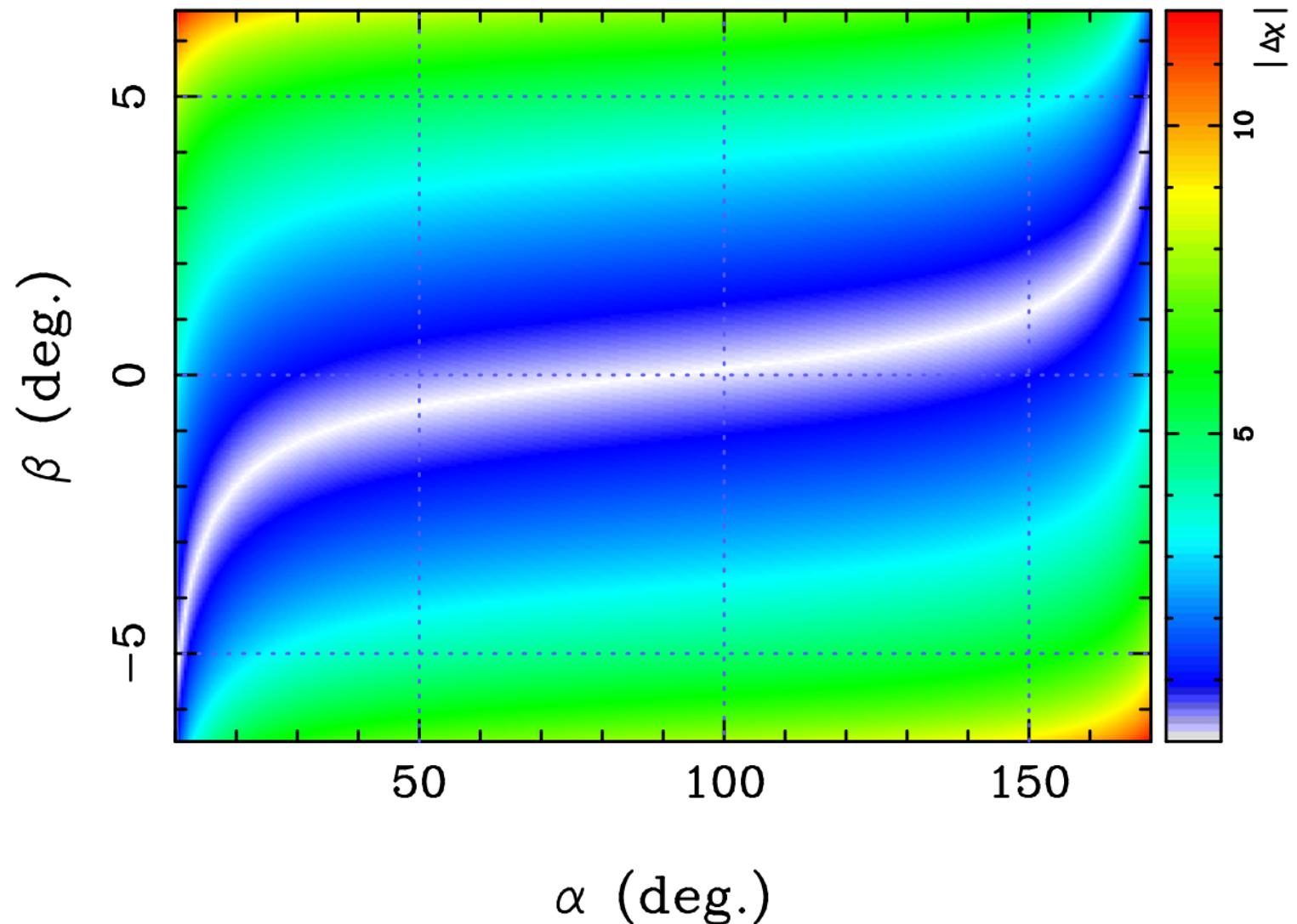
**And mildly on:**

- 4) Sub-pulse modulation period,
- 5) Component position change,
- 6) Aberration effects.

# Subpulse phase-offset: variations with viewing geometry

*Change in the magnetic azimuth ( $\Delta\chi$ ) between 250 and 600 MHz.*

$\Delta\Theta \sim N_{sp} \times \Delta\chi$



# Frequency-dependent subpulse phase-offset: Observable Implications

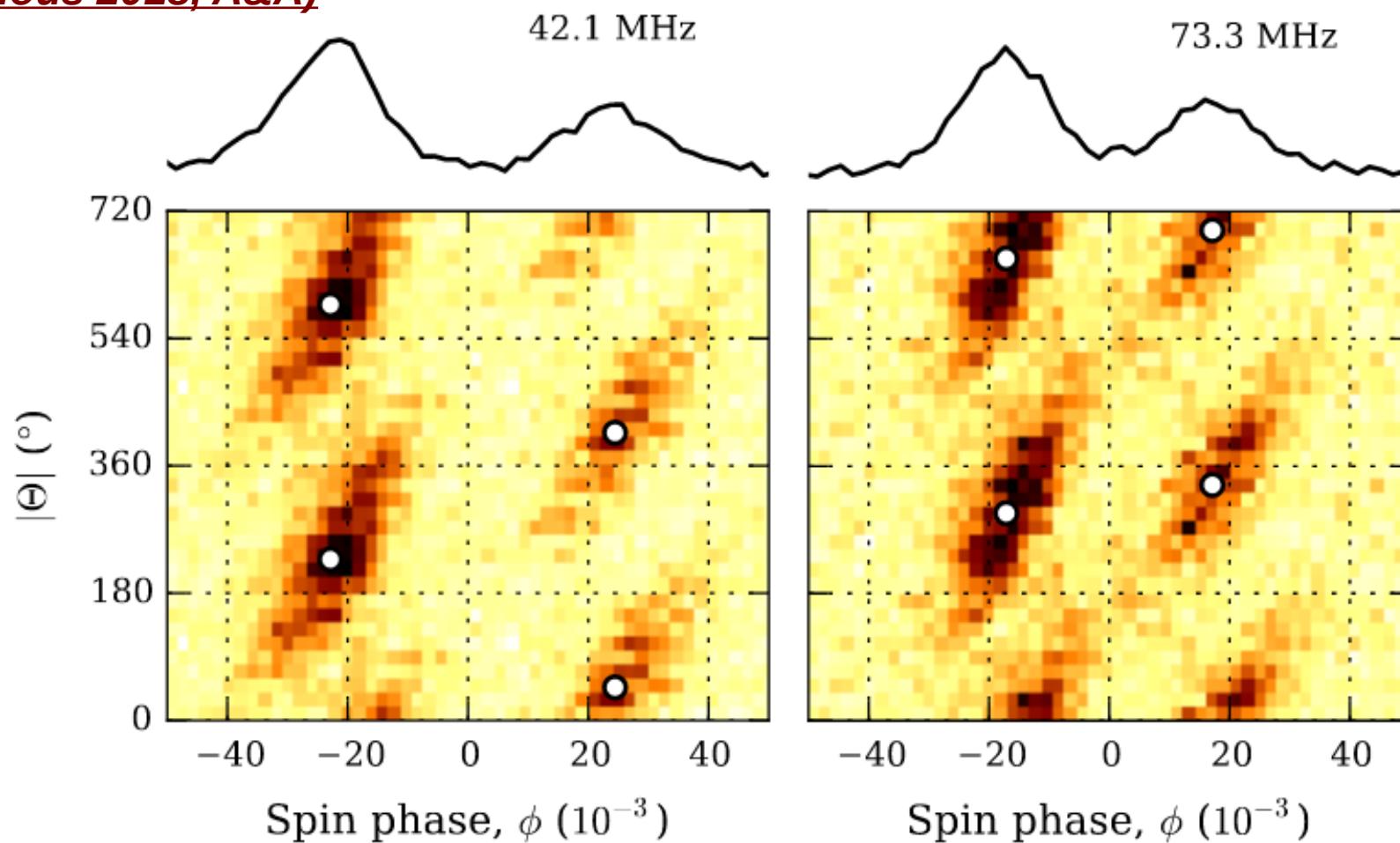


# Observable implications of the geometrical phase-offset

- **1. Testing the Carousel model**
- **2. Test single frequency multi-altitude emission**
- **3. Modeling the emission geometry**
- **4. Resolving the aliasing in subpulse modulation period**
- **5. A clean probe of any twist in the magnetosphere**
- **6. Two-dimensional mapping of the polar-cap**

# Observable Implications...

*Observed subpulse phase-offsets for B0943+10 using LOFAR LBA.  
(Bilous 2018, A&A)*



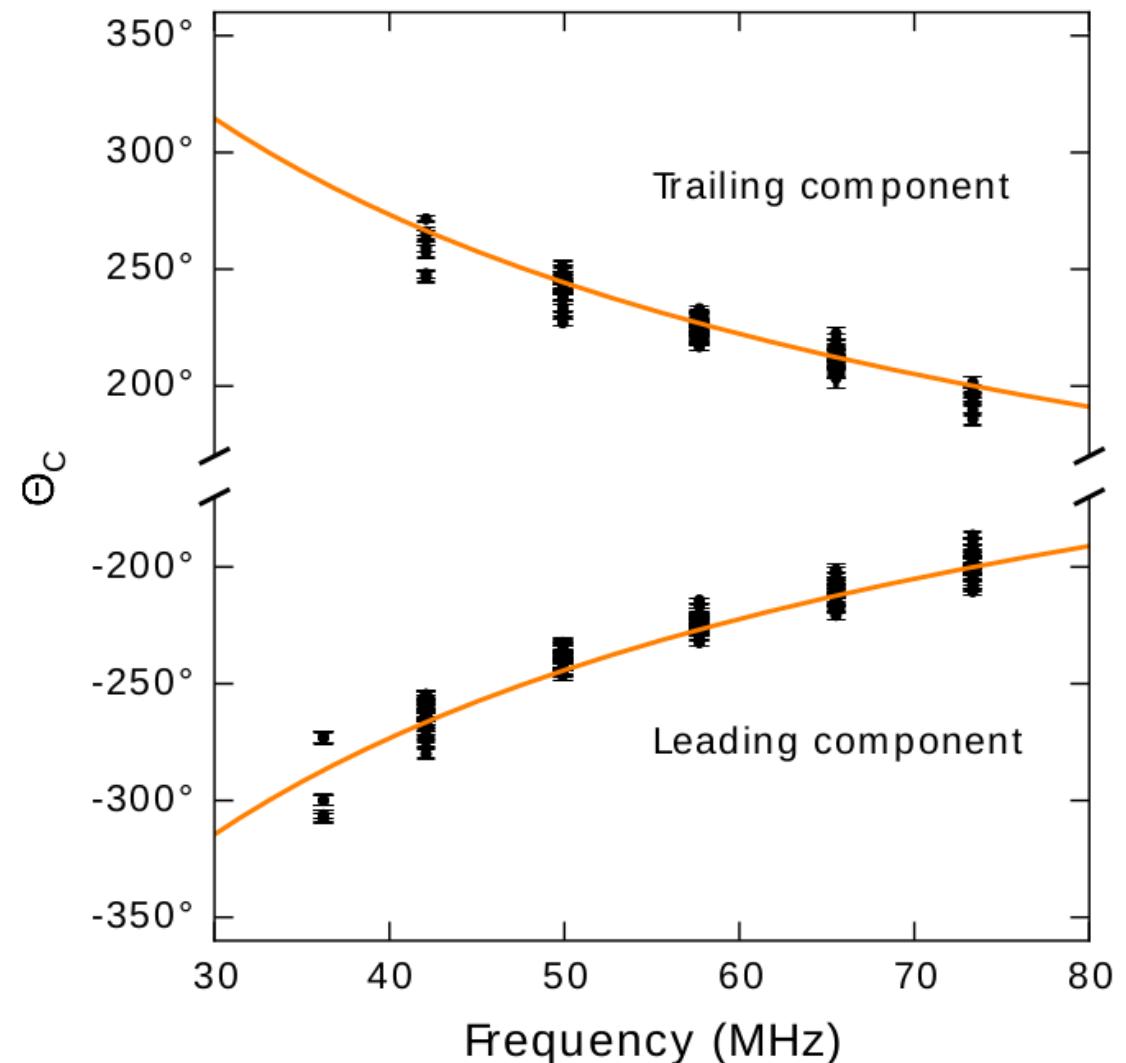
# Observable Implications...

## - 1. Testing the Carousel model

*B0943+10 observations consistent with the carousel model. (Bilous 2018, A&A)*

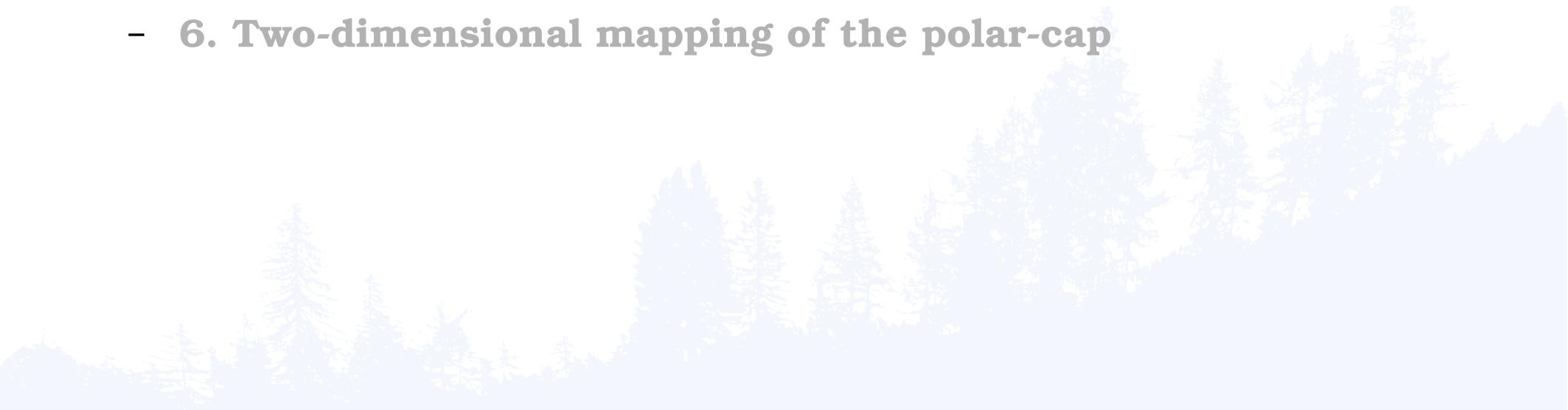
*Magnetic inclination angle ( $\alpha$ ) for B0943+10 is only about  $6^\circ$  and a grazing line-of-sight.*

Stringent tests to be done for pulsars with more central lines-of-sight.



# Observable Implications

- 1. Testing the Carousel model
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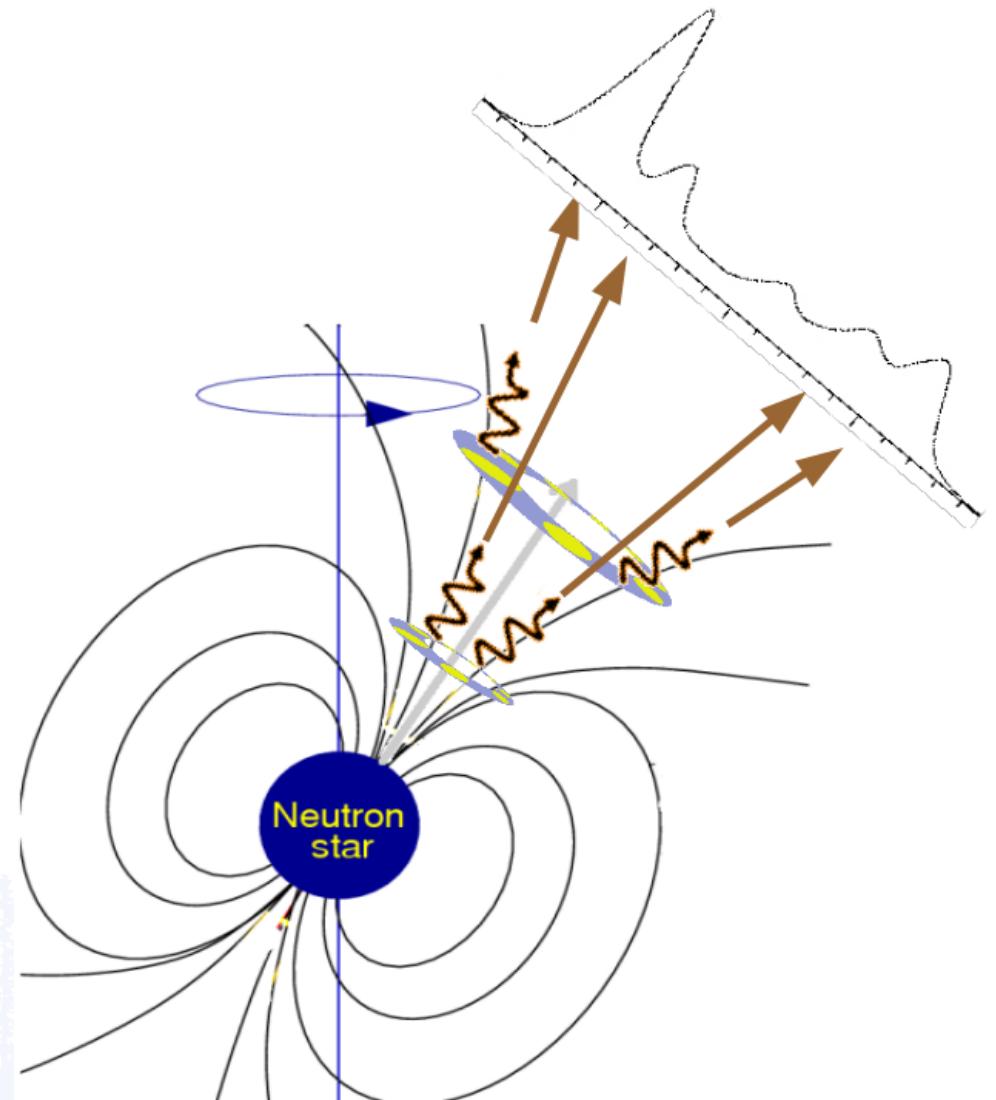
# Single-frequency Multi-altitude emission

## M-type profiles

- **Phase-locked modulation between inner and outer cones,**
- **B1237+25:** inner cone emitted at lower altitudes compared to outer cone
- **Number of sub-beams same in the emission patterns of the two cones**

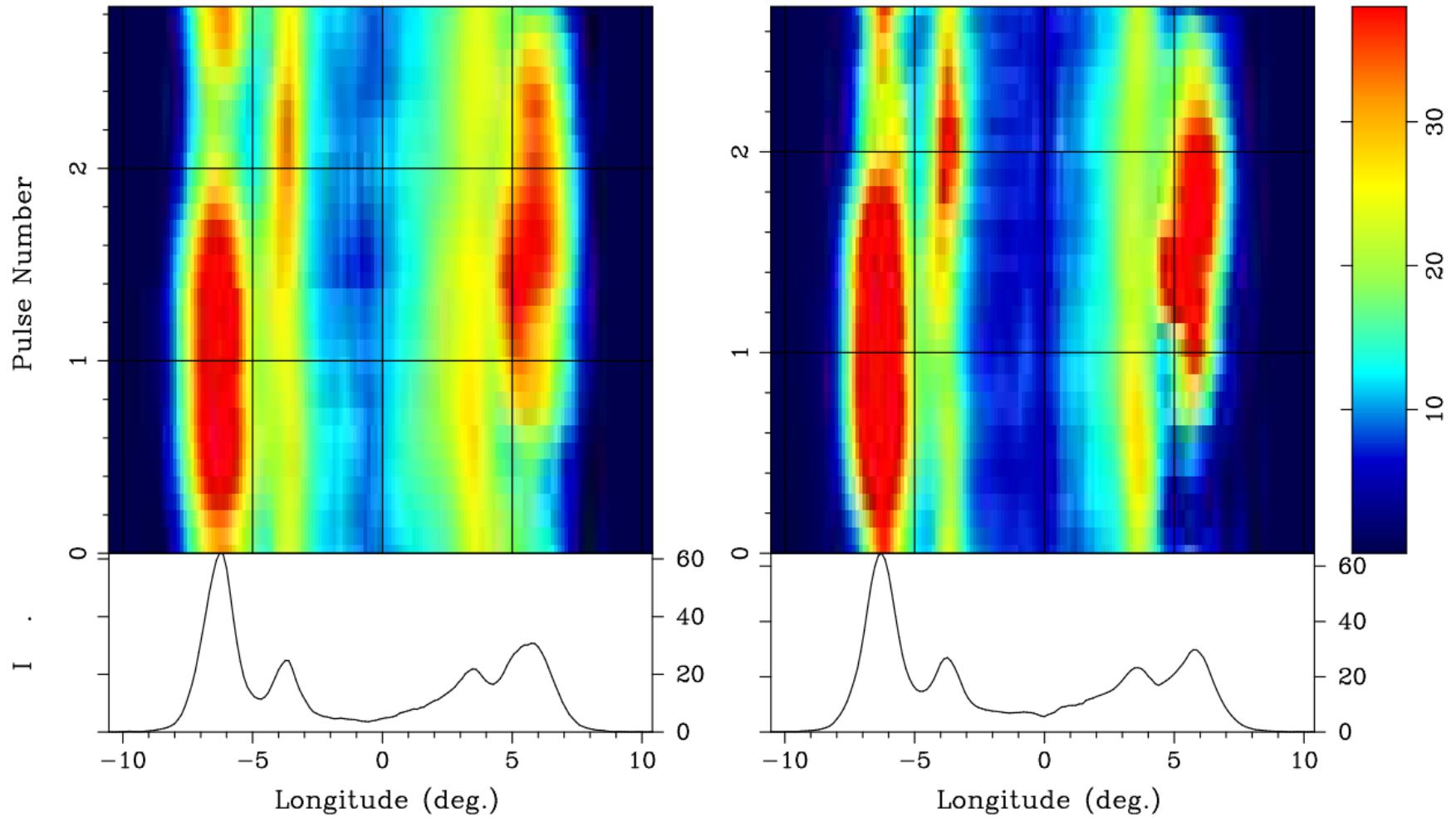
=> **Single frequency Multi-altitude emission**

**Rankin (1993),  
Maan and Deshpande (2014)**



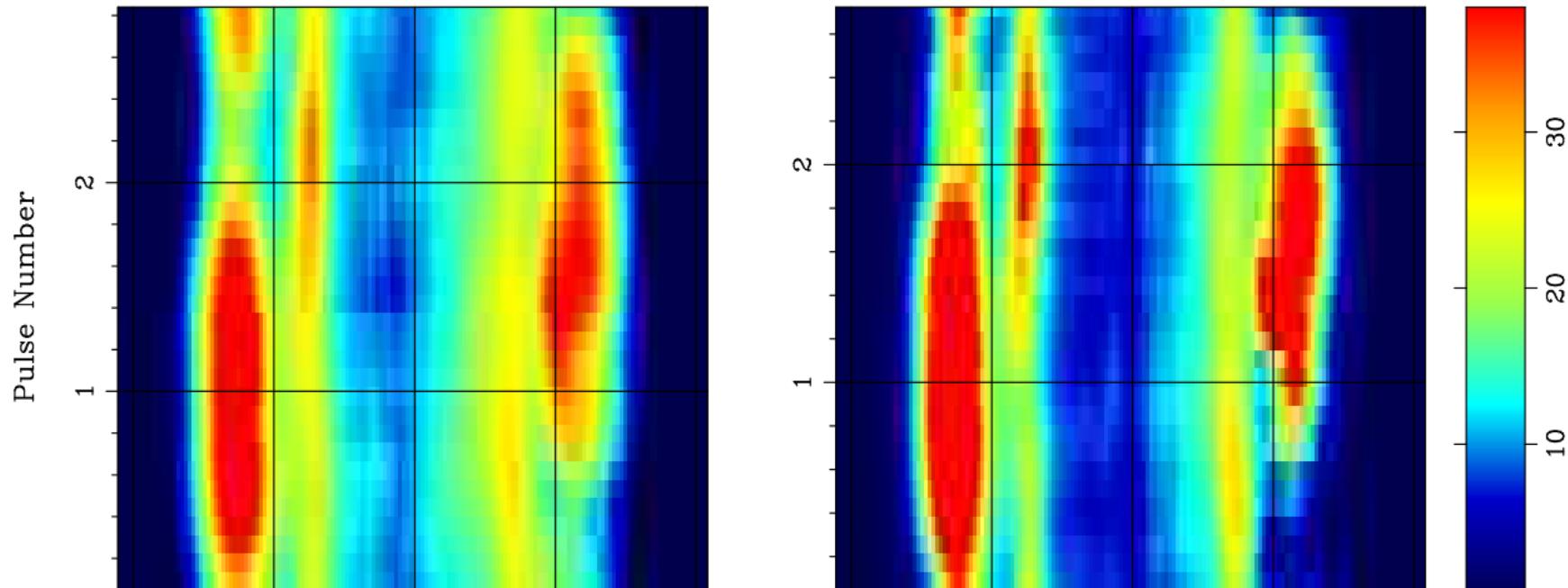
# Multi-altitude emission (B1237+25)

*Implications for the subpulse phase*



# Multi-altitude emission (B1237+25)

*Expected and observed phase-offsets. (Maan 2019, ApJ)*



I .	Subseq.	Components I and II		Components IV and V	
		$\rho_{\max}$ (%)	$\Delta\Theta_{\text{obs}}$ ( $^{\circ}$ )	$\rho_{\max}$ (%)	$\Delta\Theta_{\text{obs}}$ ( $^{\circ}$ )
	$S_1$	$91.0 \pm 6.7$	$+137 \pm 32$	$76.5 \pm 16.4$	$-104 \pm 36$
	$S_2$	$95.6 \pm 3.4$	$+137 \pm 22$	$71.3 \pm 19.0$	$-115 \pm 47$

## Multi-altitude emission (B1237+25)

*Within the scope of dipolar geometry,  
the observed phase-offsets can be explained by multi-altitude  
emission scenario.*

*A firm evidence for multi-altitude emission.*

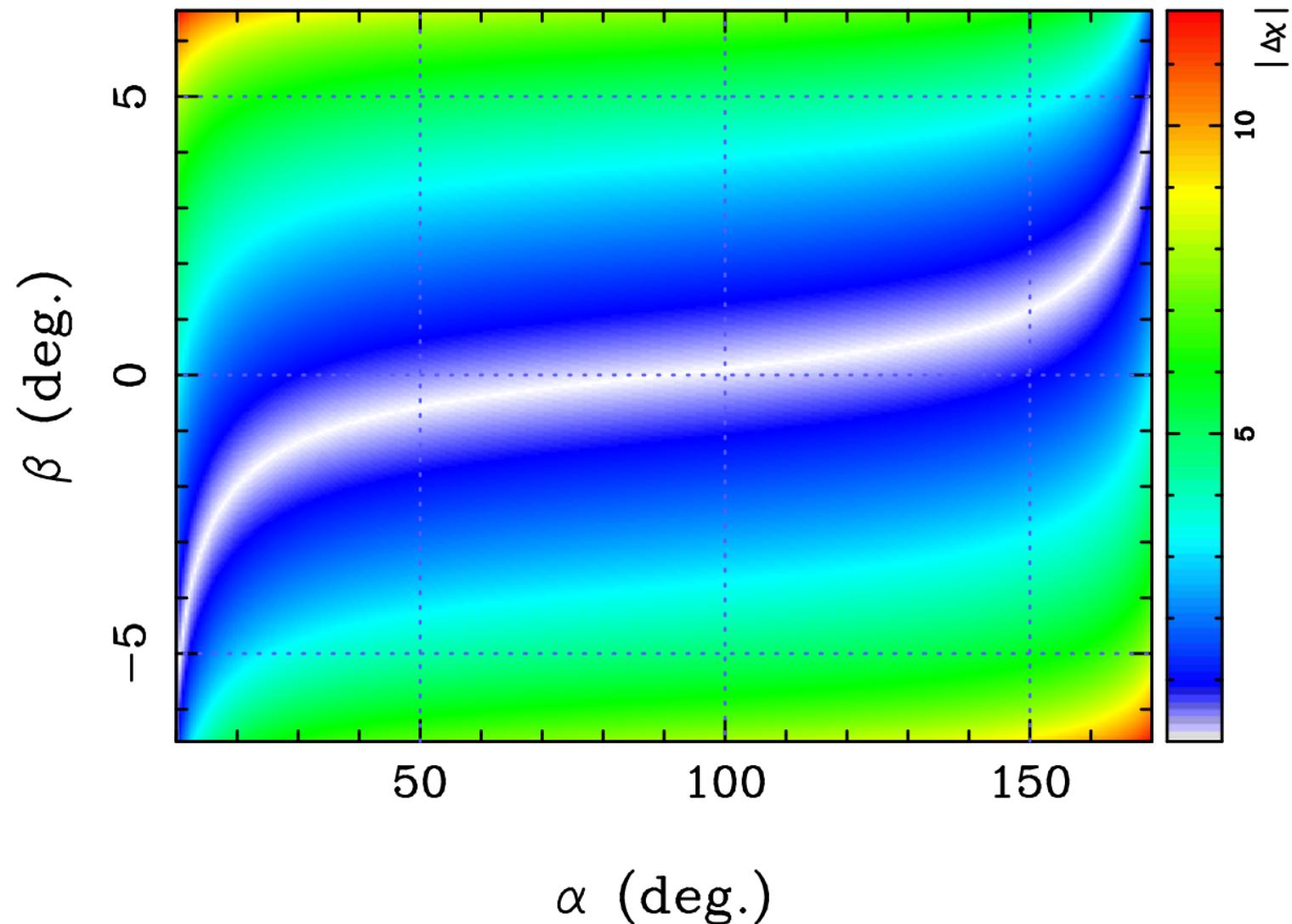
# Observable Implications

- 1. Testing the Carousel model
- 2. Test single frequency multi-altitude emission
- **3. Modeling the emission geometry (particularly alpha)**
- 4. Resolving the aliasing in subpulse modulation period
- 5. A clean probe of any twist in the magnetosphere
- 6. Two-dimensional mapping of the emission-beam

# Observable Implications...

*Modeling the magnetic inclination angle ( $\alpha$ ) is a difficult task.*

*Observed phase-offsets could be useful to estimate  $\alpha$ , especially for nearly aligned rotators.*



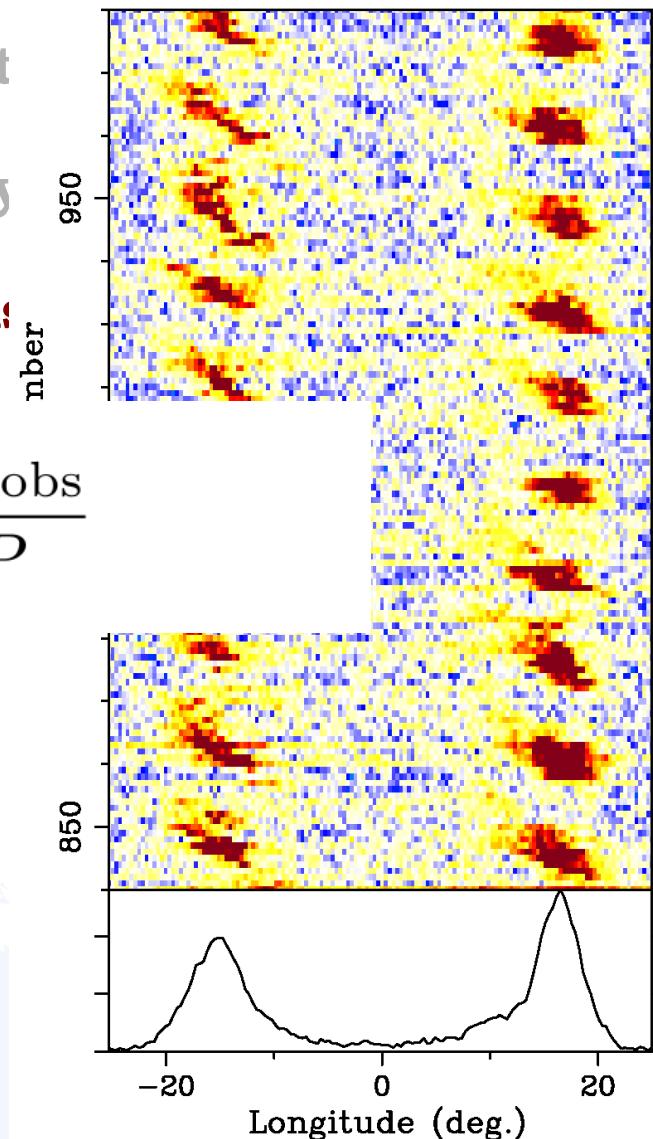
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# Observable Implications...

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- 4. Resolving the aliasing in subpulse

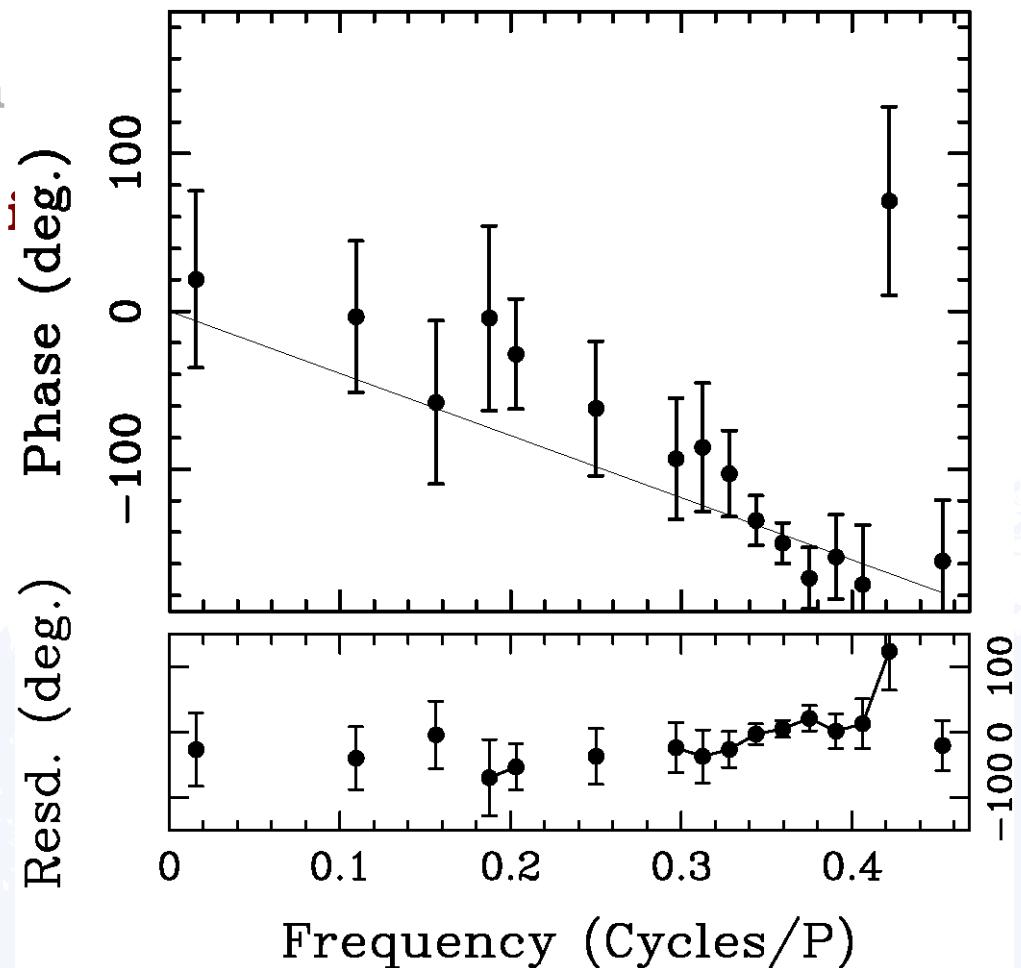
$$\Delta\Theta_{\text{obs}} = 2\pi \left( n + \frac{P}{P_3^{\text{obs}}} \right) \frac{\Delta t_{\text{obs}}}{P}$$



# Observable Implications...

- 1. Testing the Carousel model
- 2. Test single frequency multi-altitude emission
- 3. Modeling the emission
- 4. Resolving the aliasing

Within multi-altitude emission scenario,  
modulation in B1237+25 is  
not aliased.



## More implications

- 1. Testing the Carousel model
- 2. Test single frequency multi-altitude emission
- 3. Modeling the emission geometry (particularly alpha)
- 4. Resolving the aliasing in subpulse modulation period
- 5. **A clean probe of any twist in the magnetosphere**

$$\delta\chi_{\text{twist}} \approx \frac{\delta\Theta_{\text{twist}}}{N_{sp}} = \frac{\Delta\Theta_1 + \Delta\Theta_2}{2 N_{sp}}$$

# Observable Implications

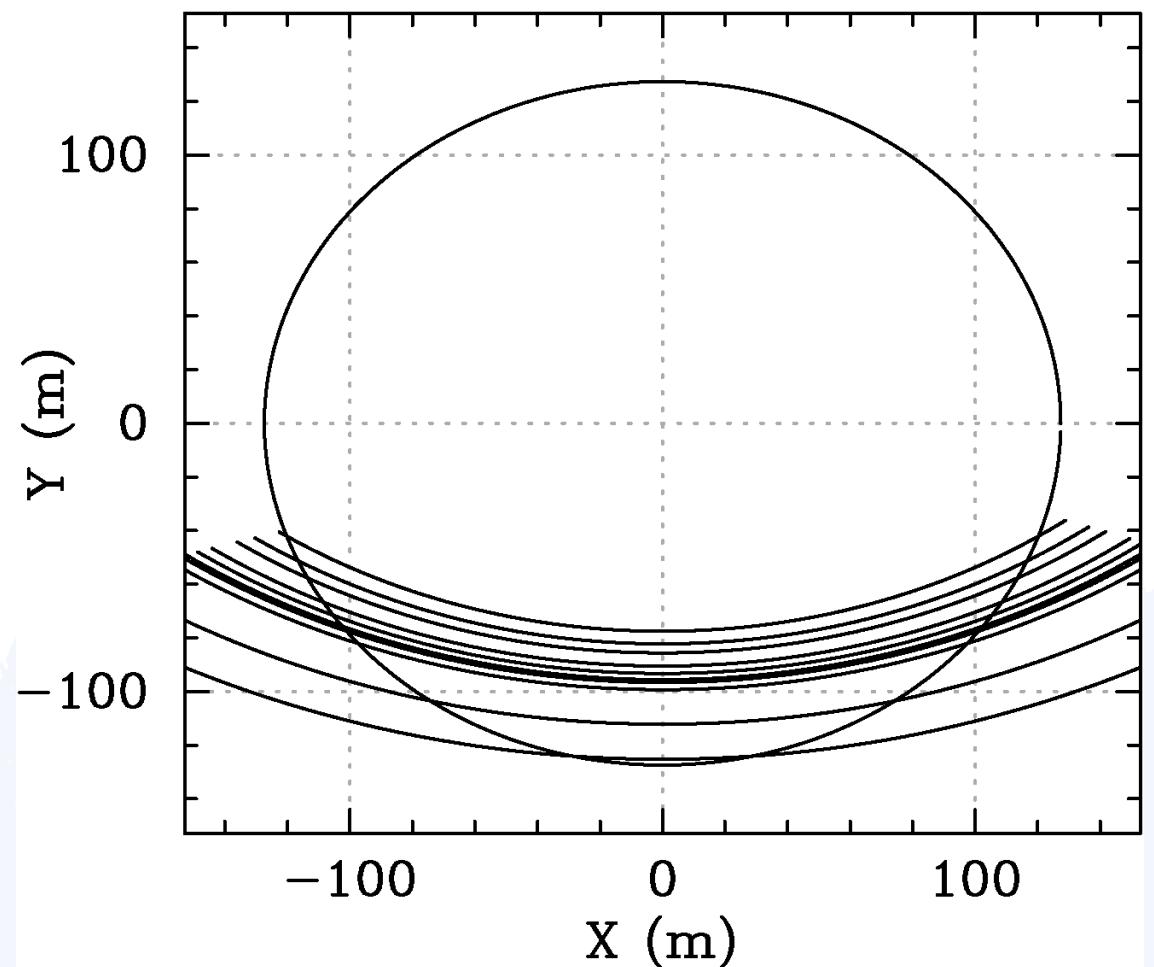
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# Observable Implications

- - **6. Two-dimensional mapping of the emission-beam**

Even if the carousel circulation time is unknown.

Scope for making a global map of emission beam using only average profiles.

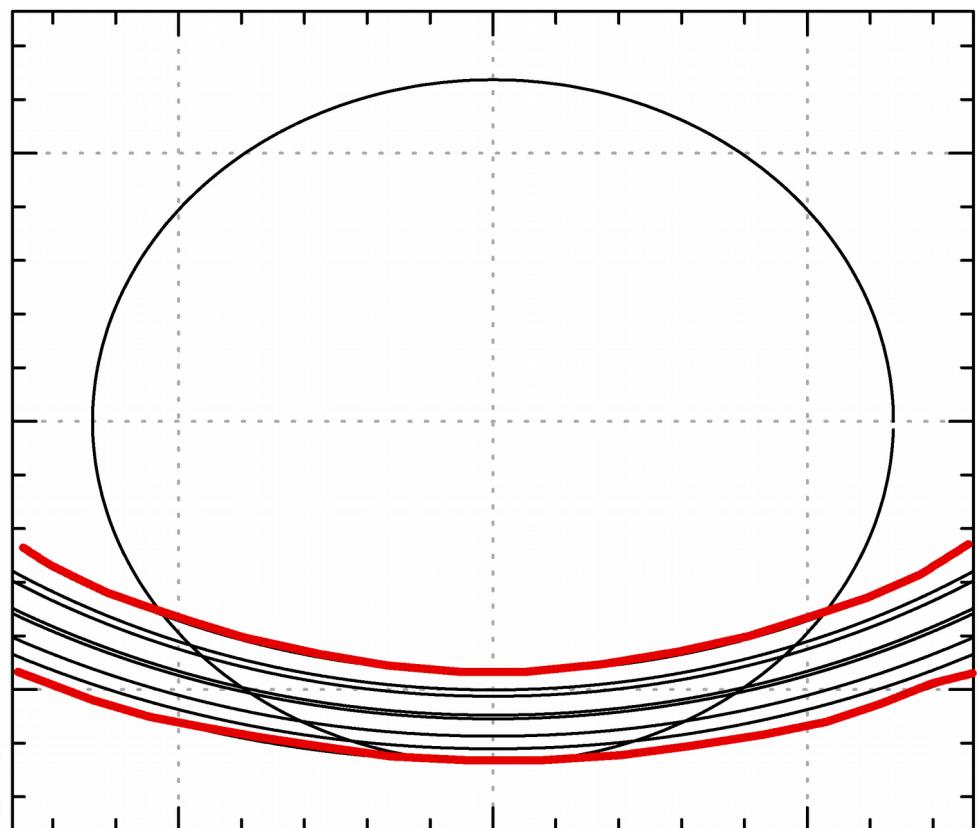


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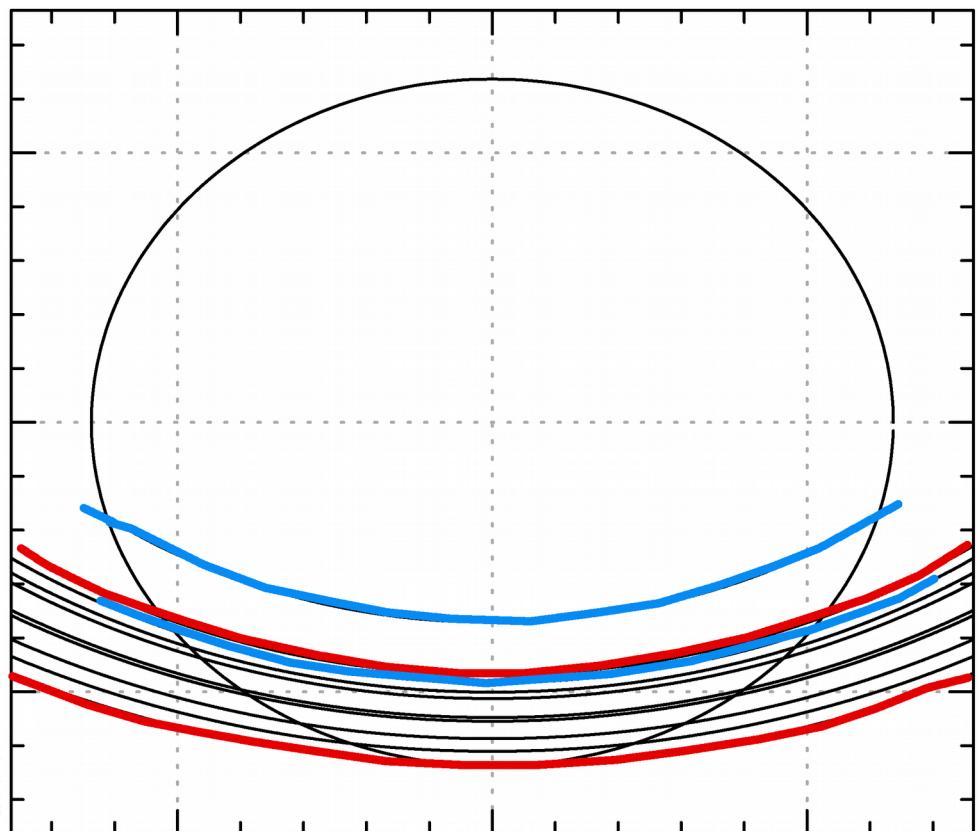
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Scope for making a global map of emission beam using only average profiles.

GMRT+LOFAR (30–1500 MHz) would provide a significant coverage of the beam.



# Summary

**A viewing-geometry induced subpulse phase-offset is predicted in simultaneous multi-frequency observations.**

- **Observations of B0943+10 (and B0809+74) already confirm this geometrical effect (Bilous 2018, A&A).**
- **Observed phase-offsets in B1237+25 provide firm support for multi-altitude emission scenario (Maan 2019, ApJ).**
- **This geometrical effect is extremely useful in stringent tests of the carousel model, 2D mapping of the emission-beam and resolving the aliasing of  $P_3$  (work in progress).**

