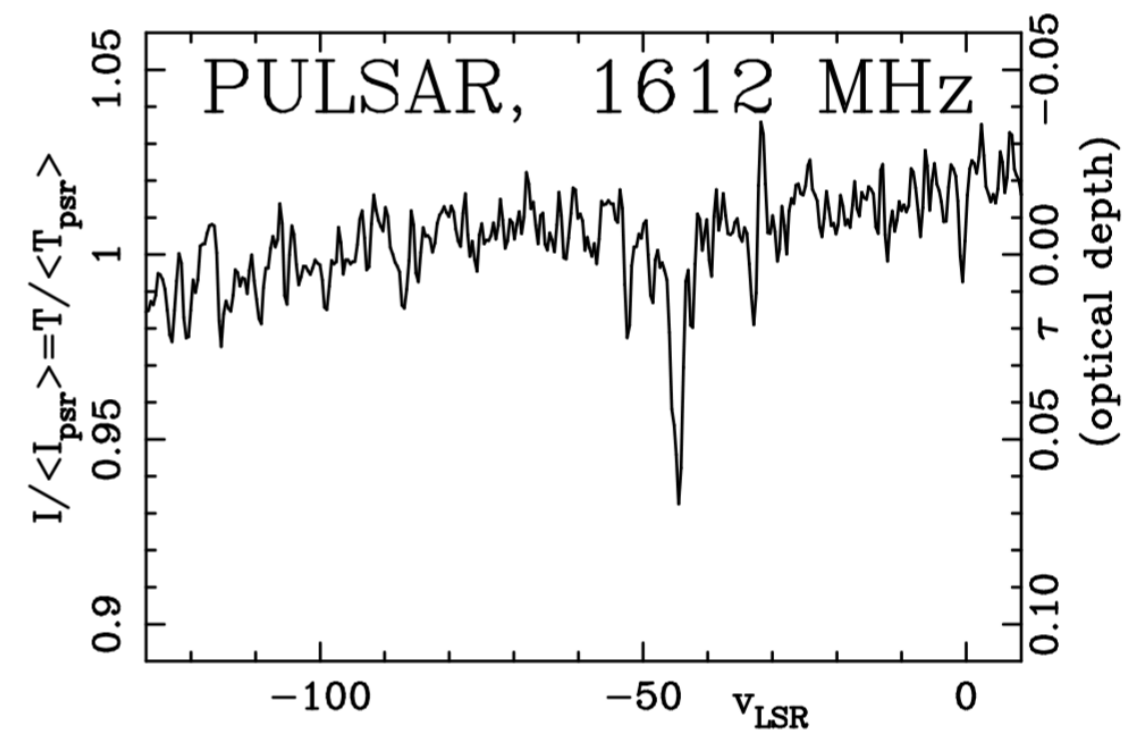
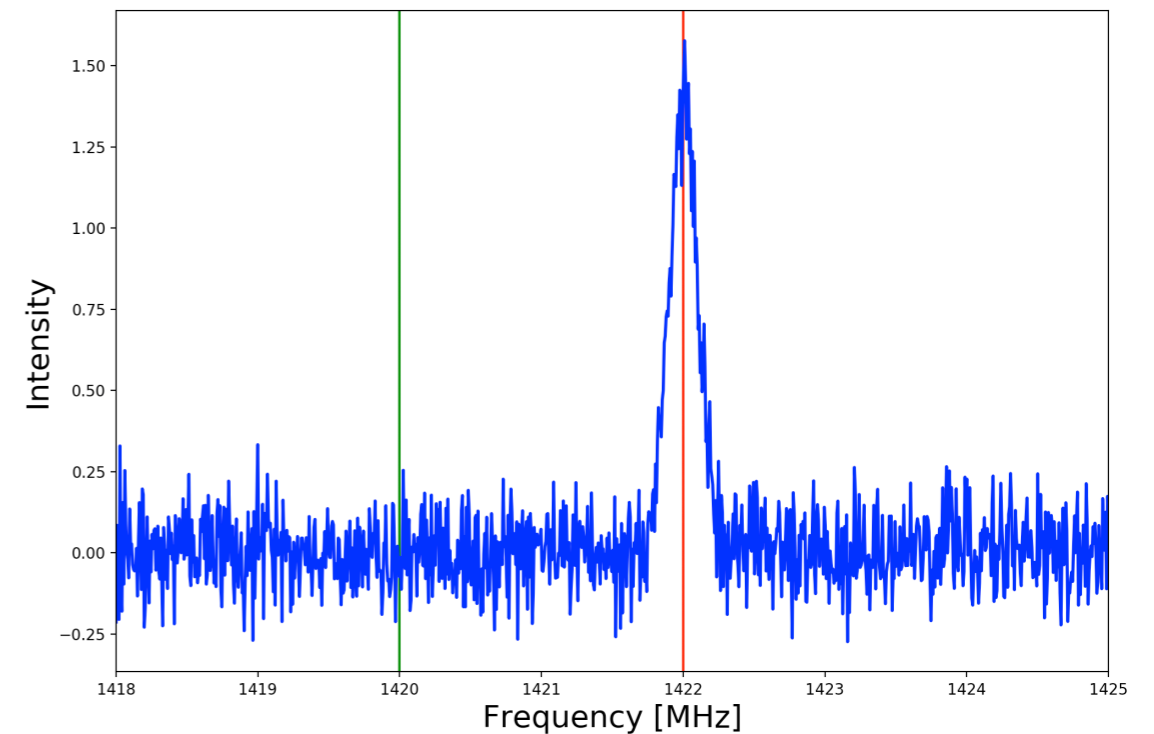


# Spectral Line Techniques

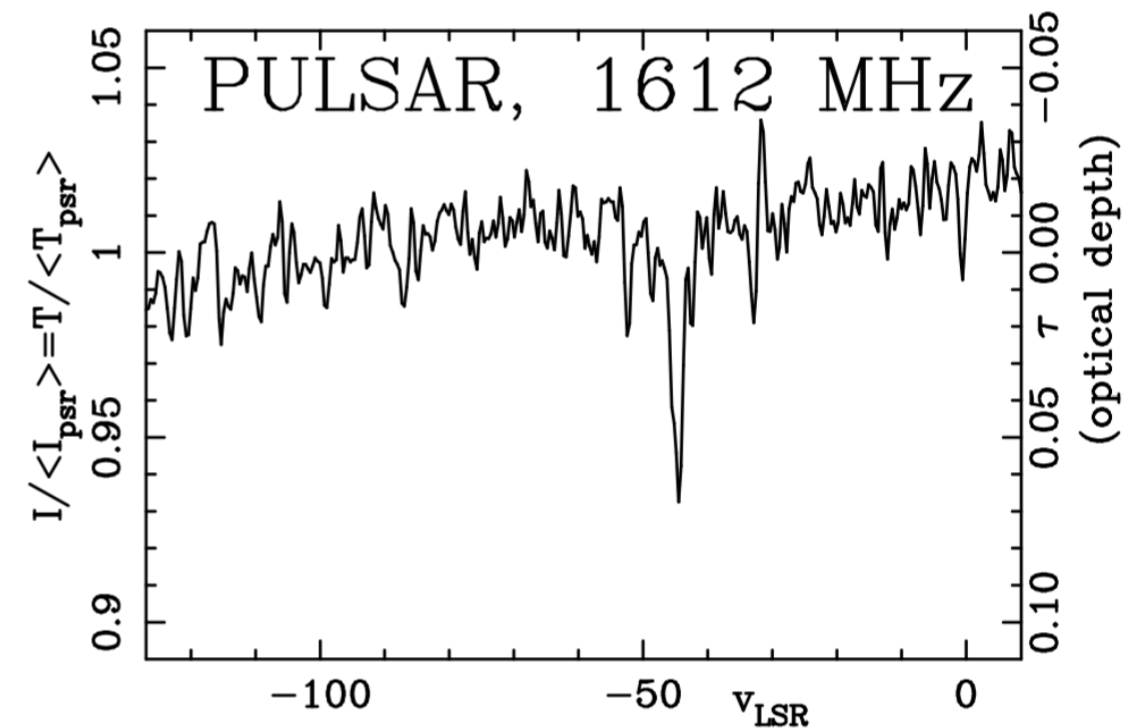
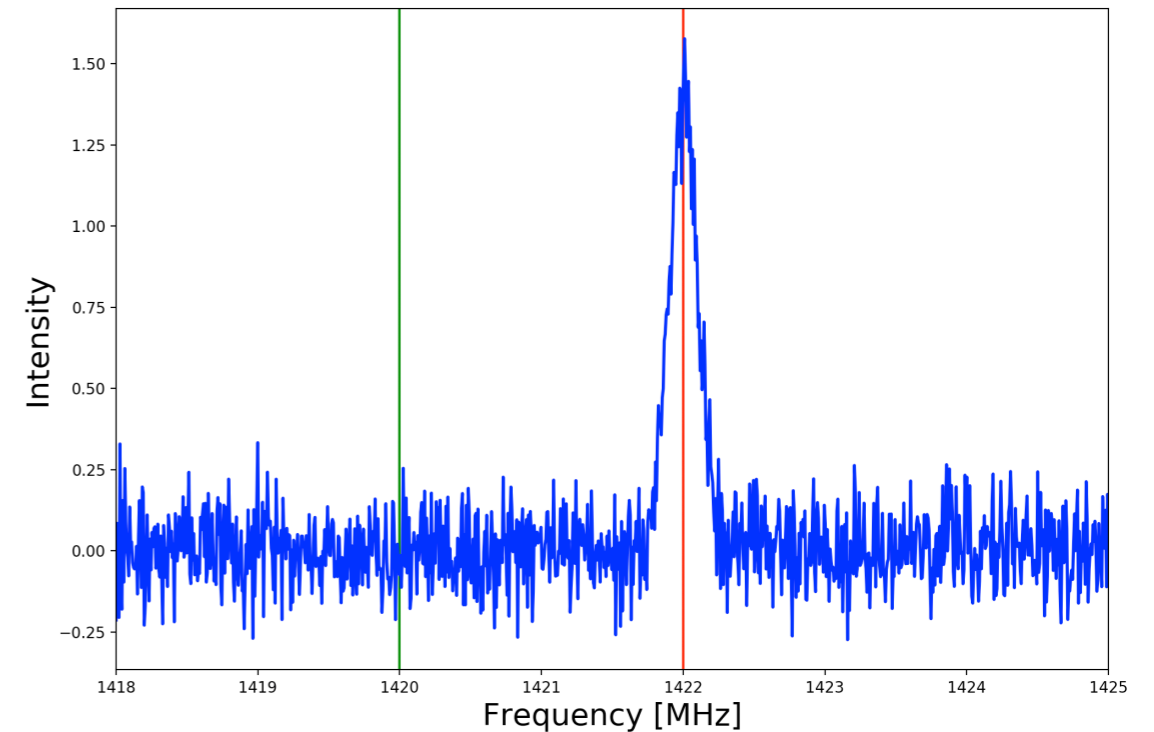
Prasun Dutta

*email: [pdutta.phy@itbhu.ac.in](mailto:pdutta.phy@itbhu.ac.in)*



# Spectral Line Techniques

- Most of the emission is restricted to a narrow frequency range
- The transitions are well known from atomic/molecular physics
- Emission and Absorption \*
- Almost always have associated continuum emission
- Emission/Absorption can be from extended sources, high resolution image/map making requires to do interferometry.



# Importance to learn spectral line analysis (for continuum studies!)

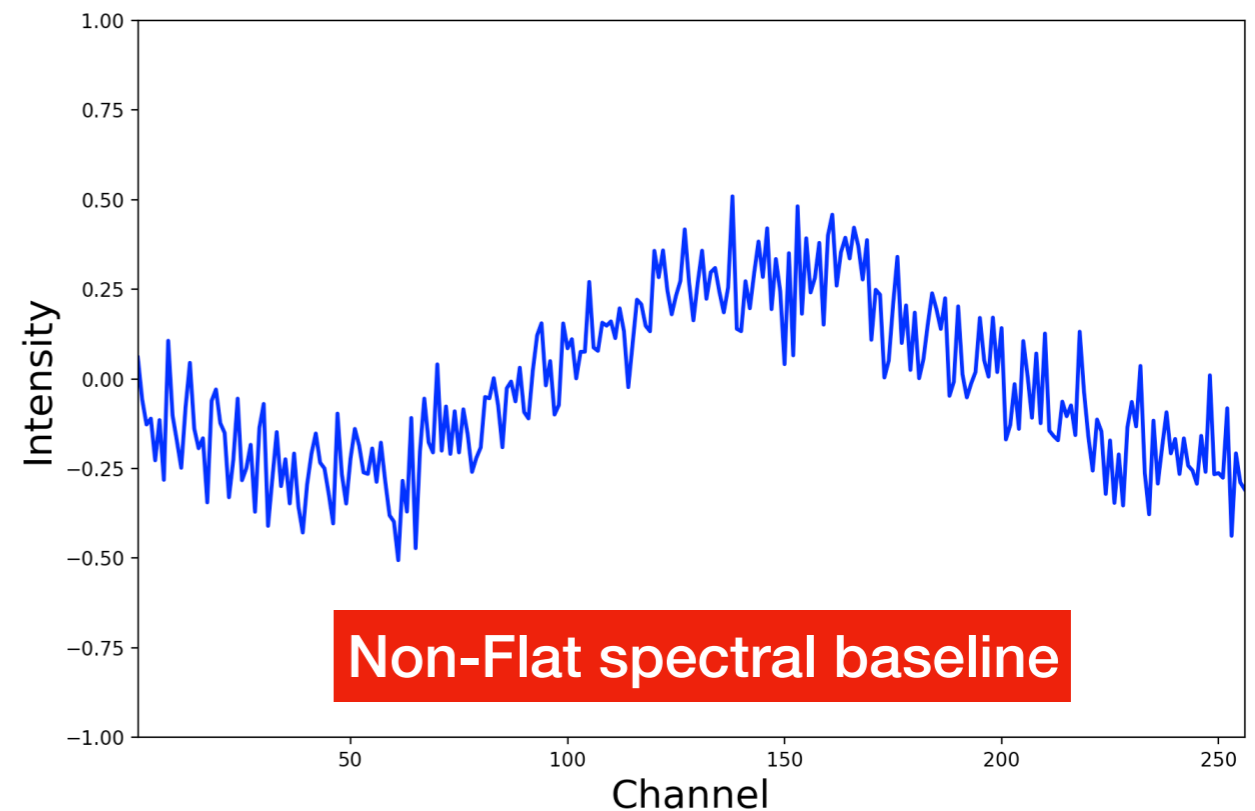
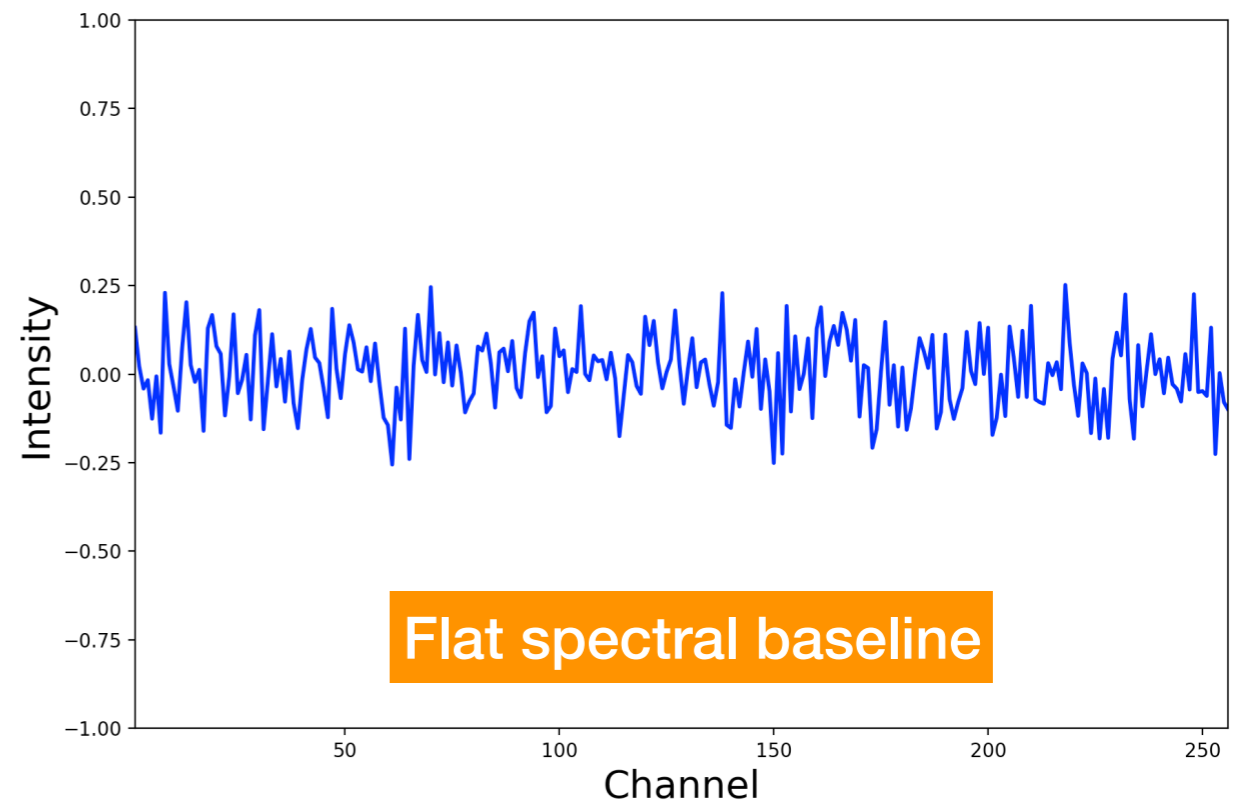
Single channel noise

$$\sigma_N = \frac{\sigma_1}{\sqrt{N}}$$

Averaged over channels

No of Channels

Also continuum subtraction from continuum gives a good way of checking residual RFI!



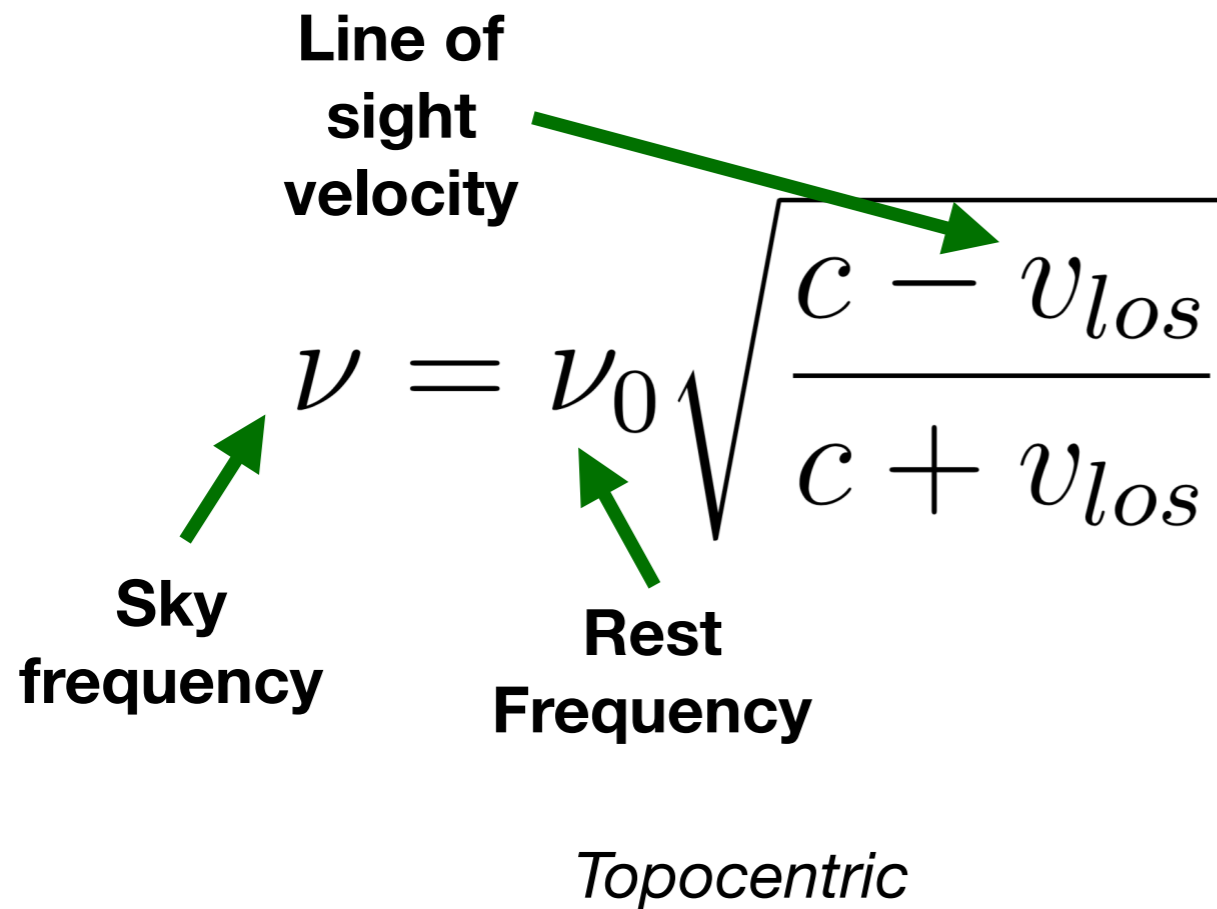
# Timeline

- Observation and Techniques with interferometers
  - Observation Preparation [Nissim again!]
  - Calibration
  - Doppler correction
  - Continuum Subtraction
  - Map making
- Science

# Takeaways for the science case

- What is the line frequency? Cosmological/Doppler redshift. Which frequency band to observe?
- Compact or extended source ? If extended do the interferometer see it all? Choose antenna configuration wisely.
- What velocity/spectral resolution is required?
- What bandwidth is required?
- Galactic/extragalactic line?

# Doppler correction I



$$z_{rad} = \frac{\nu - \nu_0}{\nu_0}$$

$$z_{opt} = \frac{\nu - \nu_0}{\nu}$$

| Frame Name     | Correction       | Velocity (km/sec) |
|----------------|------------------|-------------------|
| Geocentric     | Earth Spin       | 0.5               |
| Heliocentric   | Earth revolution | 30                |
| LSR            | Sun Motion       | 20                |
| Galactocentric | Galaxy rotation  | 230               |
| Local Group    | LG motion        | 100               |

**Varies with time !**

**Varies across dates!**

**For Galactic observations**

**For Extragalactic**

**For high redshift**

# Choice of channel width, bandwidth and NChan

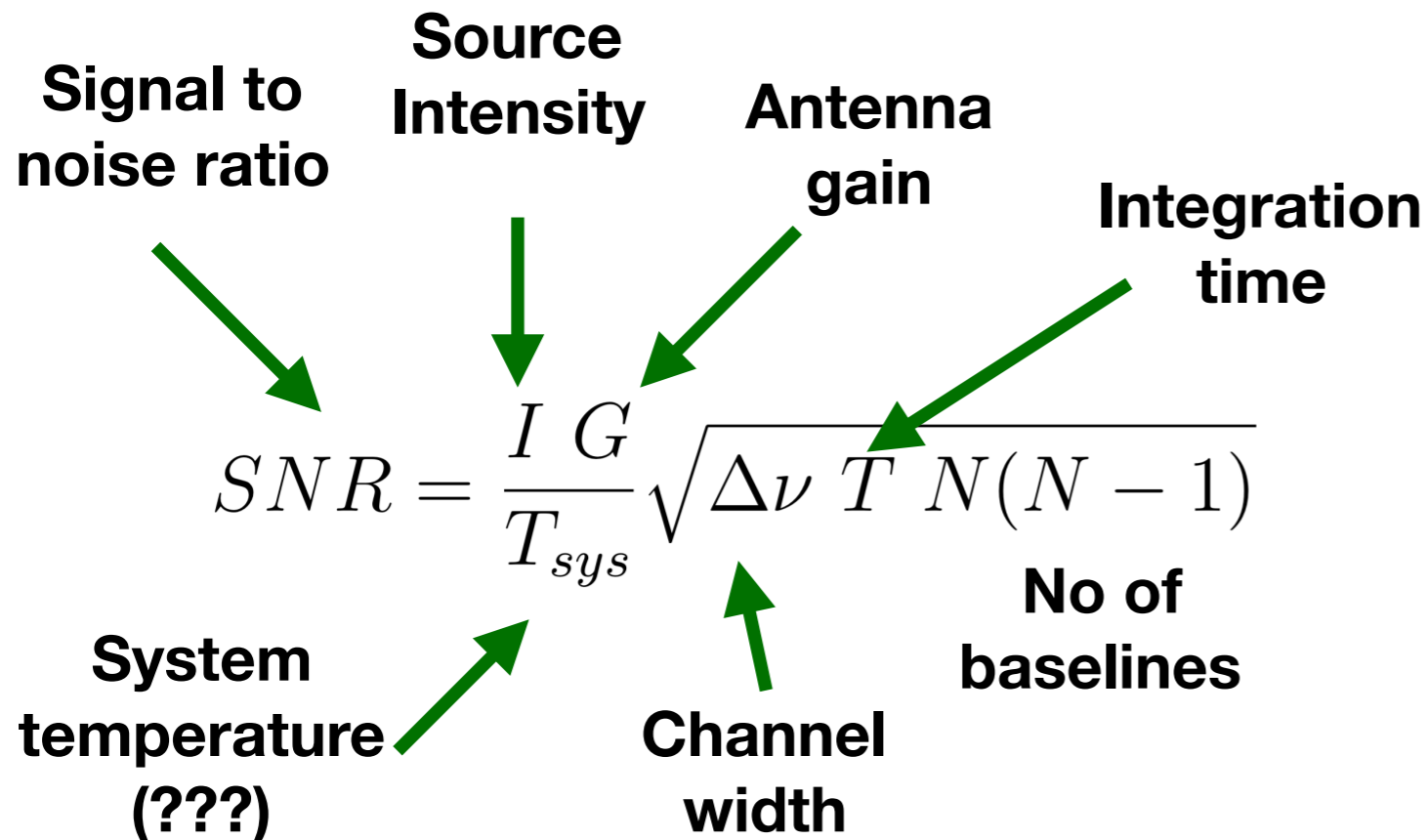
- First select the channel width required. (say 8.0 KHz)
- Guess the width of the spectral line/feature and keep enough spectral baselines in both sides. That decides the bandwidth. (say 3.8 MHz)
- Bandwidth/Channel width gives you number of spectral channel = NChan (~180)
- Choose these parameters now from one of the available sets.
- Should check the data rate!

|                                   |  |      | <b>Bandwidth</b>  | <b>Channels</b> | <b>Integ. Time</b> |
|-----------------------------------|--|------|---|-----------------|--------------------|
| Interferometry :<br>Spectral Line | Total Intensity<br>(16 MHz and<br>lower BW<br>modes) | 16,6 | 16 / N<br>(N=4,8,16..128)<br>(viz. 4, 2, 1,<br>0.5,0.25 & 0.125<br>MHz) | 512, 256        | 2,4,8..(sec)       |

**Check the GWB setups and figure out what you will do.**

# Choosing Bandpass calibrator(s)

- \*Need to choose phase and flux calibrators (Ishwar)
- Bandpass Calibration: Calibration for the spectral response of Interferometer.
- A calibrator source is used, the source need not be a point source.
- If the phase calibrator has enough flux then that can be used. Calibrator spectra need to be flat!



$$SNR_{BP} \gg SNR_{TS}$$

$$T_{BP} = \left[ \frac{I_{TS}}{I_{BP}} \right]^2 T_{TS}$$

**Remember bandpass slowly changes with time!**



# Choosing Bandpass Methods(s)

- Main spectral response come from the baseband filter
- **Position Switching:** By observing a strong calibrator source near to the target source. Almost all observation not involving spectral line from our galaxy uses this method.
- **Frequency Switching:** Shift the sky frequency. This does not change the response of the bandpass filter. Almost all observations involving spectral line from our galaxy uses this method.
  - **Frequency switching (In band):** If a large bandwidth is available, one can switch the frequency inside the band itself. This improve the signal to noise.
- Choosing calibrator with low optical depth.

| Source                 | Coordinates<br>( $l, b$ ) | $S_{1.4}^a$<br>Jy | $\tau_{\text{rms}}^b$<br>$\times 10^{-3}$ | $\tau_{\text{peak}}$ |
|------------------------|---------------------------|-------------------|---|----------------------|
| <u>GMRT targets:</u>   |                           |                   |   |                      |
| B0316+162              | 166.6, -33.6              | 7.8               | 0.75                                      | 0.496                |
| B0438-436              | 248.4, -41.6              | 5.0               | 1.46                                      | < 0.0009             |
| B0531+194              | 186.8, -7.1               | 6.8               | 0.99                                      | 0.631                |
| B0834-196 <sup>g</sup> | 243.3, +12.6              | 5.0               | 1.08                                      | 0.187                |
| B1151-348              | 289.9, +26.3              | 5.0               | 1.05                                      | 0.120                |
| B1245-197              | 302.0, +42.9              | 5.3               | 1.23                                      | 0.032                |
| B1345+125              | 347.2, +70.2              | 5.2               | 1.07                                      | 0.086                |
| B1827-360              | 358.3, -11.8              | 6.9               | 0.89                                      | 0.227                |
| B1921-293              | 9.3, -19.6                | 6.0               | 1.02                                      | 0.377                |
| B2223-052              | 59.0, -48.8               | 5.7               | 0.79                                      | 0.148                |
| <u>WSRT targets:</u>   |                           |                   |   |                      |
| B0023-263              | 42.3, -84.2               | 7.5               | 1.04                                      | 0.0037               |
| B0114-211              | 167.1, -81.5              | 3.7               | 1.58                                      | 0.044                |
| B0117-155              | 154.2, -76.4              | 4.2               | 1.51                                      | 0.0067               |
| B0134+329 <sup>g</sup> | 134.0, -28.7              | 16.5              | 0.53                                      | 0.058                |
| B0202+149              | 147.9, -44.0              | 3.5               | 0.98                                      | 0.084                |
| B0237-233              | 209.8, -65.1              | 5.7               | 1.19                                      | 0.116                |
| B0316+413              | 150.6, -13.3              | 23.9              | 0.49                                      | 0.230                |
| B0355+508              | 150.4, -1.6               | 5.3               | 2.12                                      | 6.438                |
| B0404+768              | 133.4, +18.3              | 5.8               | 1.16                                      | 0.424                |
| B0429+415              | 161.0, -4.3               | 8.6               | 0.90                                      | 0.716                |
| B0518+165              | 187.4, -11.3              | 8.5               | 1.08                                      | 1.130                |
| B0538+498              | 161.7, +10.3              | 22.5              | 0.49                                      | 0.912                |
| B0831+557              | 162.2, +36.6              | 8.8               | 1.15                                      | 0.089                |
| B0906+430              | 178.3, +42.8              | 3.9               | 0.82                                      | 0.0059               |
| B1328+254              | 22.5, +81.0               | 6.8               | 0.33                                      | 0.0016               |
| B1328+307              | 56.5, +80.7               | 14.7              | 0.30                                      | 0.0082               |
| B1611+343              | 55.2, +46.4               | 4.8               | 0.72                                      | 0.0033               |
| B1641+399              | 63.5, +40.9               | 8.9               | 0.49                                      | 0.0014               |

# Bandpass Calibration

$$V_{AB}^{sky}(\nu) = \langle E_A^* E_B \rangle$$

- The spectral variation of bandpass is weak.

**Measured** **Unknown**

$$V_{AB}^{obs}(t, \nu) = \mathcal{G}_{AB}(t, \nu) V_{AB}^{sky}(\nu)$$

**Calibration is to know this.**

$$\mathcal{G}_{AB}(t, \nu) = g_{AB}(t) B_{AB}(t, \nu)$$

**Baseline based** **Fast variation In time** **Slow variation In time**

- If single channel does not have enough signal to noise, some channels can be averaged to gain in sensitivity for temporal calibration ( $g_{AB}$ ).

- The temporal variation in  $g_{AB}$  may not be weak, but the temporal variation in  $B_{AB}$  is weak.

# Bandpass Calibration

Measured

Unknown

Known

$$V_{AB}^{band}(t, \nu) = g_{AB}(t) B_{AB}(t, \nu) V_{AB}^{sky}$$
$$V_{AB}^{band}(t, \nu_0) = g_{AB}(t) B_{AB}(t, \nu_0) V_{AB}^{sky}$$

**Amplitude and Phase Calibration**

- We first do calibration for a given channel ( $\nu_0$ ) and find the stronger temporal variations in gain,  $g_A(t)$ .

# Bandpass Calibration

| Measured                  |   | Unknown                      |  | Known          |
|---------------------------|---|------------------------------|--|----------------|
| $V_{AB}^{band}(t, \nu)$   | = | $g_{AB}(t) B_{AB}(t, \nu)$   |  | $V_{AB}^{sky}$ |
| $V_{AB}^{band}(t, \nu_0)$ | = | $g_{AB}(t) B_{AB}(t, \nu_0)$ |  | $V_{AB}^{sky}$ |

$$\frac{V_{AB}^{band}(t, \nu)}{V_{AB}^{band}(t, \nu_0)} = \frac{B_{AB}(t, \nu)}{B_{AB}(t, \nu_0)} = B'_{AB}(t, \nu)$$

**AIPS: BPASS, BPASSPRM(5) = 1, BPASSPRM(10) = 3**

$$B'_{AB}(t, \nu) = b_A^*(t, \nu) b_B^*(t, \nu)$$

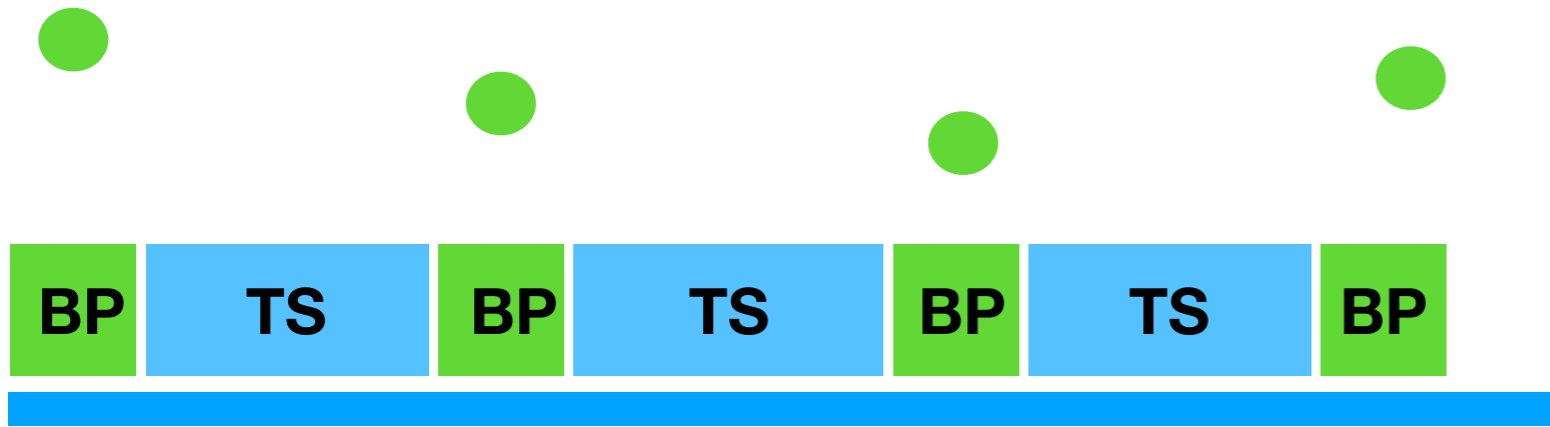
**N antenna -> N(N-1)/2 measurements**

- We first do calibration for a given channel ( $\nu_0$ ) and find the stronger temporal variations in gain,  $g_A(t)$ .
- If the bandpass calibrator is not a point source, then the visibilities at different baselines can be different. Do not worry, the variation with baseline is taken care of when you do the (complex) division.
- Gains are antenna based

# Bandpass Calibration

$$B'_{AB}(t, \nu) = b_A^*(t, \nu)b_B^*(t, \nu)$$

**N antenna -> N(N-1)/2 measurements**



**Single Baseline, Time** →

## AIPS: DOBAND

- = 1 : Average everything
- = 2 : Nearest in time
- = 3 : Interpolate in time

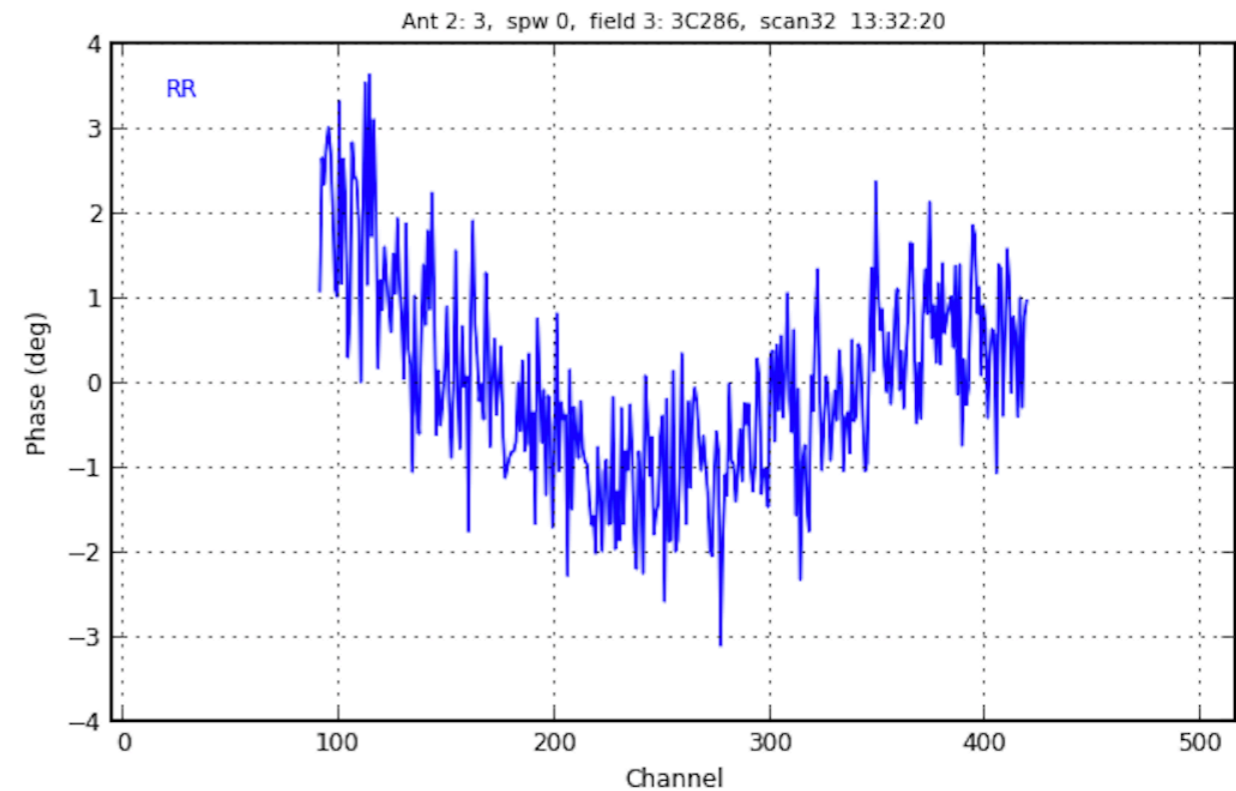
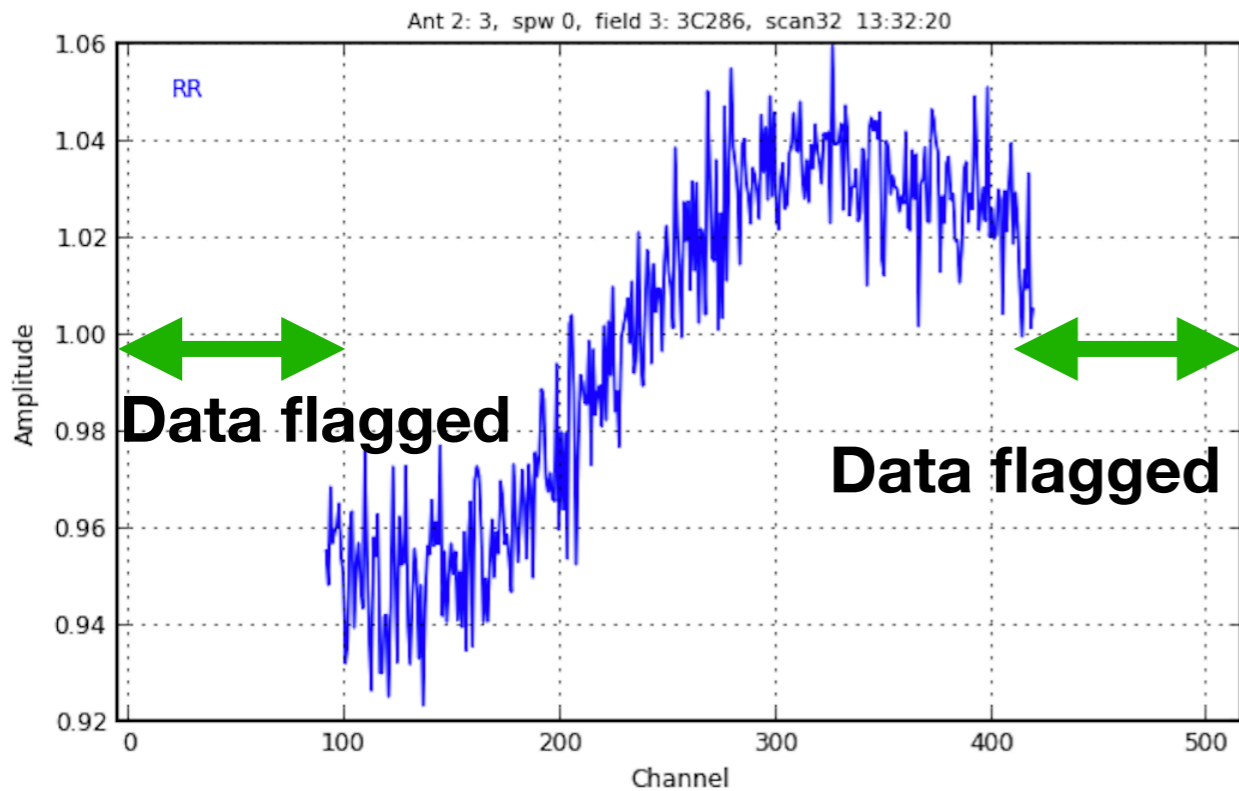
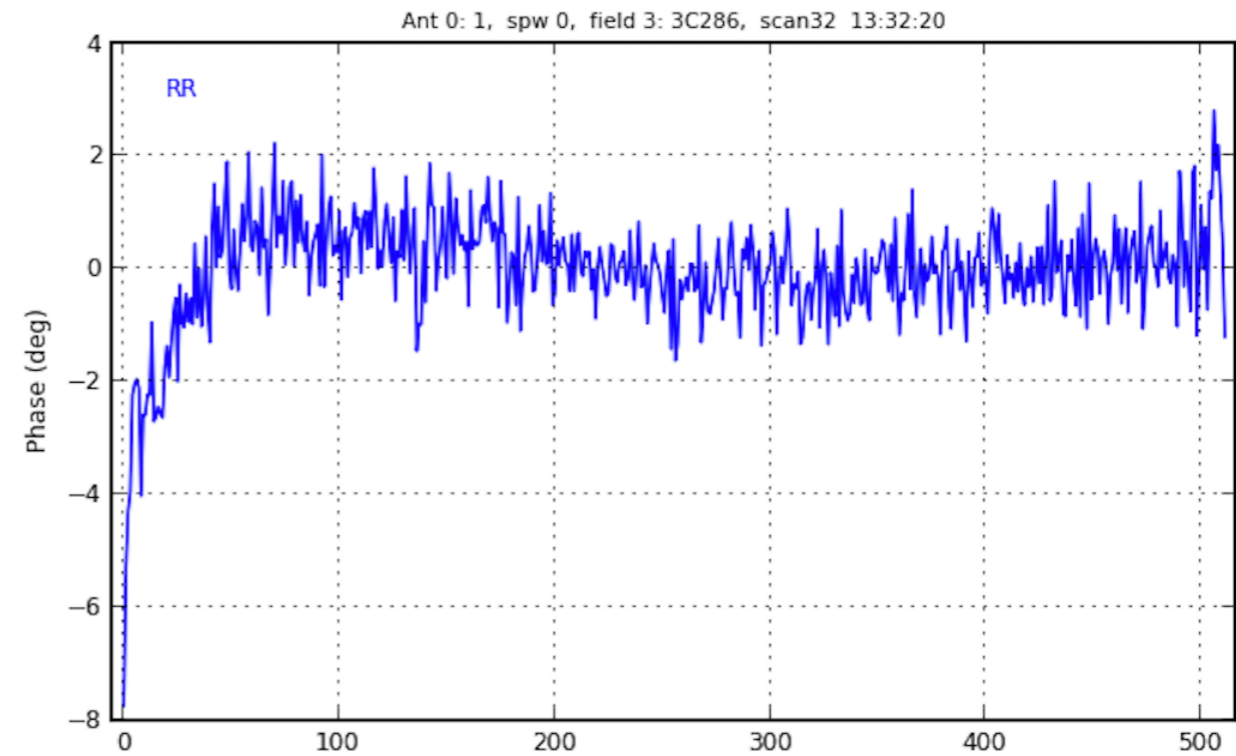
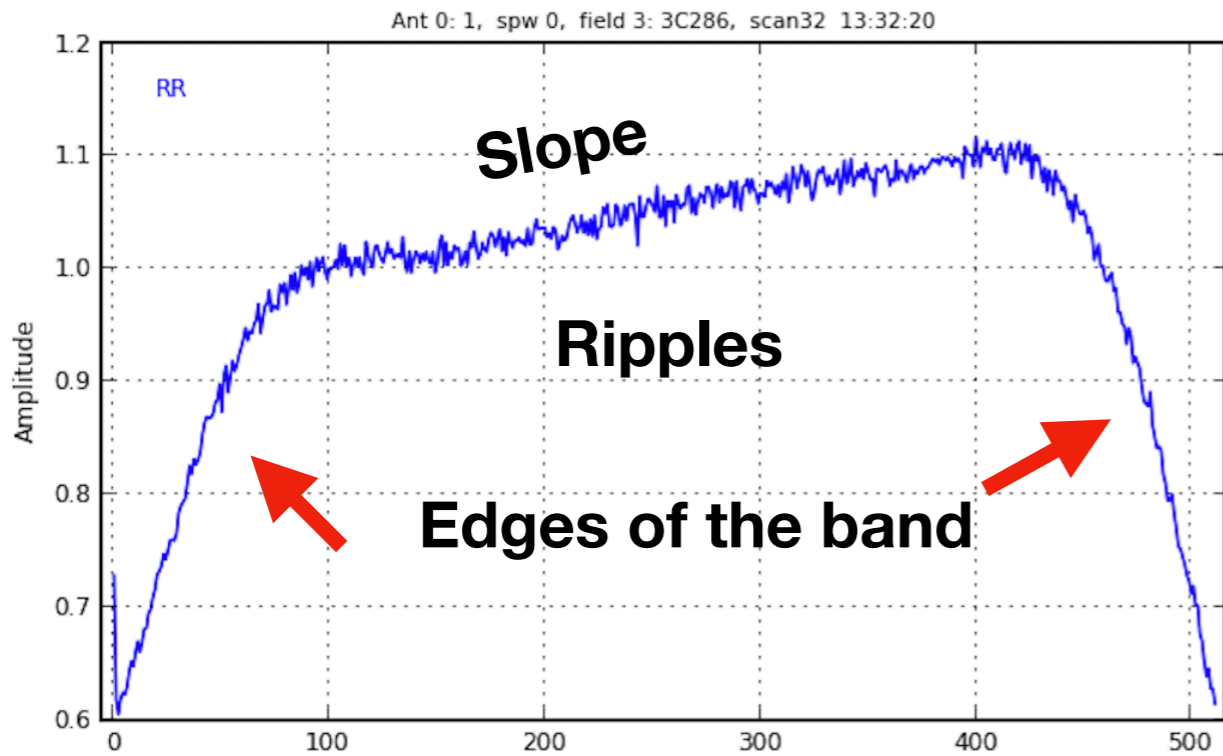


*When only one observation*

*Check which gives better result*

- In case you have many observations of bandpass, interpolate in time/use nearest bandpass in time.
- If you happened to have only one... or two bandpass separated over large time, then just average all entries.
- Polynomial fit across time/frequency also can be tried.

# Bandpass Calibration



# Bandpass Calibration

- Data need to be FLAGGED for different spectral lines too.
- Bandpass solutions for bad antennas are often completely different from the good ones... easy identifications.
- Do Scalar averaged cross power spectra and look for spikes (positive or negative) and inspect those channels.
- Do FLAGGING and BANDPASS calibration iteratively.

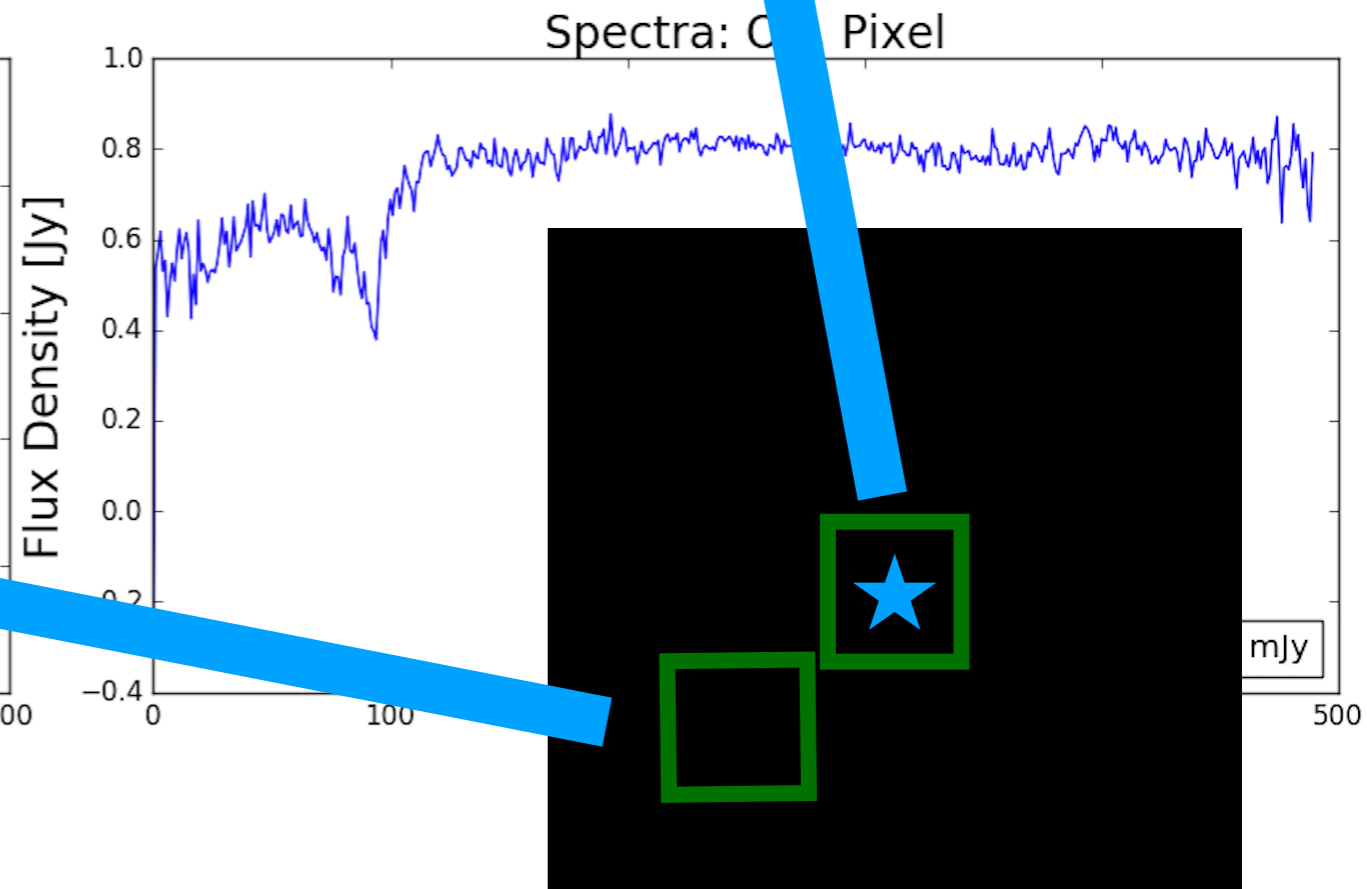
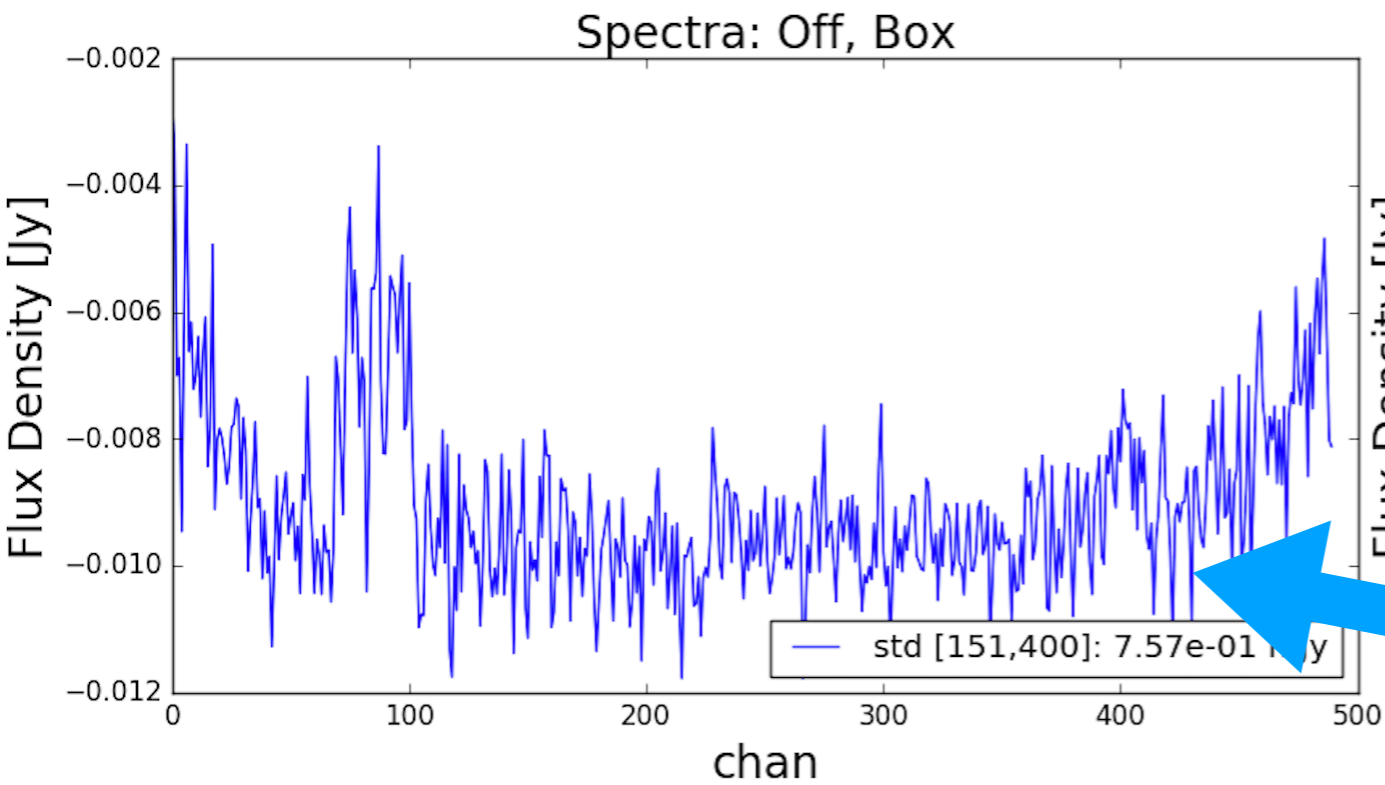
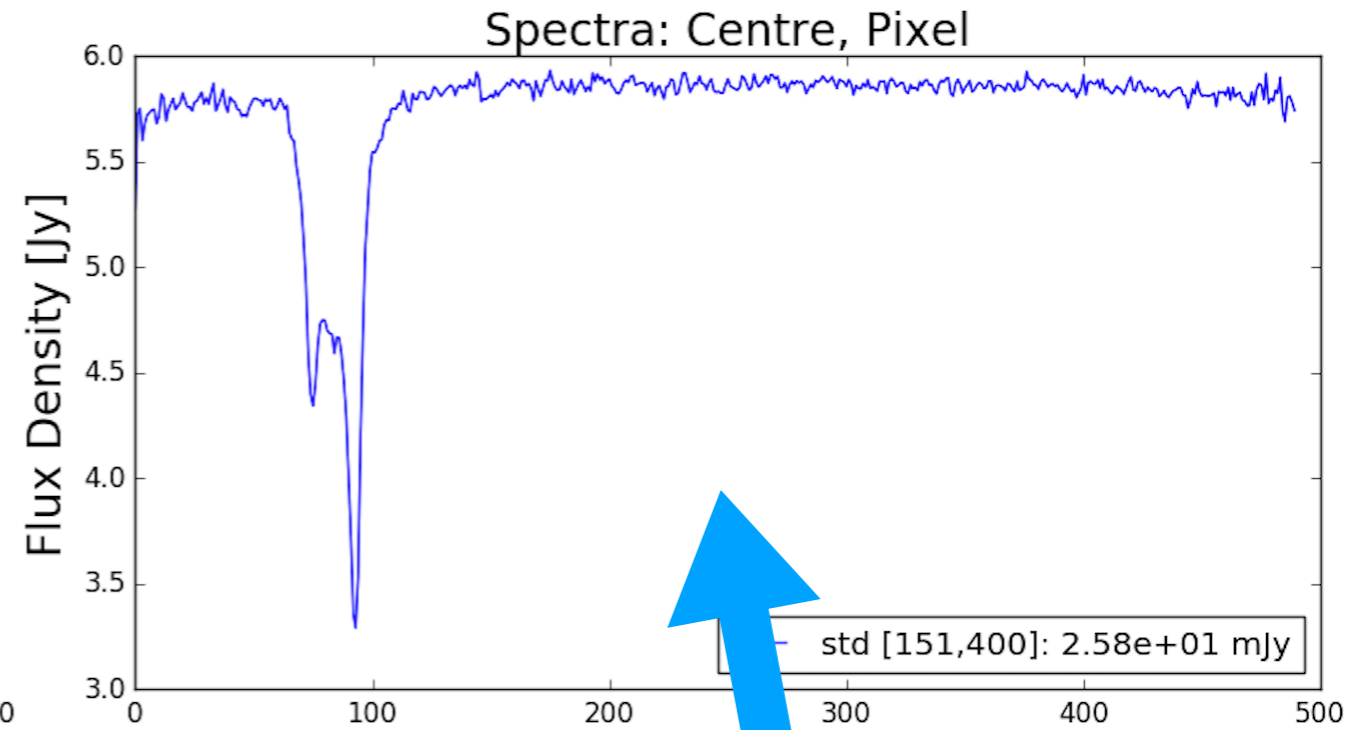
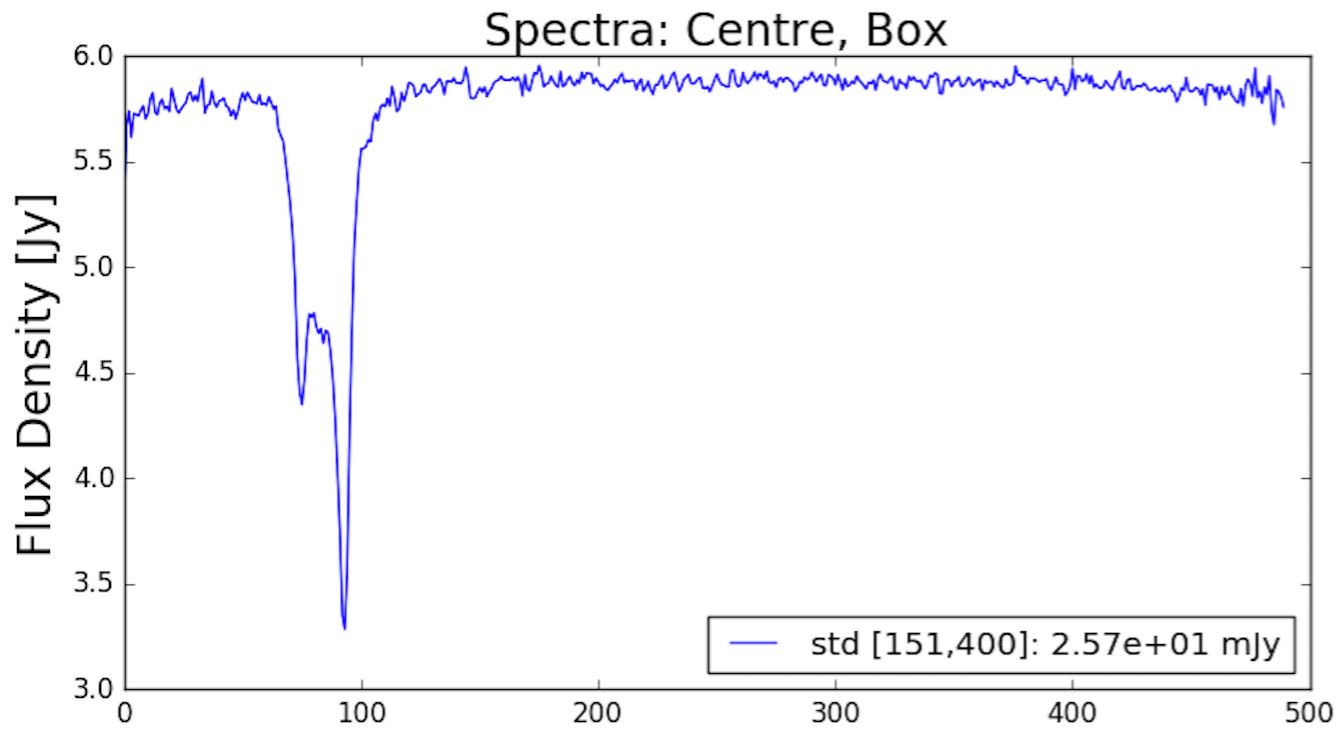
**Scalar Average:**

*Average  
amplitudes  
and phases  
separately*

**Vector Average:**

*Average  
Real and  
Imaginary  
separately*

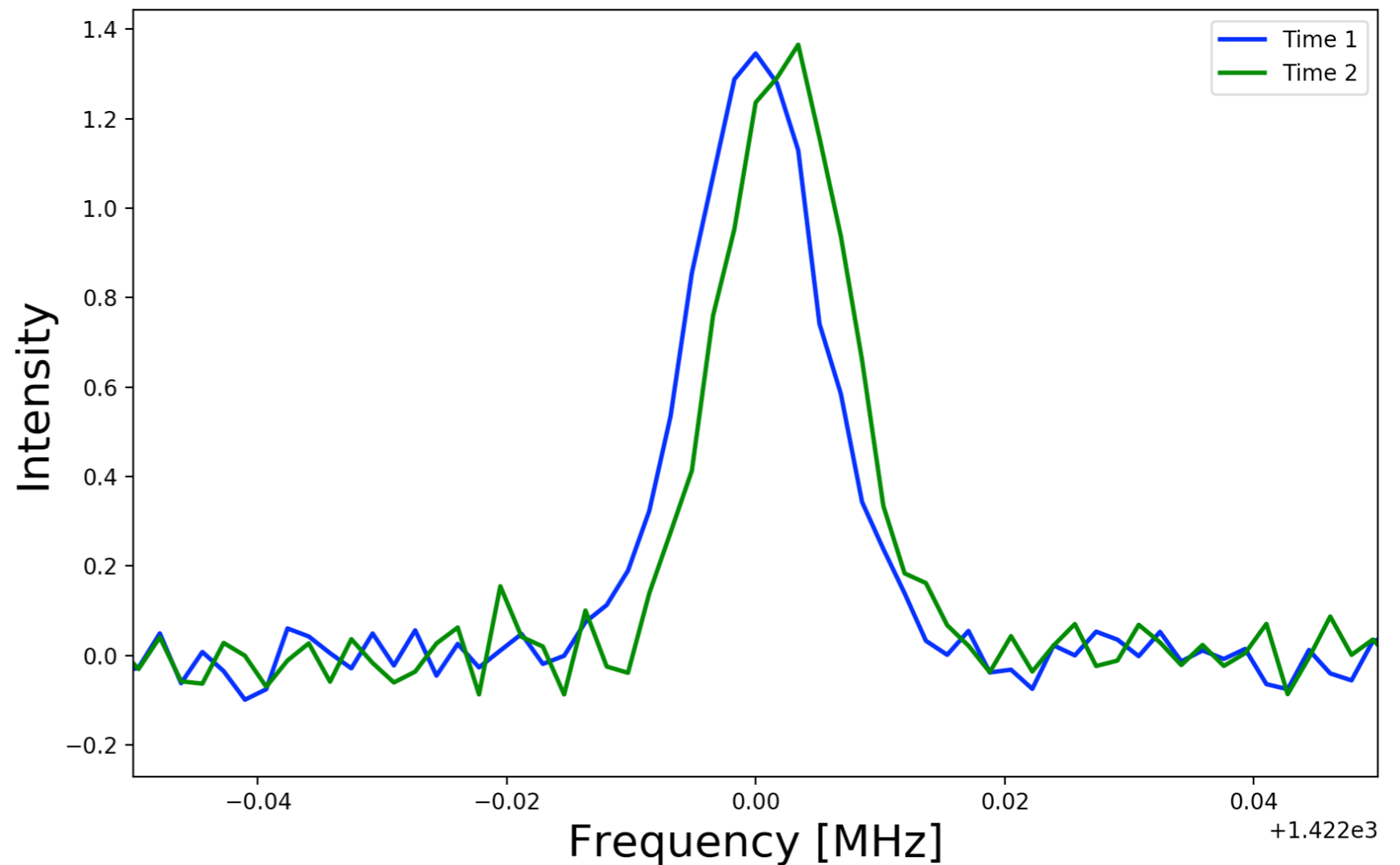
# Bandpass Calibration



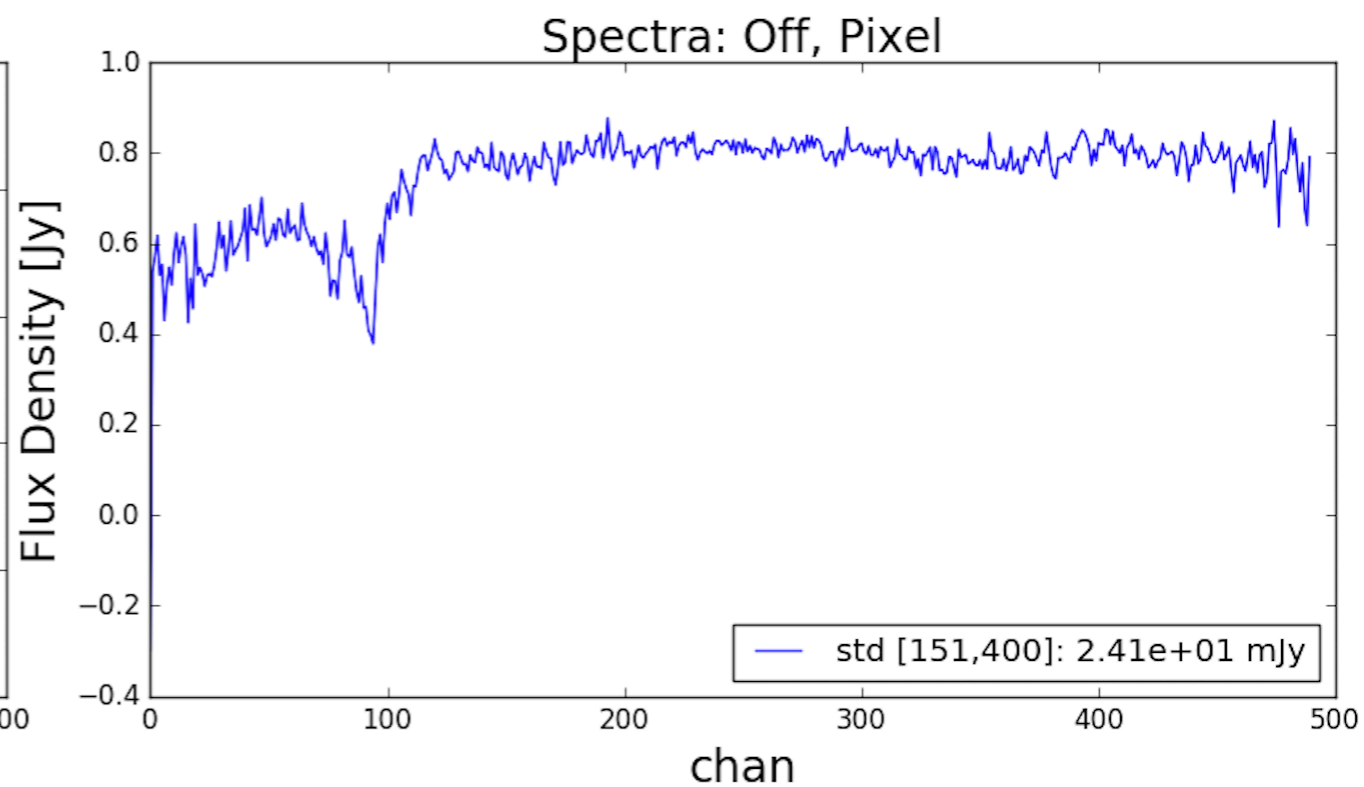
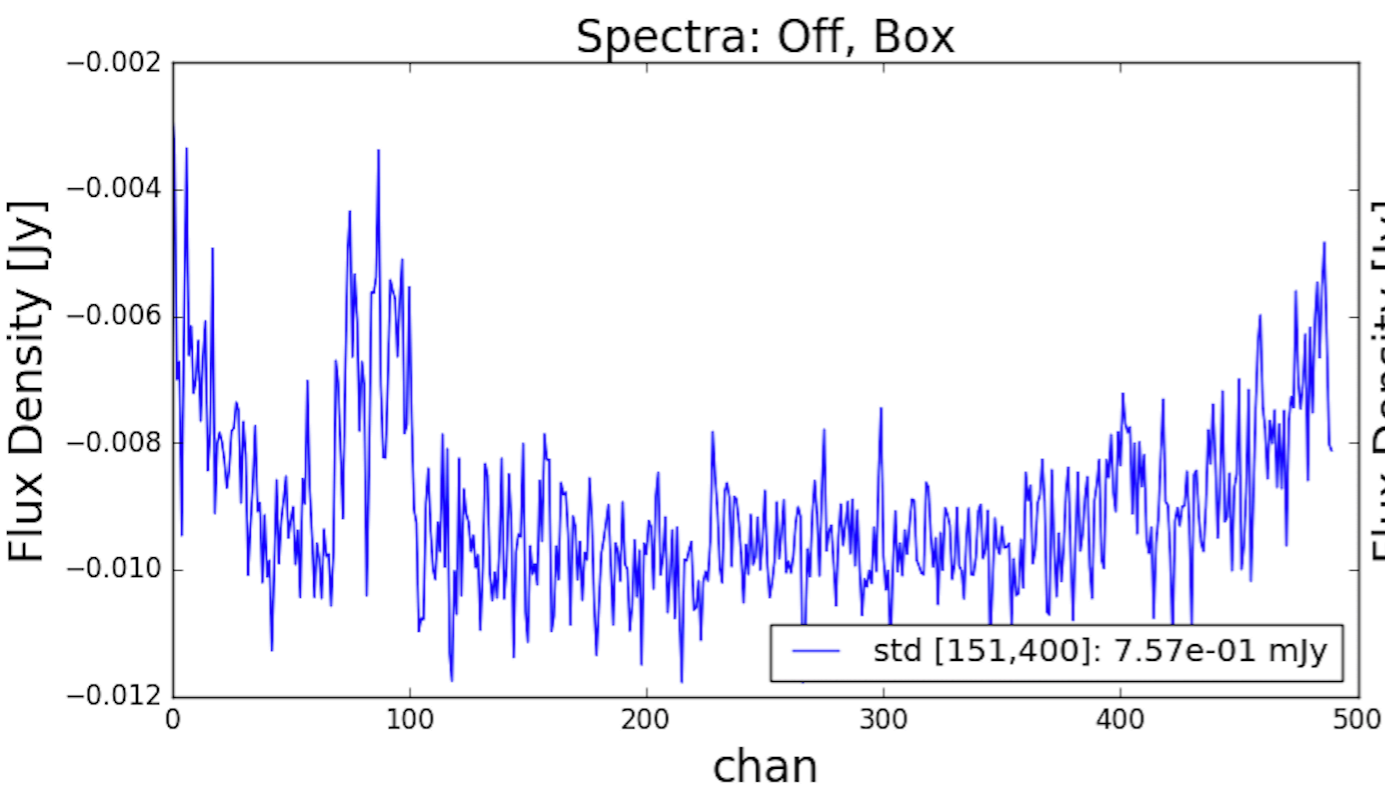
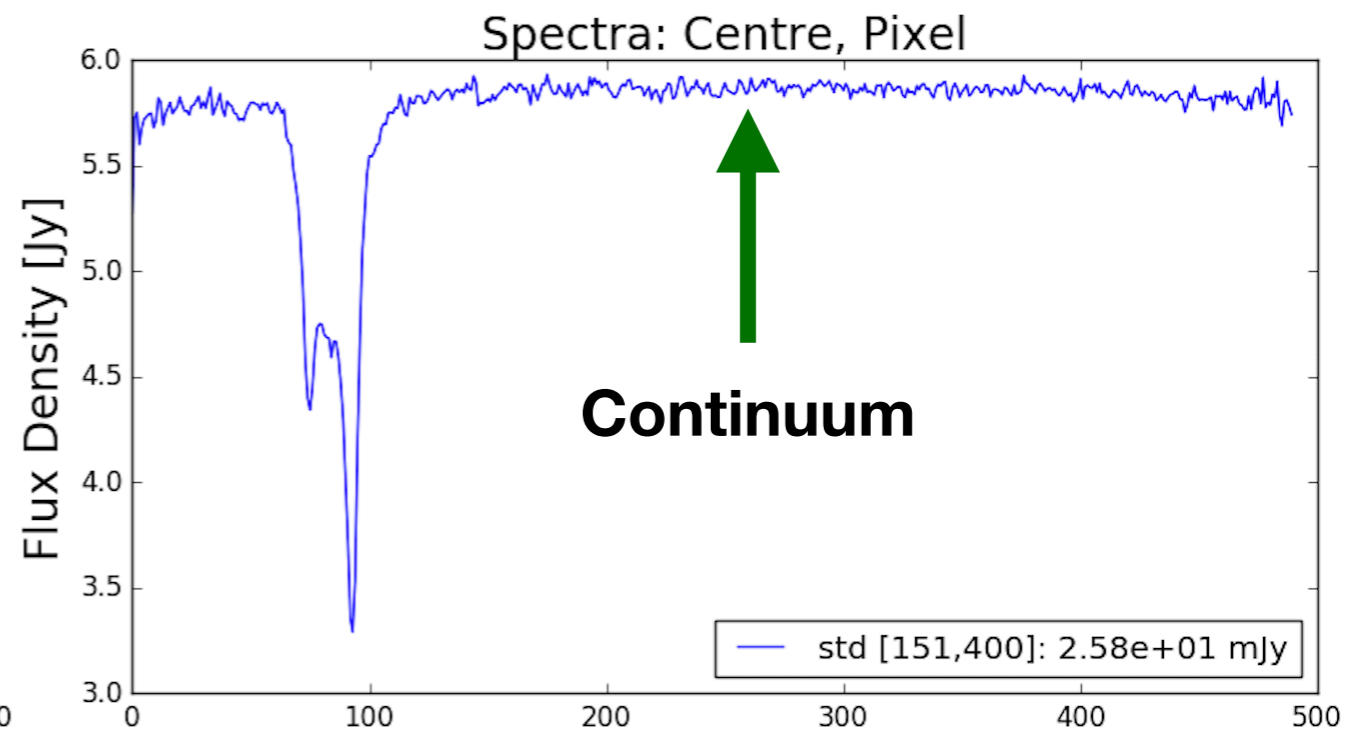
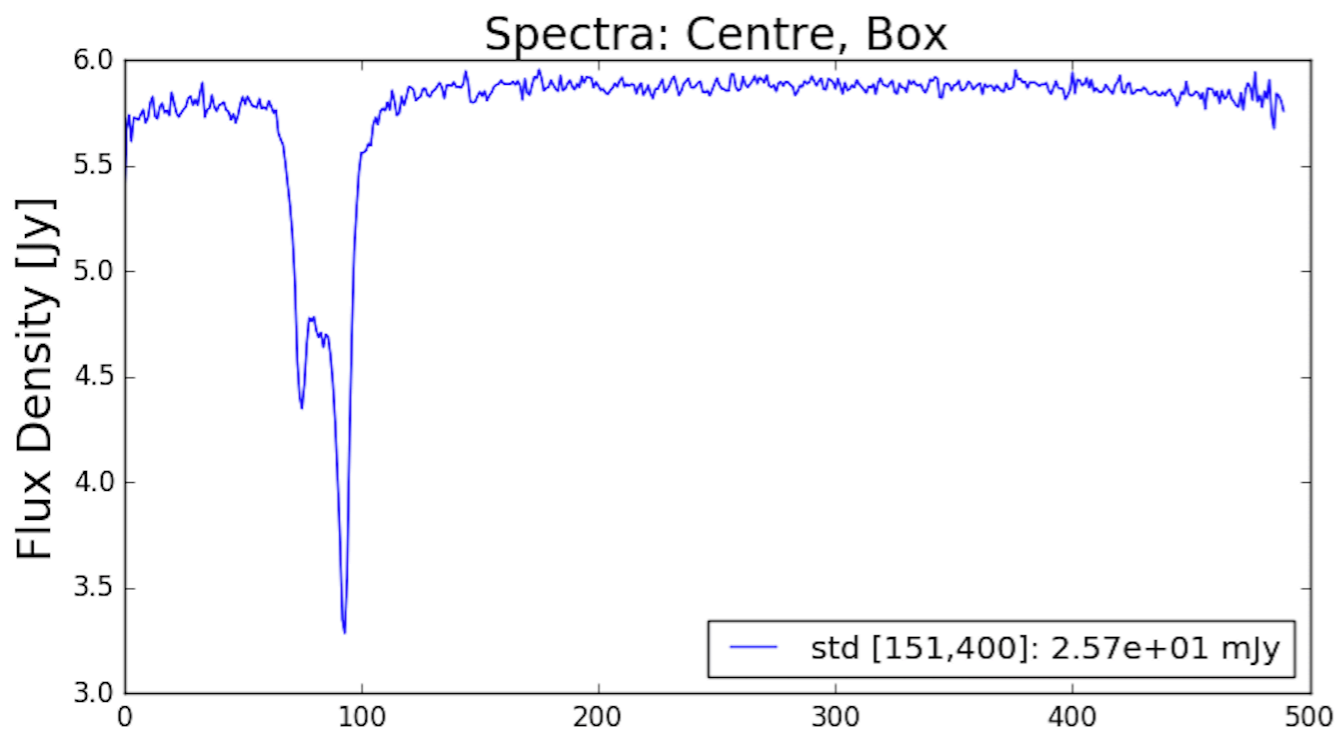


# Doppler correction II

- Necessary if you need spectral resolution  $> 1.2$  km /sec.
- This correction is for the earth's rotation during the observation.
- Task used is CVEL



# Continuum Subtraction



# Continuum Subtraction

$$V_{AB}(\nu) = V_{AB}^{cont}(\nu) + V_{AB}^{line}(\nu)$$

$$I(l, m, \nu) = I^{cont}(l, m, \nu) + I^{line}(l, m, \nu)$$

**Both baseline based [UVSUB, UVLIN]**

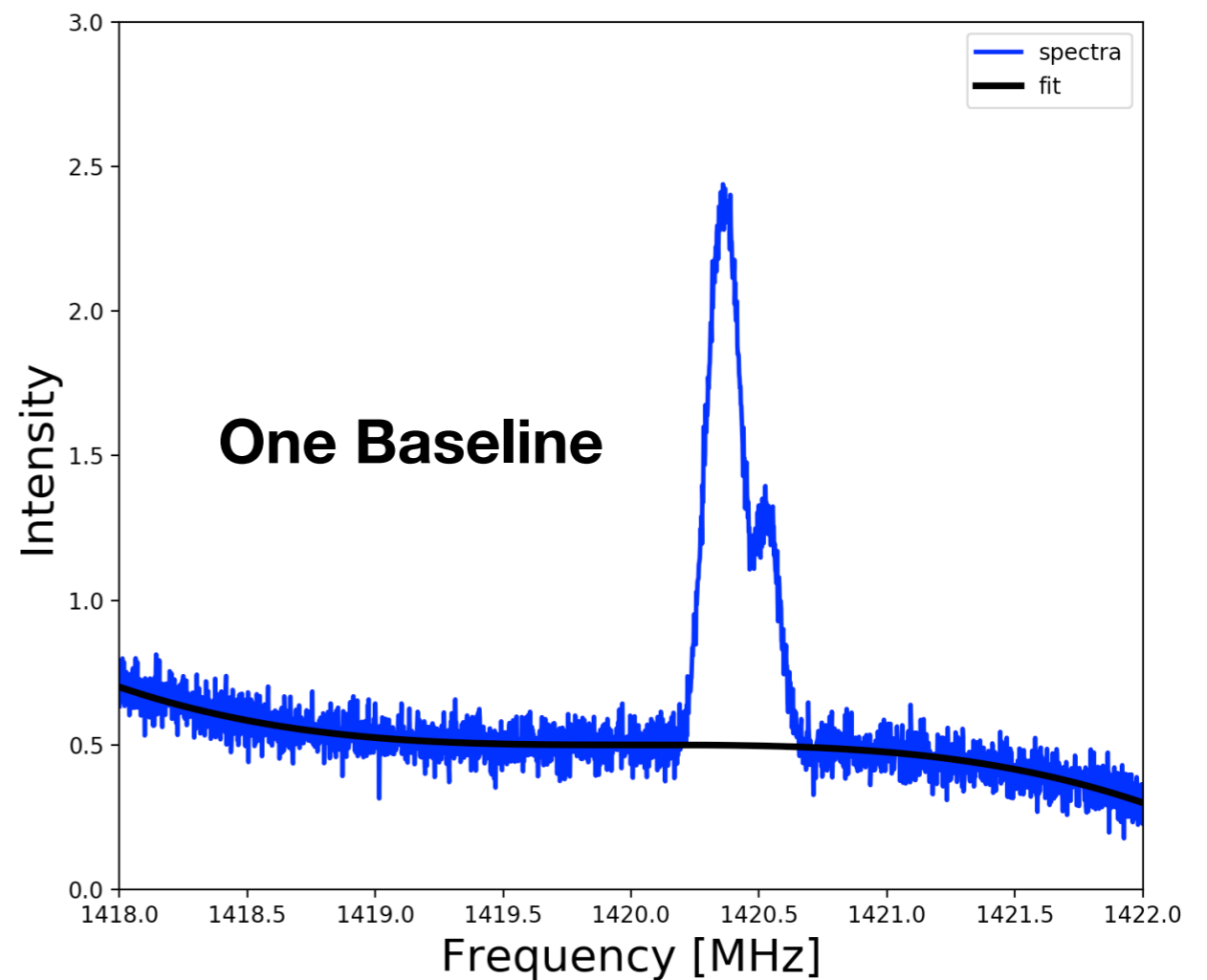
**and**

**Image based [IMLIN] algorithms exists**

# Continuum Subtraction [UVLIN]

$$V_{AB}(\nu) = V_{AB}^{cont}(\nu) + V_{AB}^{line}(\nu)$$

- Works on each baseline separately.
- Choose line free channels in the band and fit a low order polynomial.
- Identify outliers compared to the fit and FLAG those!
- Subtract the polynomial from all channels.



# Continuum Subtraction [UVLIN]

## Advantages

- No need to make an image!
- Fast algorithm.
- Automated flagging.
- Statistics of continuum is estimated.

## Disadvantages

- Assumes uniform uv coverage across frequencies
- Field of view over which works is restricted
- More residual flux away from phase centre

# Continuum Subtraction [UVLIN]

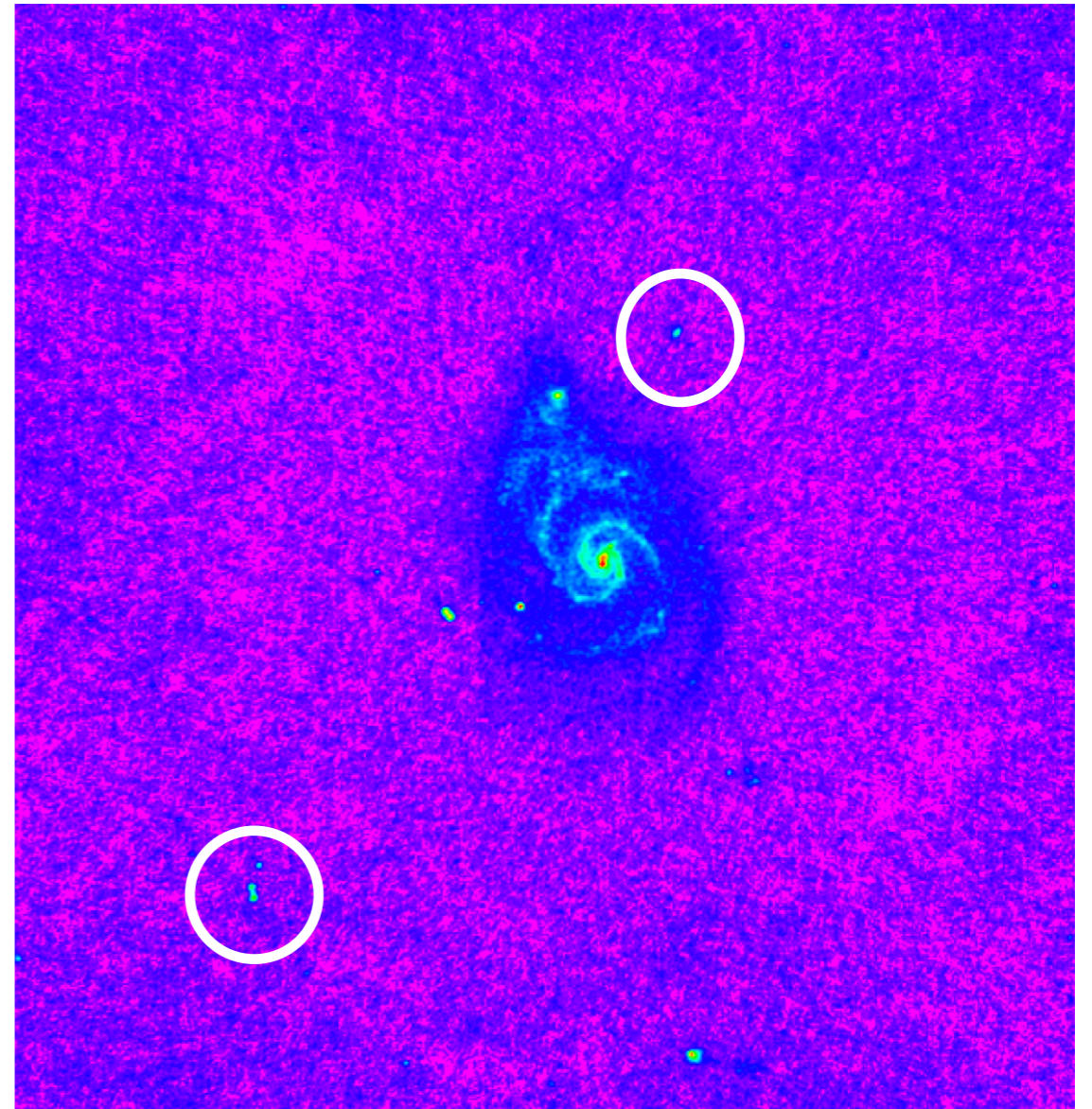
$$V(u, v, \nu) = I_0 \left[ \cos \left( \frac{2\pi \nu}{c} [b_x l_0 + b_y m_0] \right) + i \sin \left( \frac{2\pi \nu}{c} [b_x l_0 + b_y m_0] \right) \right]$$

$$\theta_S \ll \frac{\nu_0}{\Delta\nu} \theta_{beam}$$

$$\Delta S \sim S \frac{\pi^2}{36} \left( \frac{\Delta\nu}{\nu_0} \right)^2 \frac{\theta_S^2}{\theta_{beam}^2}$$

## Disadvantages

- Assumes uniform uv coverage across frequencies
- Field of view over which works is restricted
- More residual flux away from phase centre



# Continuum Subtraction [IMLIN]

- Make image for each channel ( a data cube) by deconvolving the dirty beam
- For each pixel fit a lower order polynomial across the channels and subtract the polynomial values from the same pixel at all channels
- Assumes point spread function and noise to be same across the band

$$\Delta S \sim S \frac{\pi^2}{36} \left( \frac{\Delta \nu}{\nu_0} \right)^2 \frac{(\theta - \theta_S)^2}{\theta_{beam}^2}$$

## Advantages

- Fast algorithm.
- Removes continuum at even large distance from the phase centre
- Statistics of continuum is estimated.

## Disadvantages

- Imaging problems
- Residuals scales as distance from the source
- Do not work well for extended source and not good uv-coverage

# Continuum Subtraction [UVSUB]

- Make image combining all the line free channels.
- Calculate the visibility model for the continuum image
- Subtract this model from all the channels

$$\sigma_{Line} = \sigma_0 \sqrt{1 + \frac{1}{N}}$$

**Dynamic  
Range**

$$D = \frac{I_{Cont}^{peak}}{\sigma_{Line}}$$

## Advantages

- Removes continuum at even large distance from the phase centre, residuals in the line free channels are practically zero!
- Gets robust continuum maps

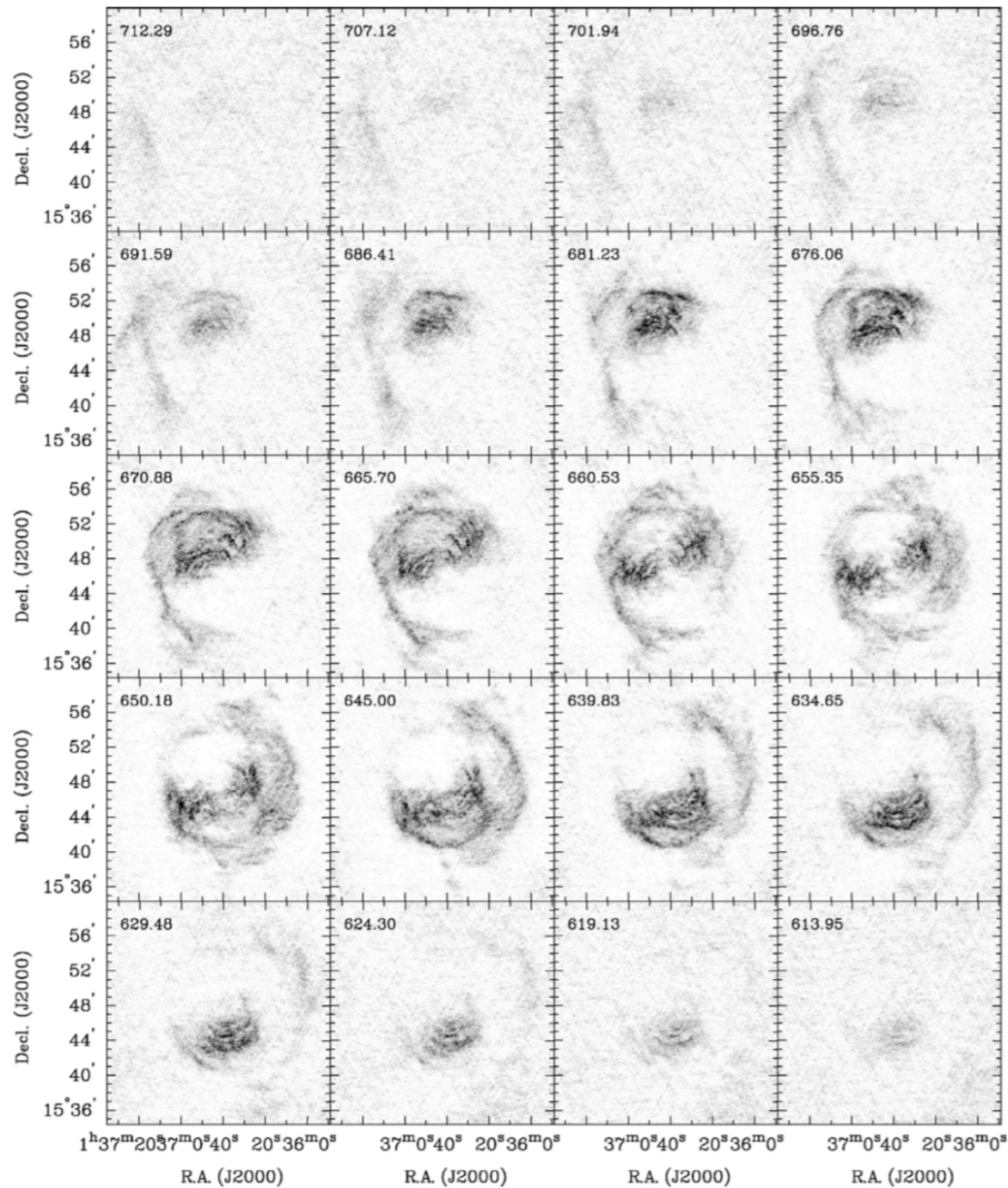
## Disadvantages

- Very slow!
- Requires good continuum image/model



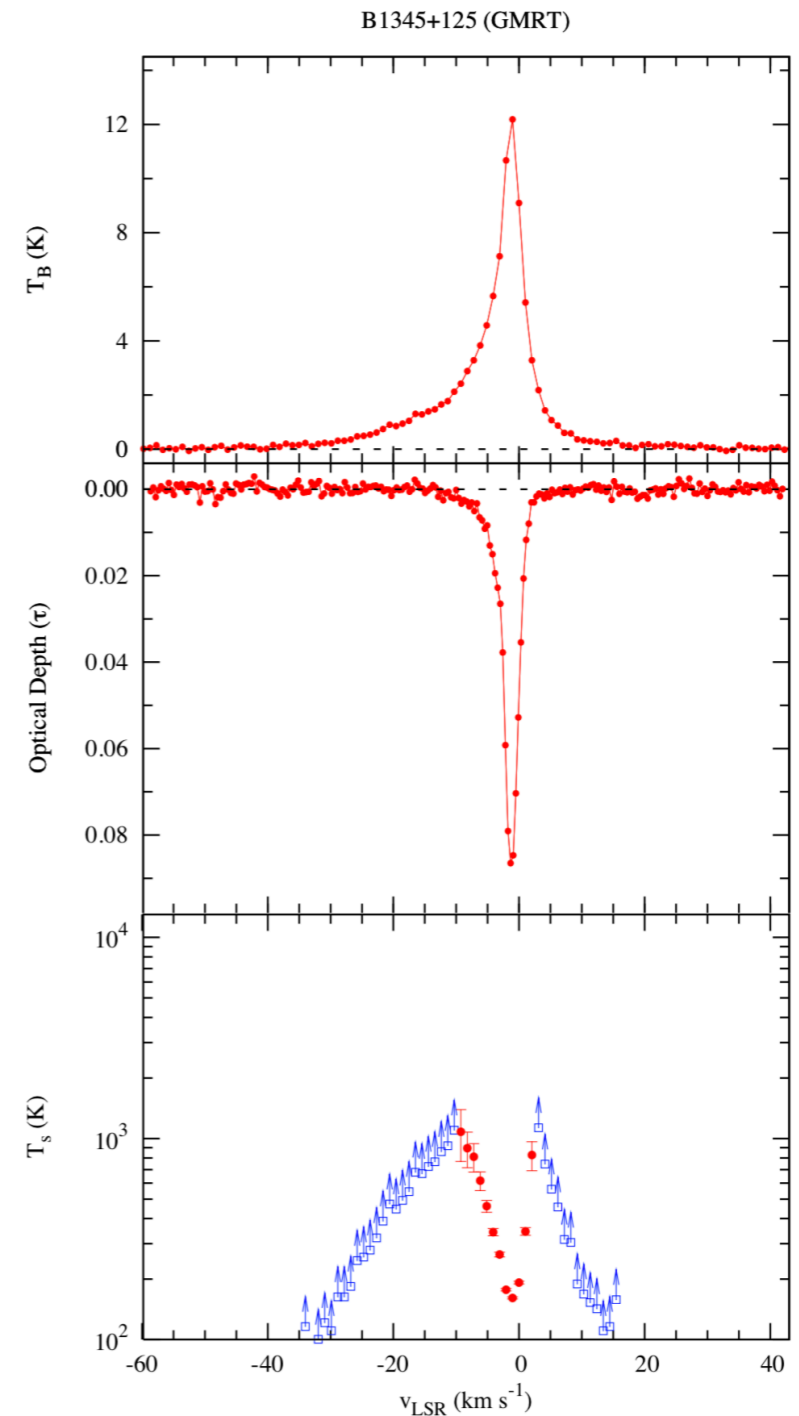
# Science Cases: Data Cube

## Extended Source: HI in Galaxy



Walter et al. (2008) ApJ, V-136, P- 2563

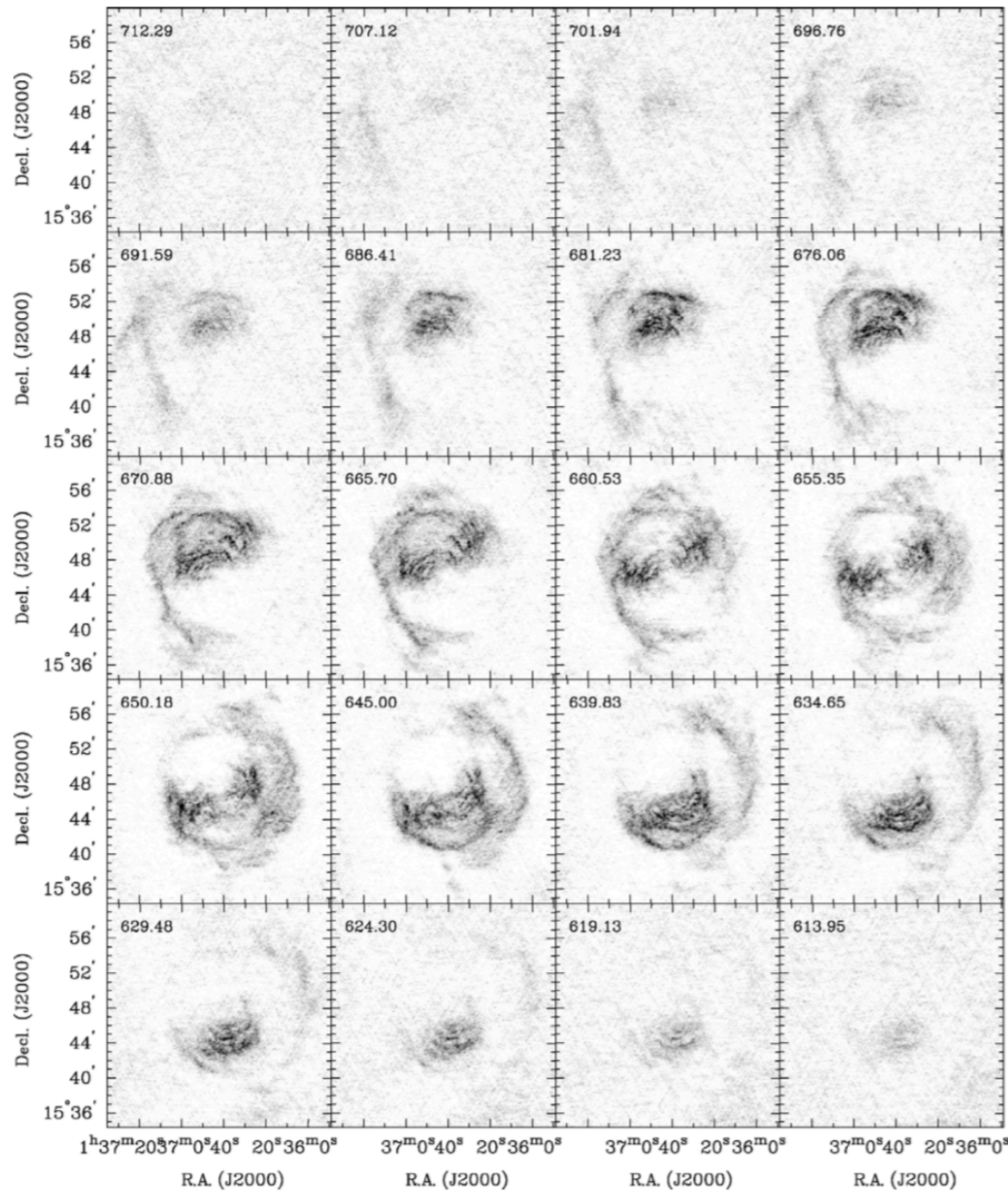
## Point Source: Galactic HI absorption



Roy et al. MNRAS, 436, 3, (2013), 2352

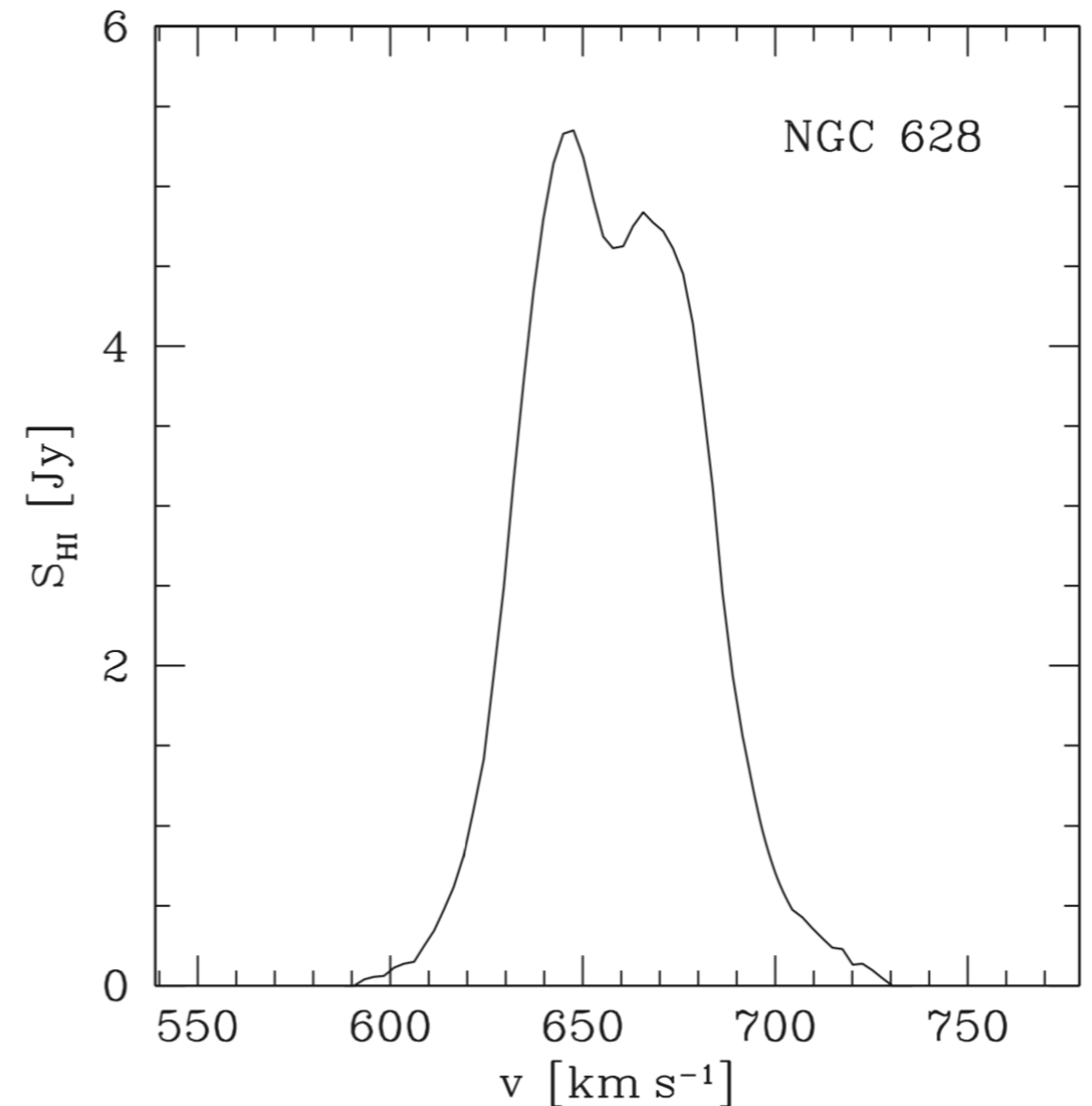
# Science Cases: HI in Galaxy

## Extended Source: HI in Galaxy

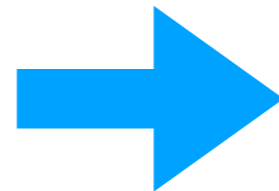
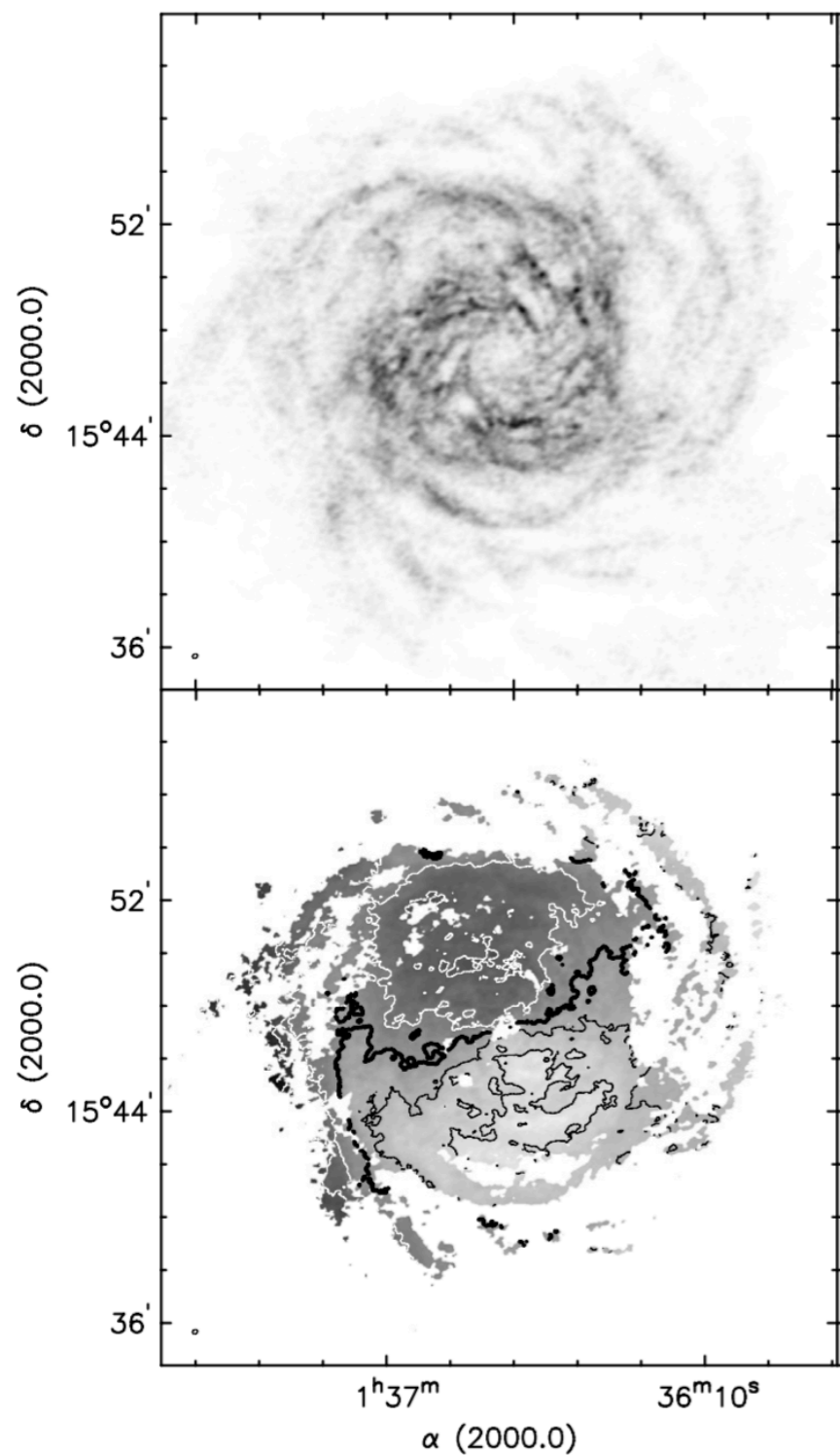


## Integrated Spectra

$$S(\nu) = \sum_{l,m} I(l, m, \nu)$$



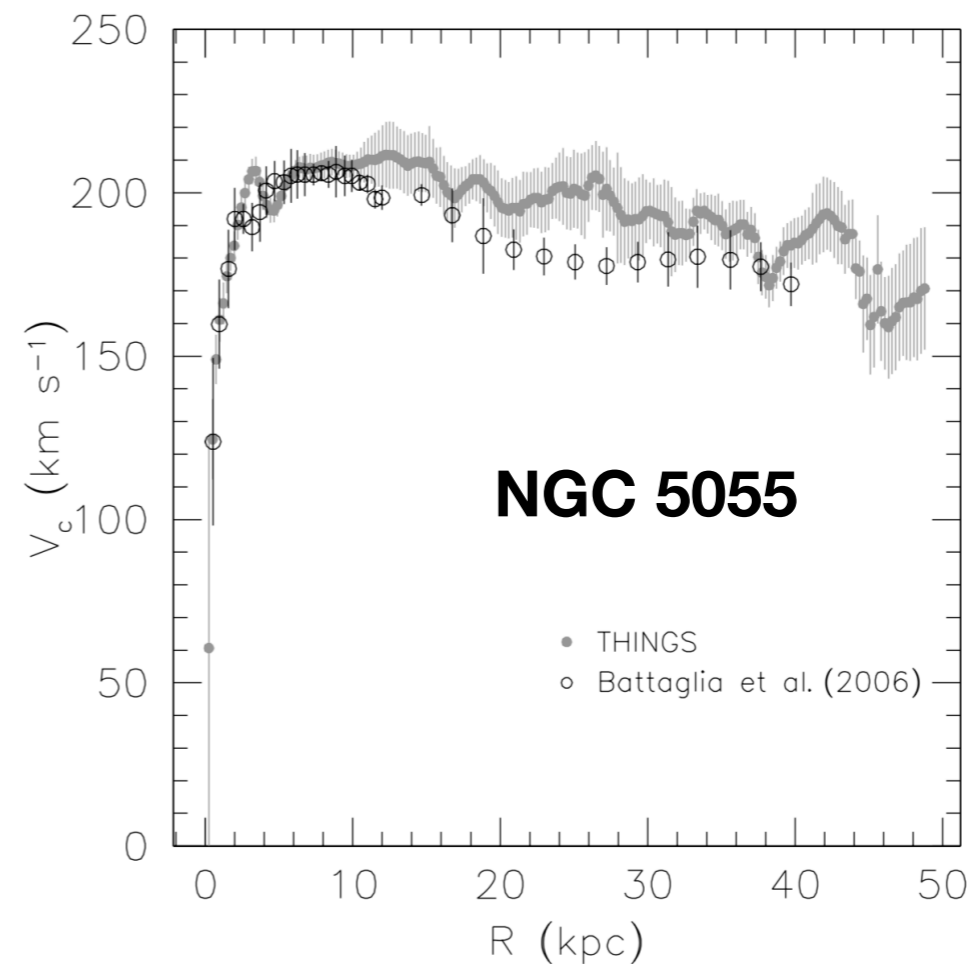
# Science Cases: HI in Galaxy



## Moment Maps

$$M_0(l, m) = \Delta\nu \sum_{i=1}^{NChan} I(l, m, \nu_i)$$

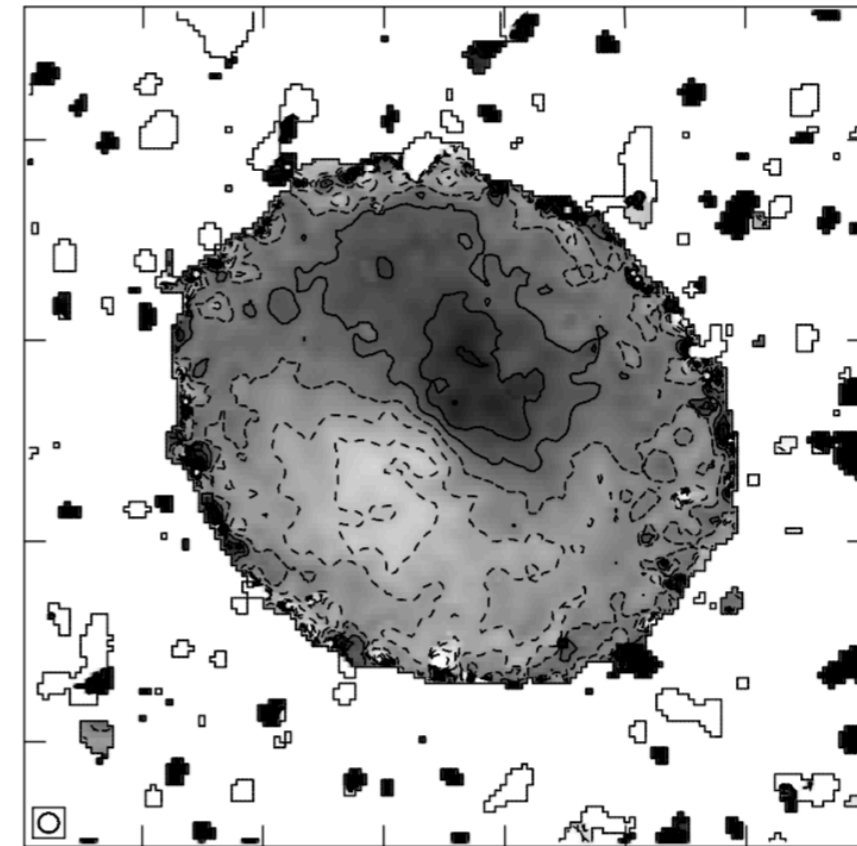
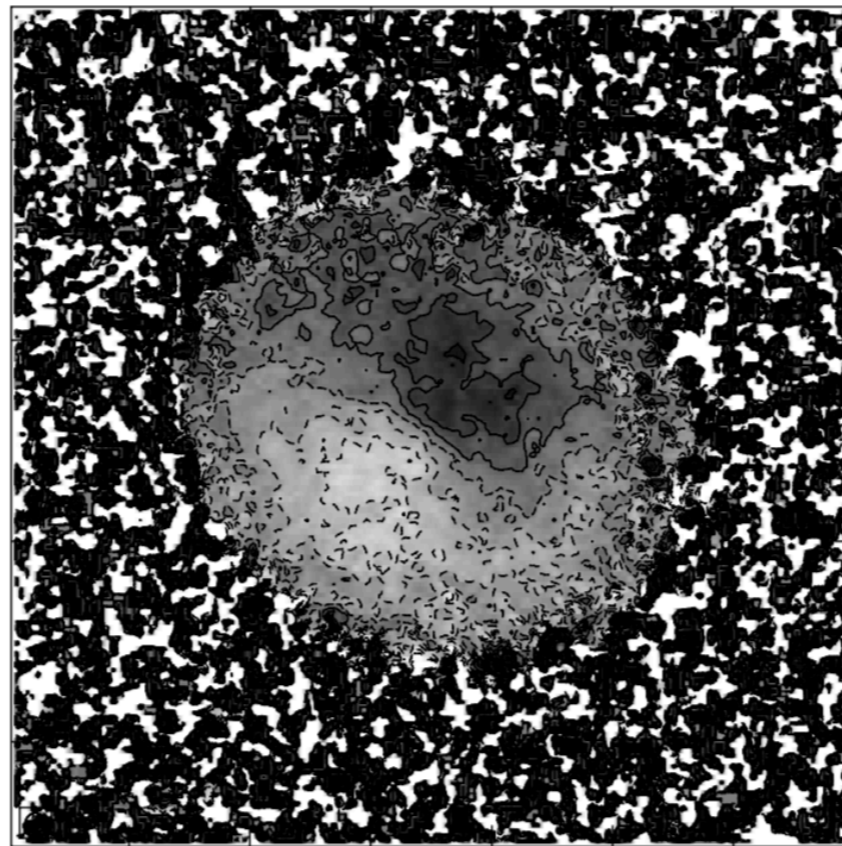
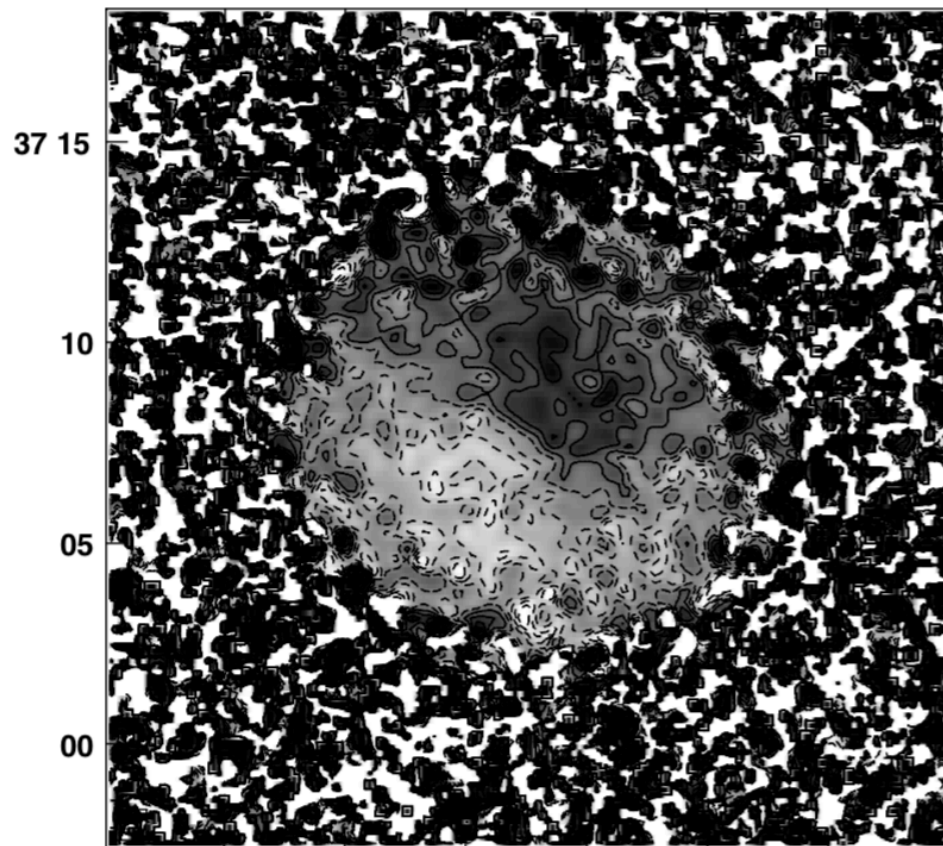
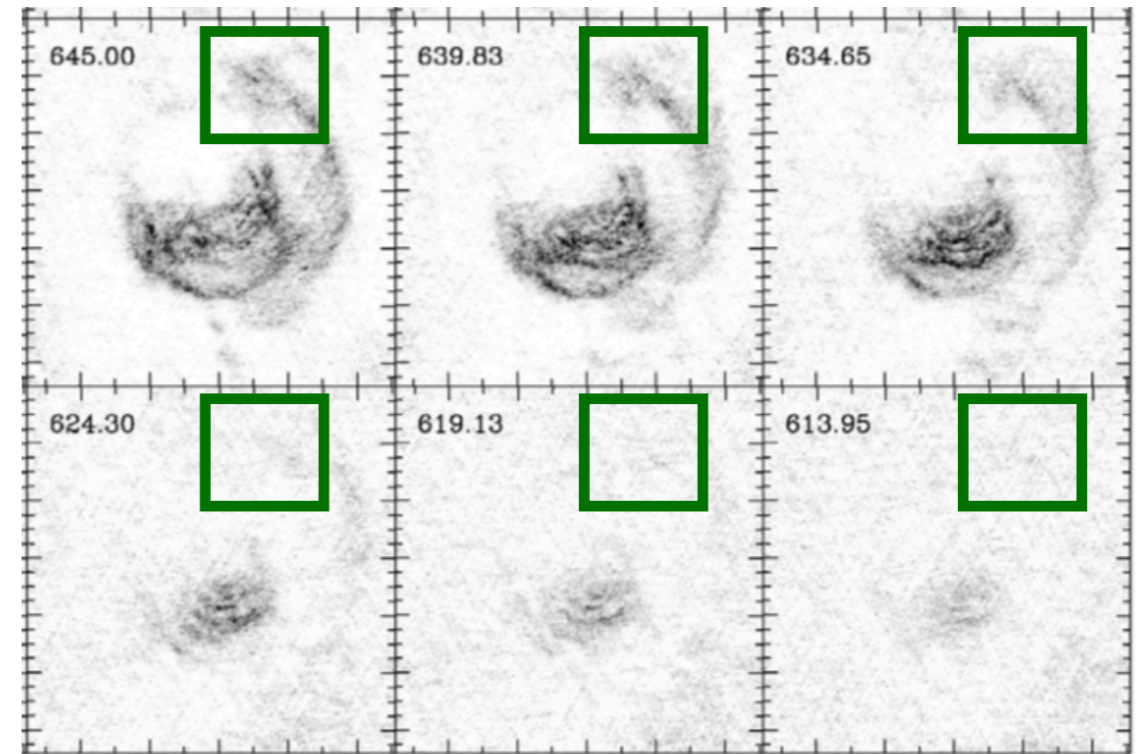
$$M_1(l, m) = \frac{\sum_{i=1}^{NChan} I(l, m, \nu) \nu_i}{\sum_{i=1}^{NChan} I(l, m, \nu_i)}$$



**Rotation Curve**

# Science Cases: HI Moments

- Use a cutoff to choose channels for moment maps.
- Average over channels and space first
- Spill over to nearby channels (from the good channels) even if the value is lower than cutoff



# What we learned ?

- Observation and Techniques with interferometers
  - Observation Preparation [Nissim again!]
  - Calibration [AIPS: POSSM, BPASS, UVFLG]
  - Doppler correction [AIPS: CVEL]
  - Continuum Subtraction [AIPS: UVSUB, UVLIN, IMLIN]
  - Map making [AIPS: IMAGR]
- Science [AIPS: ISPEC, MOMNT]